

Unitarity Triangle fit and new physics

Marcella Bona



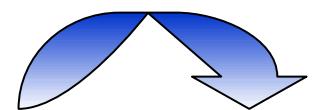
on behalf of the
UTfit Collaboration

M.B., M. Ciuchini, E. Franco, V. Lubicz,
G. Martinelli, F. Parodi, M. Pierini,
P. Roudeau, C. Schiavi, L. Silvestrini,
V. Sordini, A. Stocchi, V. Vagnoni

<http://www.utfit.org>

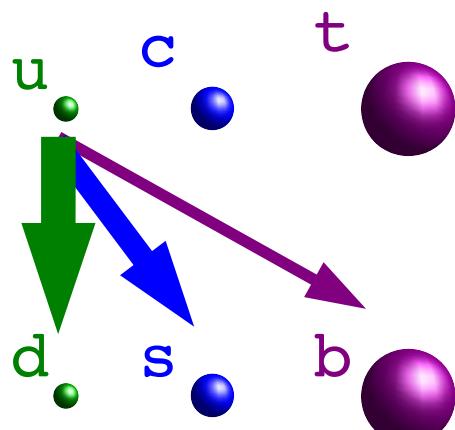
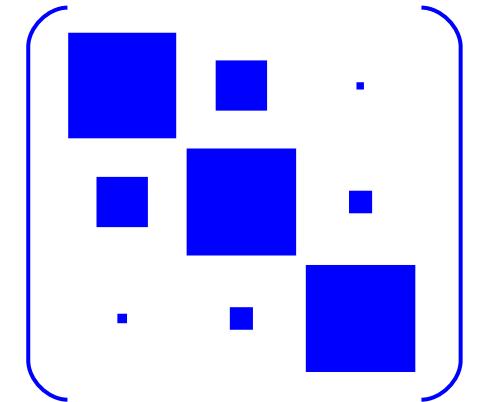


IV CKM Workshop, Nagoya, Japan
December 12th, 2006



ckm matrix and unitarity triangle

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \simeq \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\bar{\rho} - i\bar{\eta}) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \bar{\rho} - i\bar{\eta}) & -A\lambda^2 & 1 \end{pmatrix}$$



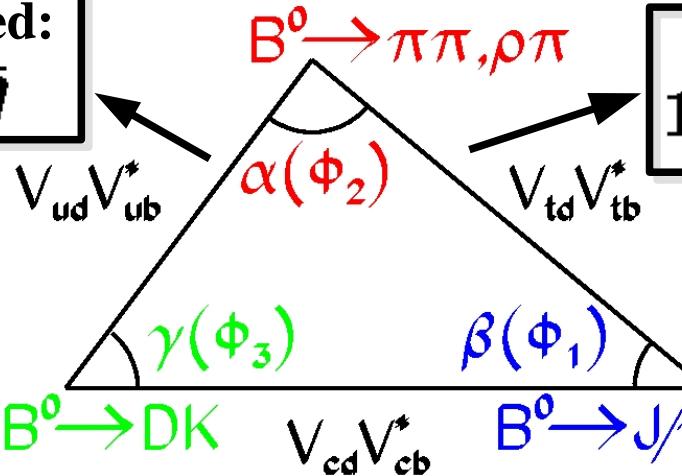
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

$$\alpha = \pi - \beta - \gamma$$

normalized:
 $\bar{\rho} + i\bar{\eta}$

normalized:
 $1 - \bar{\rho} - i\bar{\eta}$

$$\gamma = \text{atan} \left(\frac{\bar{\eta}}{\bar{\rho}} \right)$$



many observables
functions of $\bar{\rho}$ ed $\bar{\eta}$:
overconstraining

$$\beta = \text{atan} \left(\frac{\bar{\eta}}{(1 - \bar{\rho})} \right)$$

outline

see:
G. Martinelli
in this session

- + summary of the SM fit (very quickly)
- + few words on the "tension" (also very quickly)
- + new physics with the model independent analysis:
 - yellow new *new-physics*-oriented constraints
 - yellow results in **K**, **B_d**, **B_s** sectors for NP parameters
- + MFV scenario analysis and results

the method and the inputs:

Bayes Theorem

$$f(\bar{\rho}, \bar{\eta}, X | c_1, \dots, c_m) \sim \prod_{j=1,m} f_j(c_j | \bar{\rho}, \bar{\eta}, X) * \prod_{i=1,N} f_i(x_i) f_0(\bar{\rho}, \bar{\eta})$$

$X \equiv x_1, \dots, x_n = m_t, B_K, F_B, \dots$

$\mathcal{C} \equiv c_1, \dots, c_m = \epsilon, \Delta m_d / \Delta m_s, A_{CP}(J/\psi K_S), \dots$

$(b \rightarrow u)/(b \rightarrow c)$

$\bar{\rho}^2 + \bar{\eta}^2$

$\bar{\Lambda}, \lambda_1, F(1), \dots$

ϵ_K

$\bar{\eta}[(1 - \bar{\rho}) + P]$

B_K

Δm_d

$(1 - \bar{\rho})^2 + \bar{\eta}^2$

$f_B^2 B_B$

$\Delta m_d / \Delta m_s$

$(1 - \bar{\rho})^2 + \bar{\eta}^2$

ξ

$A_{CP}(J/\psi K_S)$

$\sin 2\beta$

Standard Model +
OPE/HQET/
Lattice QCD
to go
from quarks
to hadrons

m_t

M. Bona *et al.* (UTfit Collaboration)
JHEP 0507:028,2005 hep-ph/0501199

M. Bona *et al.* (UTfit Collaboration)
JHEP 0603:080,2006 hep-ph/0509219

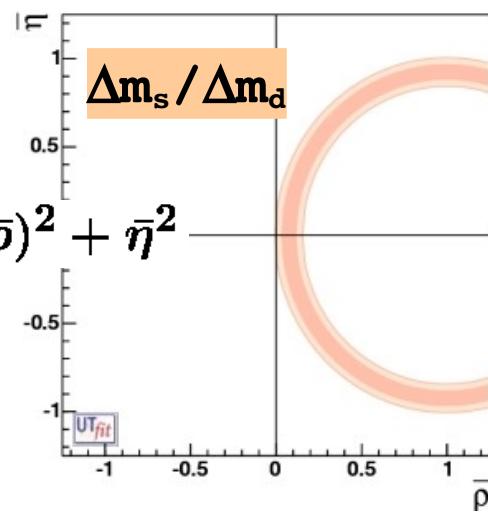
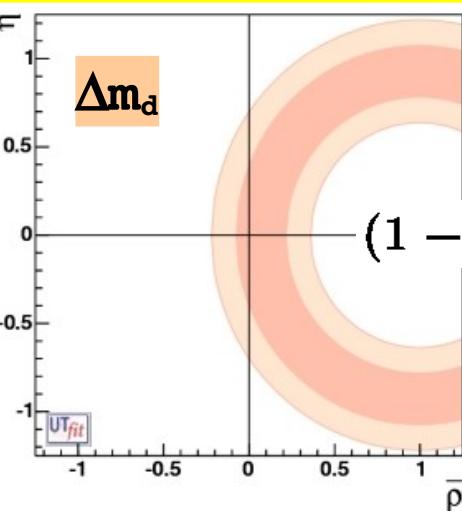
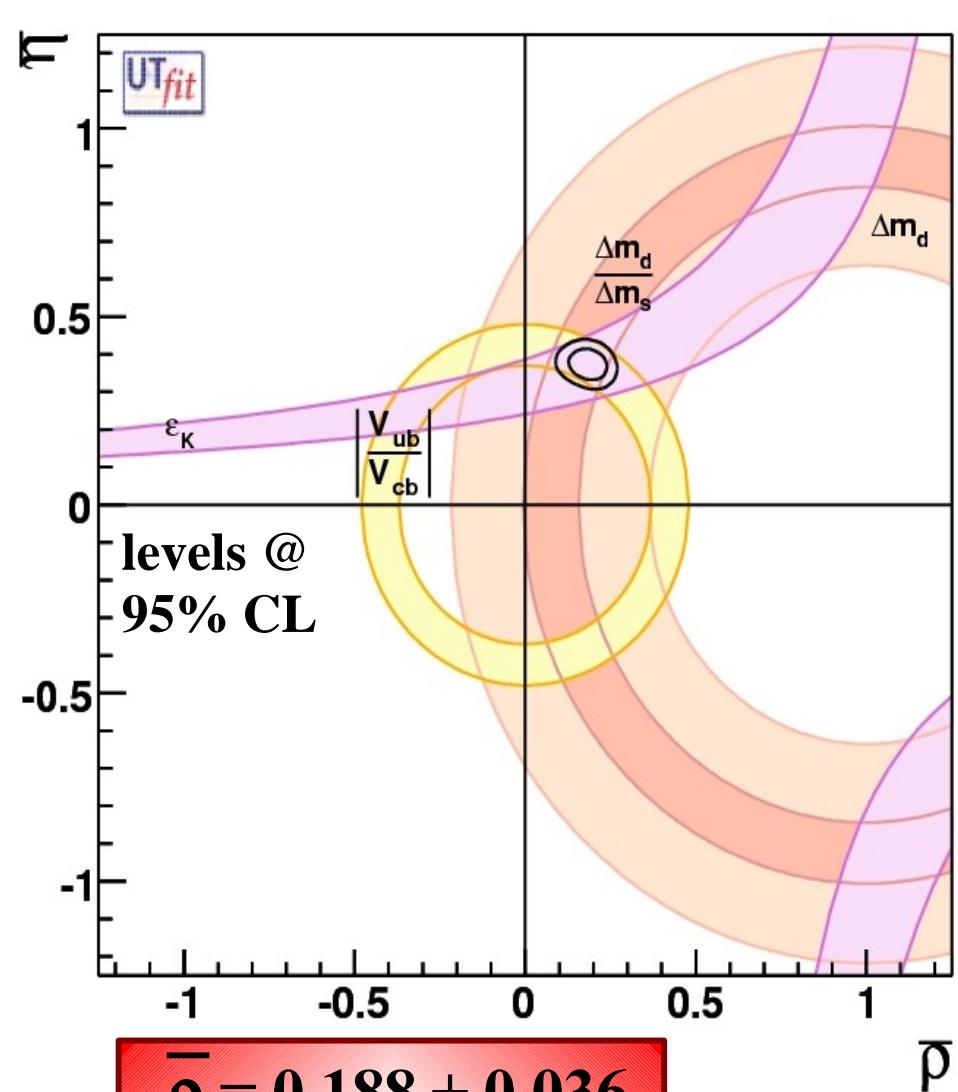
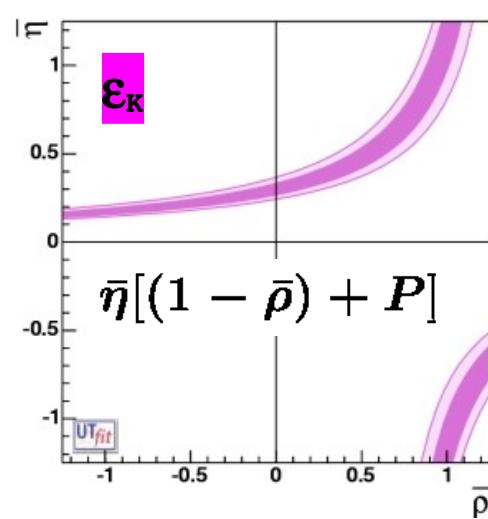
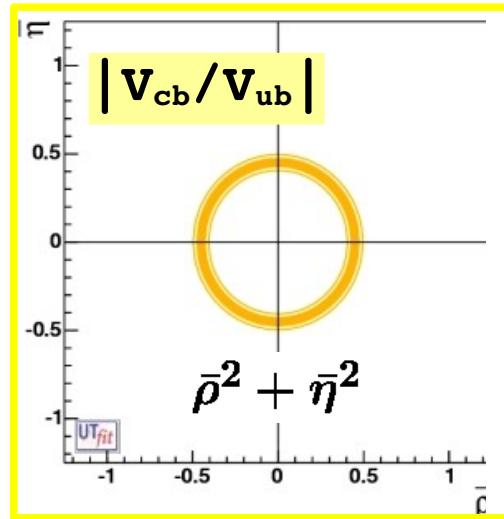
see also:

G. Martinelli at this session,

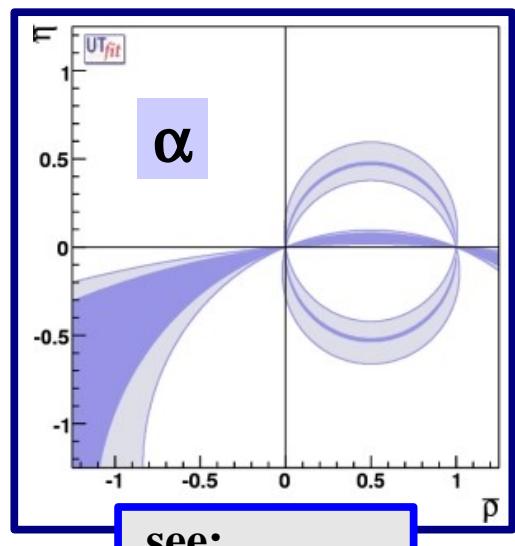
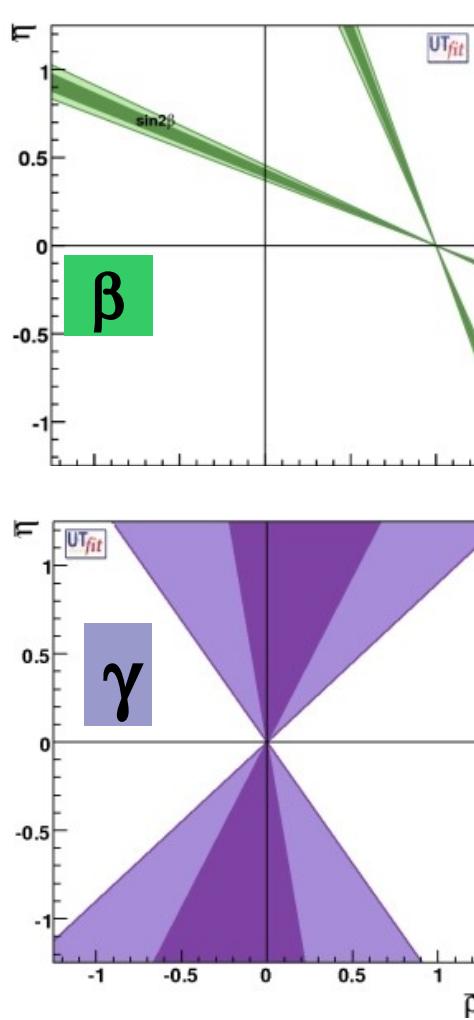
V. Lubicz at WG4 (Wed 13)

M. Pierini at WG joint session (Thur 14)

LEP-style analysis in the ρ - η plane:

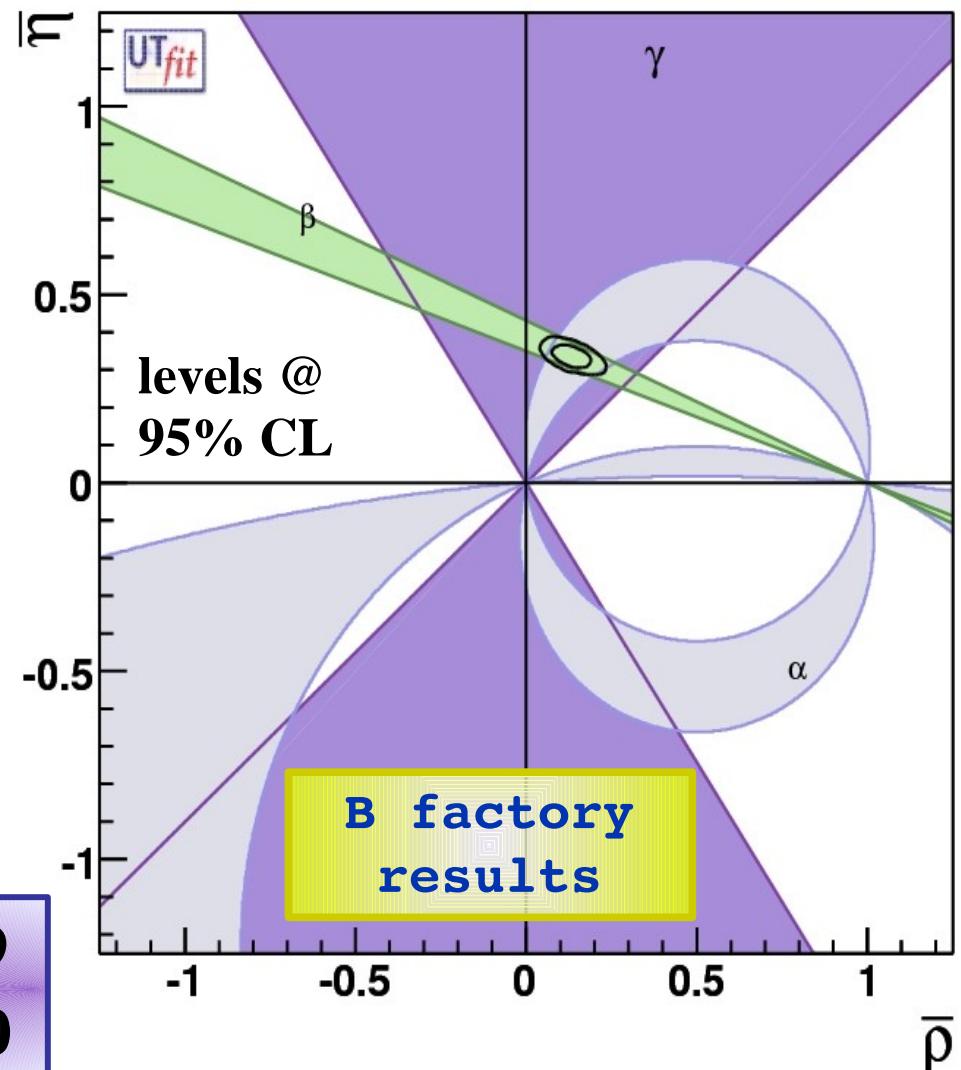


angle constraints in the ρ - η plane:



$$\bar{\rho} = 0.134 \pm 0.039$$

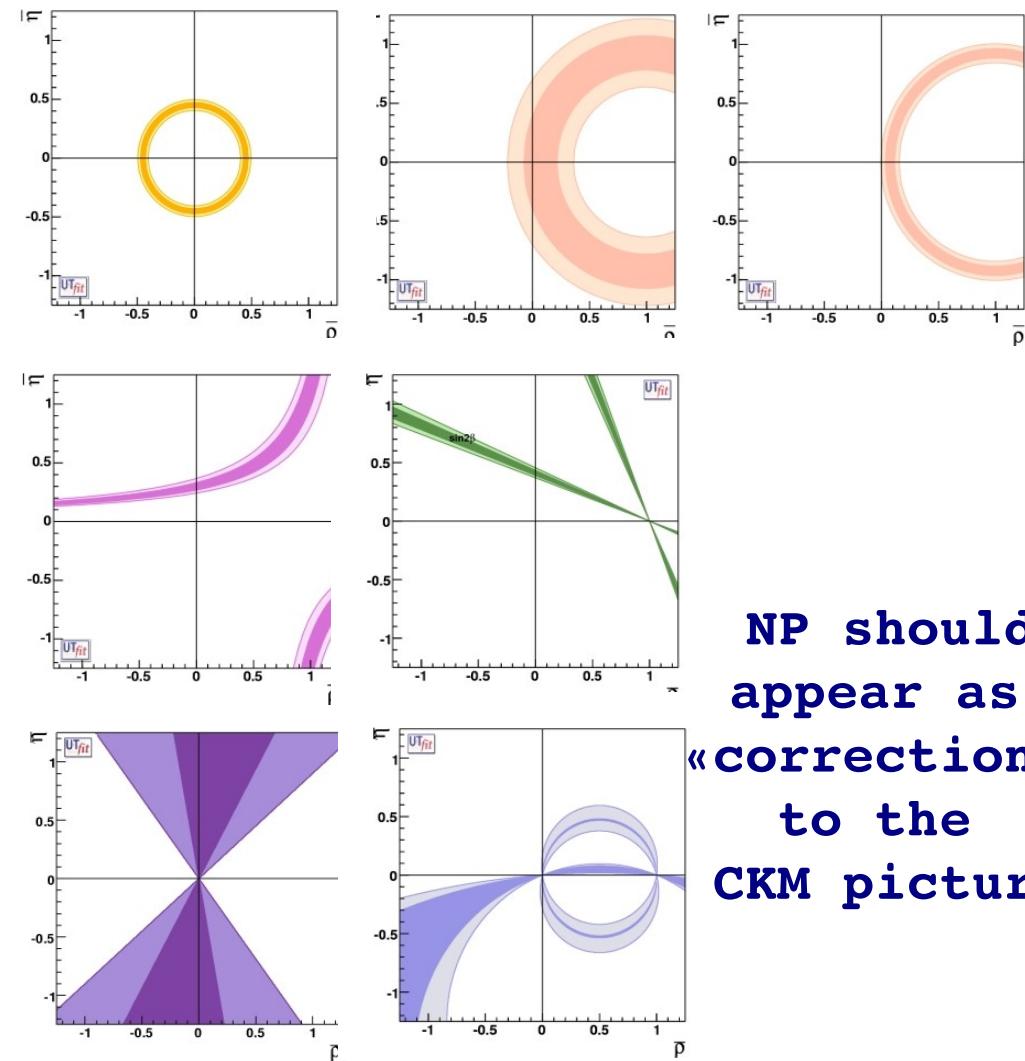
$$\eta = 0.335 \pm 0.020$$



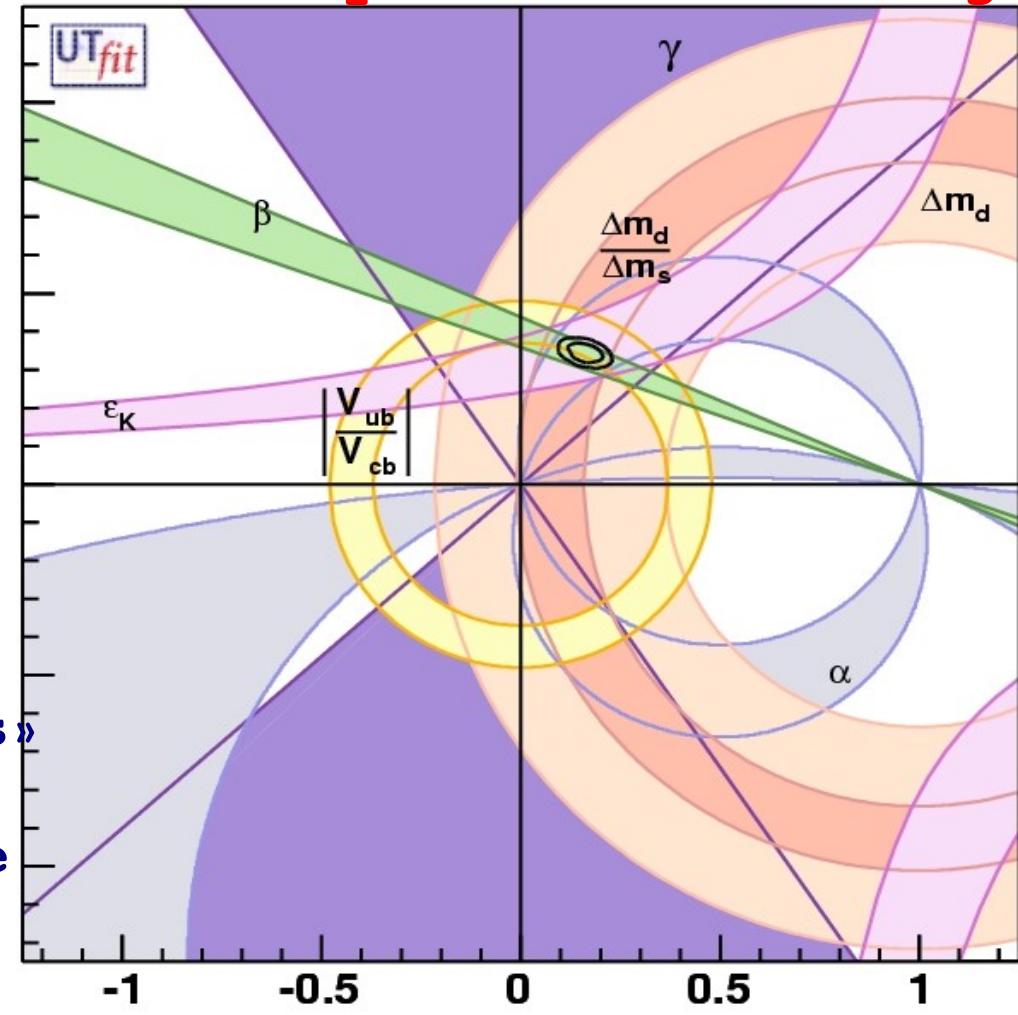
the global fit:

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JHEP 0507:028,2005 hep-ph/0501199

<http://www.utfit.org>



NP should
appear as
«corrections»
to the
CKM picture

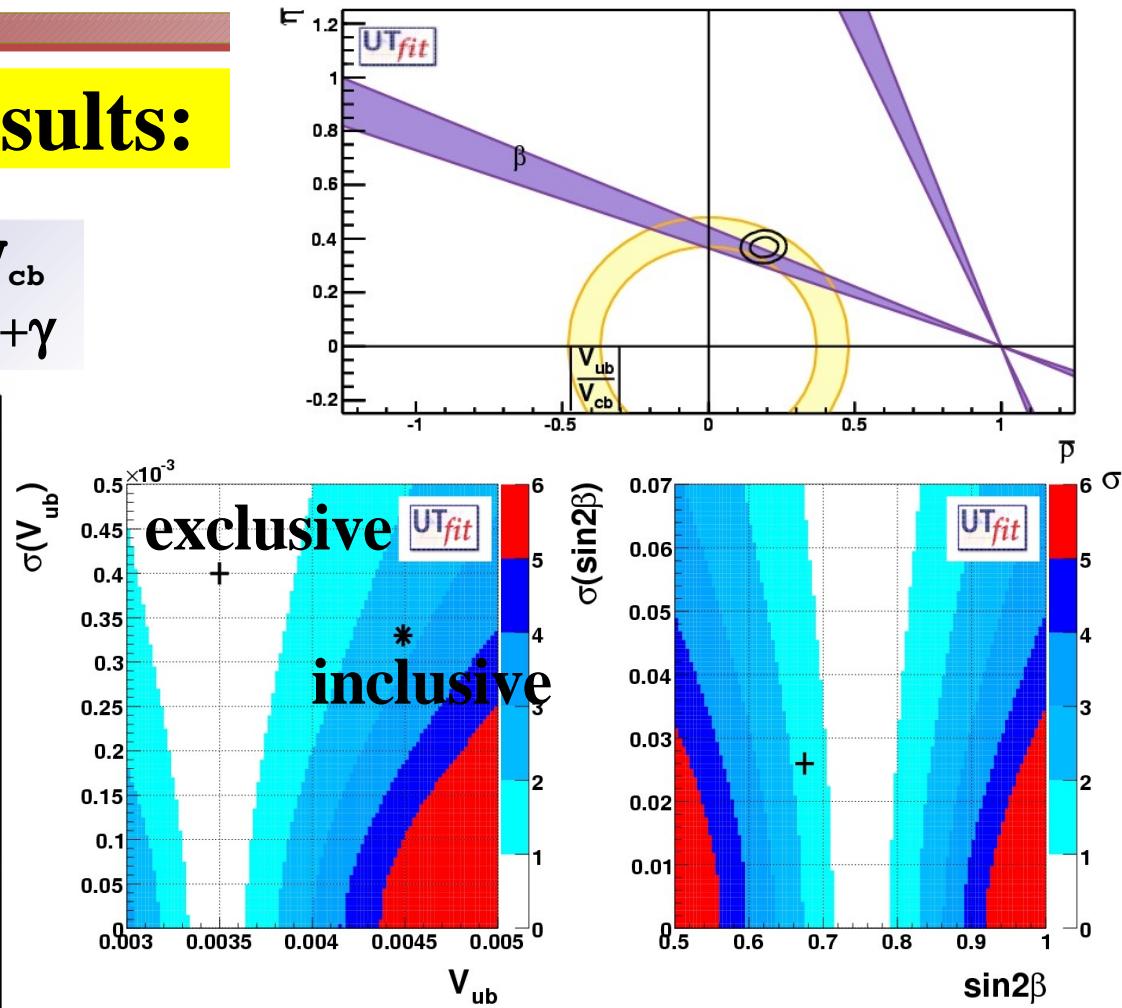
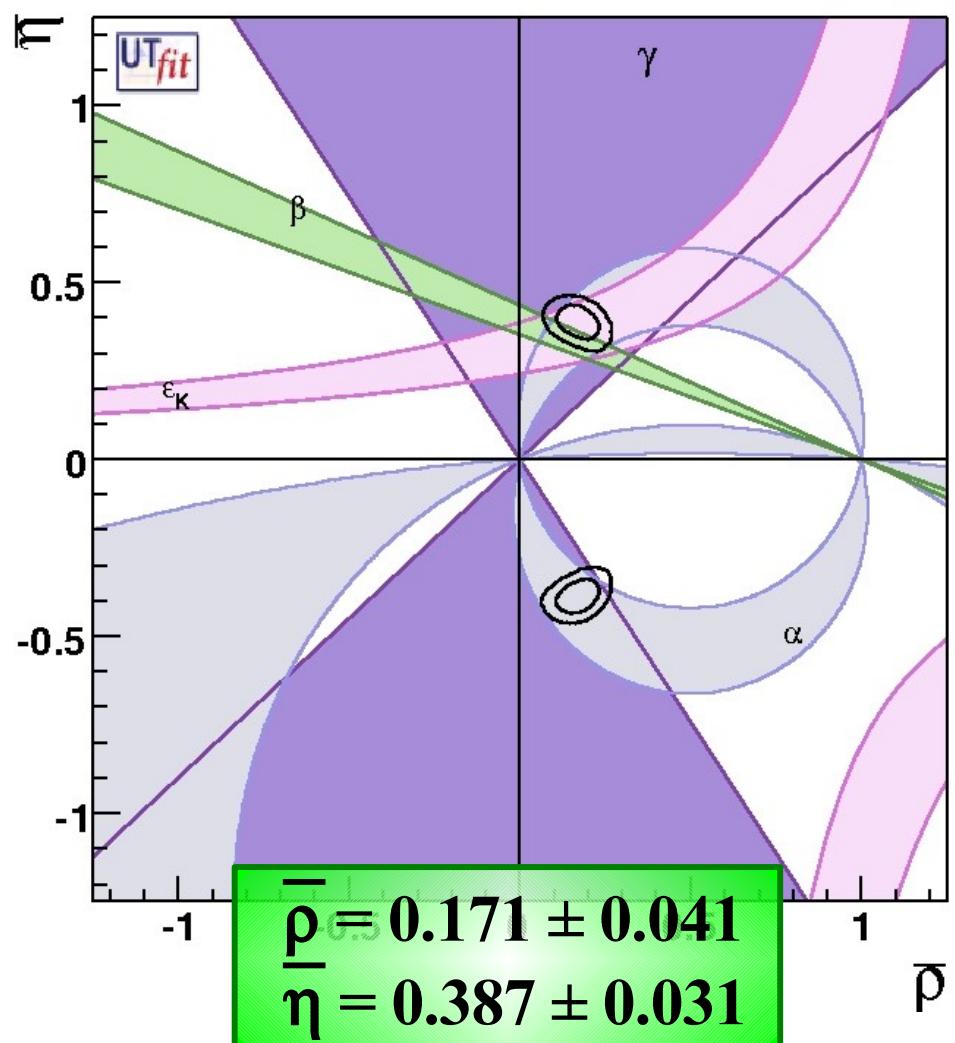


$$\bar{\rho} = 0.163 \pm 0.028$$

$$\bar{\eta} = 0.344 \pm 0.016$$

tension in the current results:

in the fit: $\Delta m_d + \Delta m_s + V_{ub} + V_{cb}$
 compared to: $\varepsilon_k + \beta + \alpha + \gamma + 2\beta + \gamma$

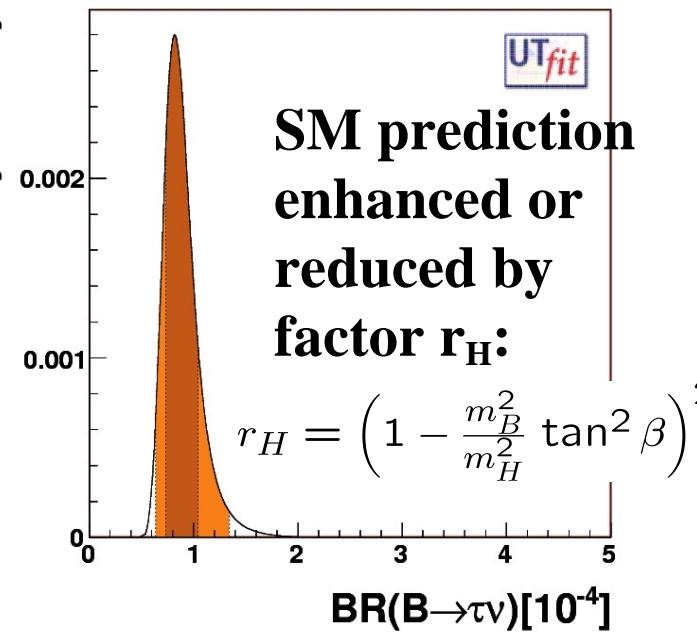


from indirect determination
 $V_{ub} = (3.48 \pm 0.20) 10^{-3}$

$\sin 2\beta = 0.752 \pm 0.038$
 from indirect determination

indirect measurement exploiting V_{ub}

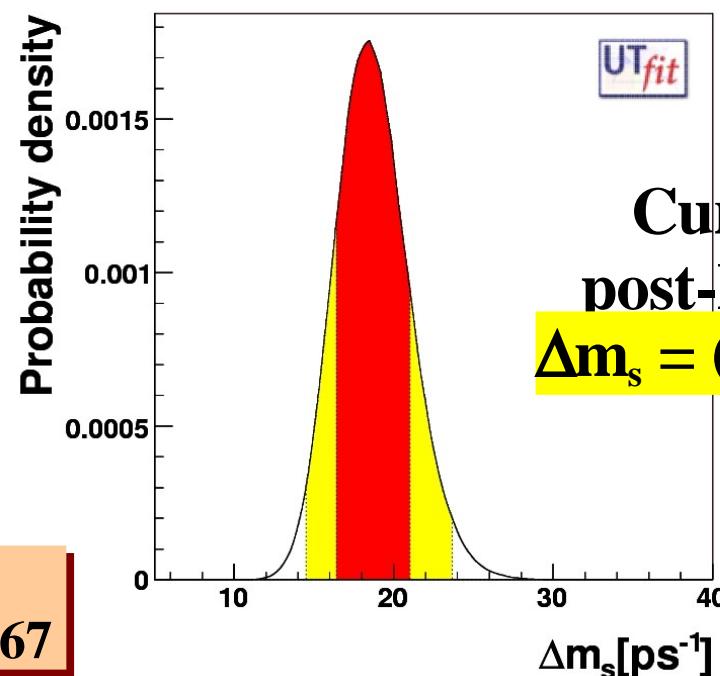
(Best SM prediction)



$f_B = (190 \pm 14) \text{ MeV}$ [UTA]	$BR(B \rightarrow \tau \nu_\tau) = (0.89 \pm 0.16) \cdot 10^{-4}$
$V_{ub} = (36.7 \pm 1.5) \cdot 10^{-4}$ [UTA]	
$f_B = (189 \pm 27) \text{ MeV}$ [LQCD]	$BR(B \rightarrow \tau \nu_\tau) = (0.84 \pm 0.30) \cdot 10^{-4}$
$V_{ub} = (35.0 \pm 4.0) \cdot 10^{-4}$ [Exclusive]	
$f_B = (189 \pm 27) \text{ MeV}$ [LQCD]	$BR(B \rightarrow \tau \nu_\tau) = (1.39 \pm 0.44) \cdot 10^{-4}$
$V_{ub} = (44.9 \pm 3.3) \cdot 10^{-4}$ [Inclusive]	
From $BR(B \rightarrow \tau \nu_\tau)$ and V_{ub} (UTA): $f_B = (237 \pm 37) \text{ MeV}$	

Same game with Δm_s :
ICHEP06 values

Δm_{sAll}	$(19.4 \pm 2.5) \text{ ps}^{-1}$
$\Delta m_{sV_{ub}(incl)}$	$(20.3 \pm 2.5) \text{ ps}^{-1}$
$\Delta m_{sV_{cb}(expl)}$	$(18.3 \pm 2.0) \text{ ps}^{-1}$



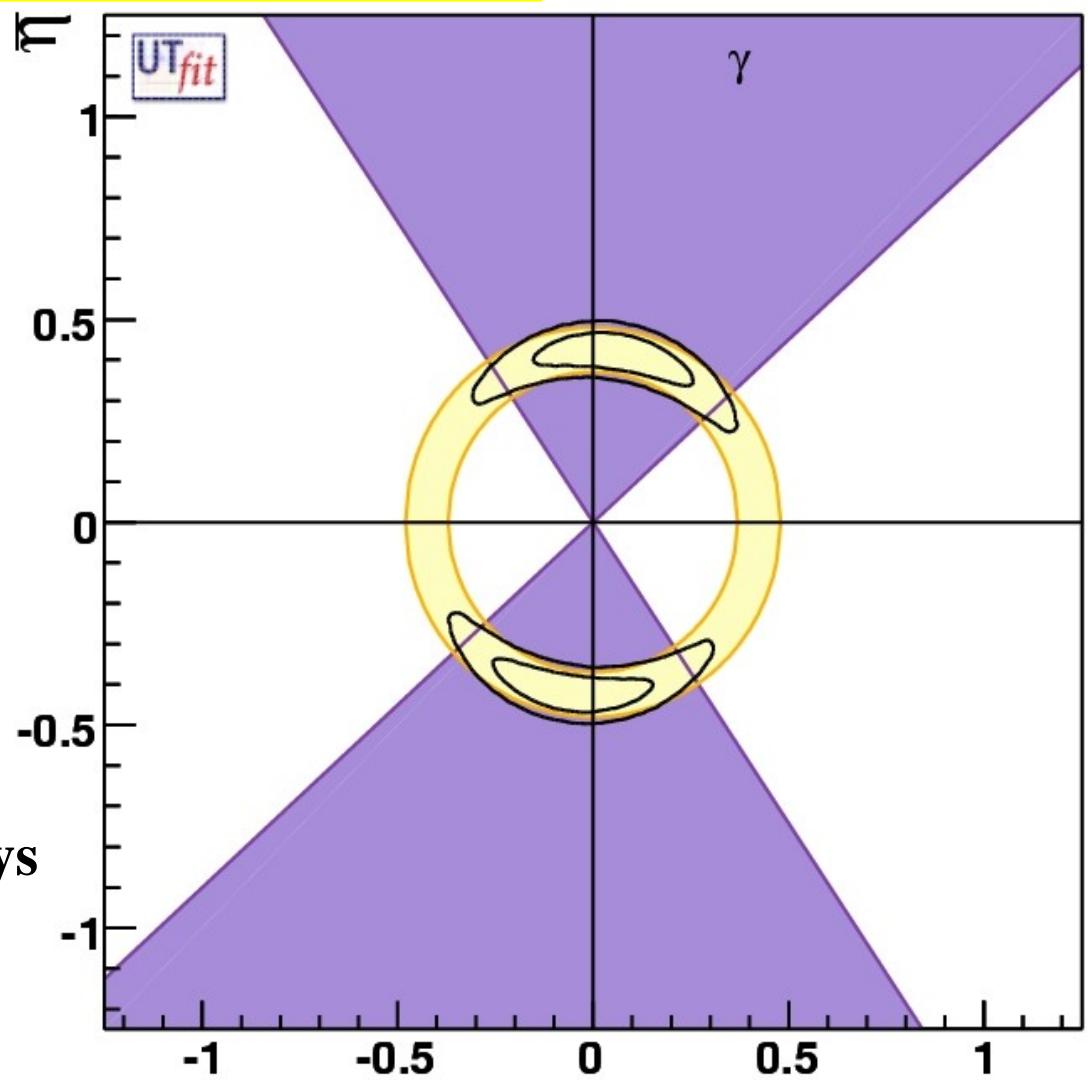
fit with NP-independent constraints

using Tree-level processes
assumed to be NP free
**the effect of the \bar{D}^0 - D^0 mixing
is negligible wrt the actual error*

$$\bar{\rho} = \pm 0.00 \pm 0.15$$

$$\bar{\eta} = \pm 0.41 \pm 0.04$$

very important to improve:
 • V_{ub}/V_{cb} from semileptoic decays
 • γ from tree level processes



reference starting point
for NP model building

model independent analysis

New Physics in $\Delta F=2$ amplitudes can be parameterized in a simple general form:

$$C_{B_q} e^{2i\phi_{B_d}} = \frac{\langle \bar{B}_q^0 | H_{eff}^{full} | \bar{B}_q^0 \rangle}{\langle \bar{B}_q^0 | H_{eff}^{SM} | \bar{B}_q^0 \rangle}, \quad (q=d, s)$$

$$C_{\epsilon_K} = \frac{\Im[\langle K^0 | H_{eff}^{full} | \bar{K}^0 \rangle]}{\Im[\langle K^0 | H_{eff}^{SM} | \bar{K}^0 \rangle]}$$

model independent assumptions

J. M. Soares and L. Wolfenstein, Phys. Rev. D 47 (1993) 1021;

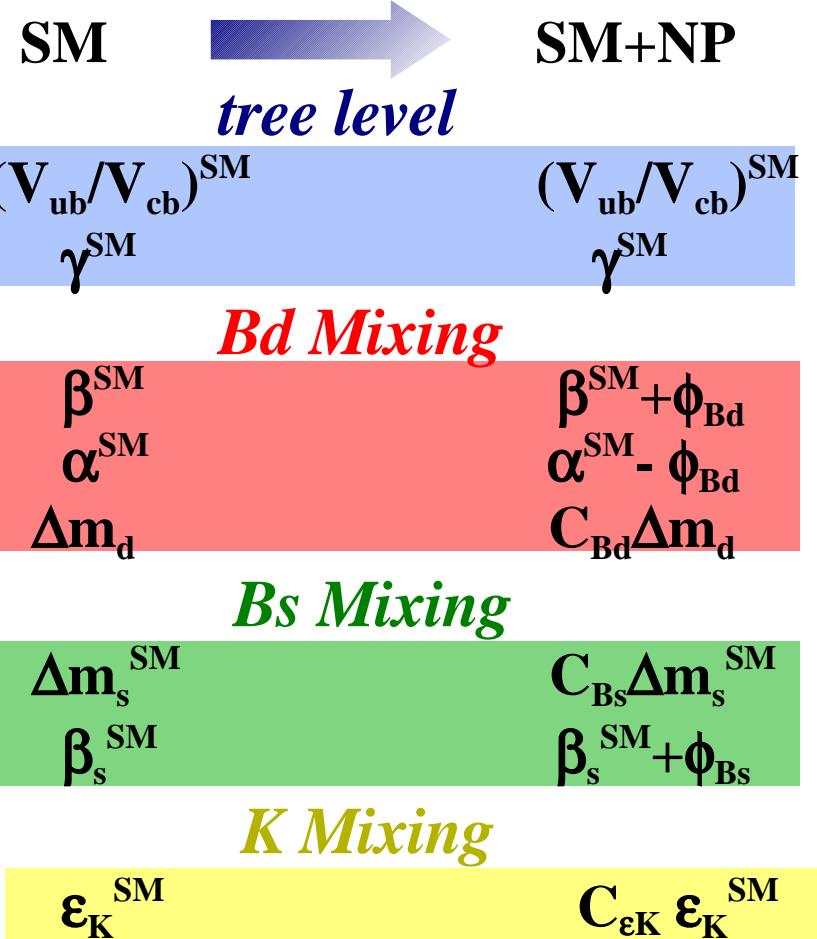
N. G. Deshpande, B. Dutta and S. Oh, Phys. Rev. Lett. 77 (1996) 4499

[arXiv:hep-ph/9608231]

J. P. Silva and L. Wolfenstein, Phys. Rev. D 55 (1997) 5331 [arXiv:hep-ph/9610208]

A. G. Cohen *et al.*, Phys. Rev. Lett. 78 (1997) 2300 [arXiv:hep-ph/9610252]

Y. Grossman, Y. Nir and M. P. Worah, Phys. Rev. Lett. B 407 (1997) 307
[arXiv:hep-ph/9704287]



M. Bona *et al.* (UTfit Collaboration)
JHEP 0603:080,2006 hep-ph/0509219

model independent approach in the fit

Using

$$|V_{ub}/V_{cb}|$$

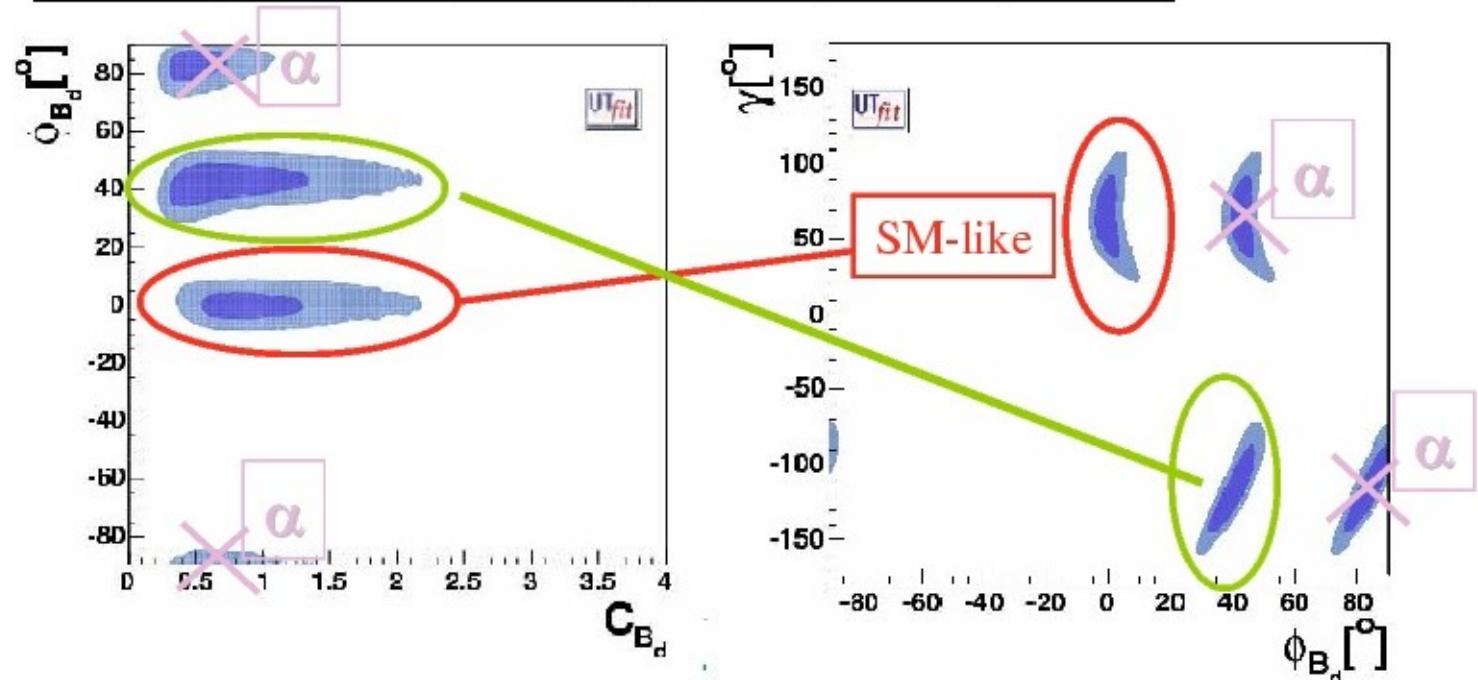
$$\Delta m_d$$

$$\epsilon_K$$

$$A_{CP}(J/\psi K^0)$$

$$\gamma(DK)$$

	γ	C_d	$\cos 2(\beta + \phi)$	$\sin 2(\alpha - \phi)$	$\sin(2\beta + \phi)$	A_{SL}
SM-LIKE	60°	1	0.68	-0.23	0.96	OK
NP1	60°	1	-0.68	0.96	-0.23	OK
NP2	-120°	0.4	0.68	-0.23	-0.96	10^{-2}
NP3	-120°	0.4	-0.68	0.96	0.23	OK



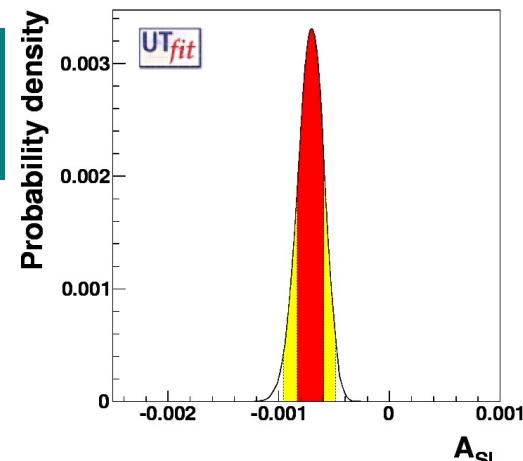
so we have to add $\longrightarrow \alpha, \cos 2\beta, A_{SL}, A_{CH}, \dots$

SM prediction
 $(-1.06 \pm 0.09) 10^{-3}$

A_{SL} in B_d decays

This is the only observable that is sensitive to NP effect on both size and phase of B mixing

$$\begin{aligned} A_{\text{SL}} &\equiv \frac{\Gamma(\bar{B}^0 \rightarrow \ell^+ X) - \Gamma(B^0 \rightarrow \ell^- X)}{\Gamma(\bar{B}^0 \rightarrow \ell^+ X) + \Gamma(B^0 \rightarrow \ell^- X)} \\ &= -\text{Re} \left(\frac{\Gamma_{12}}{M_{12}} \right)^{\text{SM}} \frac{\sin 2\phi_{B_d}}{C_{B_d}} + \text{Im} \left(\frac{\Gamma_{12}}{M_{12}} \right)^{\text{SM}} \frac{\cos 2\phi_{B_d}}{C_{B_d}} \end{aligned}$$



Direct measurement

new average = $(0.8 \pm 5.6) 10^{-3}$
(large values in case of new physics)

A_{CH} in B_{d,s} decays

First available bound on \bar{B}_s -Bs mixing phase

$$A = \frac{(\chi - \bar{\chi})(P_1 - P_3 + 0.3P'_8)}{\xi(P_1 + P_3) + (1 - \xi)P_2 + 0.28 \cdot P_7 + 0.5 \cdot P'_8 + 0.69 \cdot P_{13}} = (-1.3 \pm 1.2 \pm 0.8) 10^{-3}$$

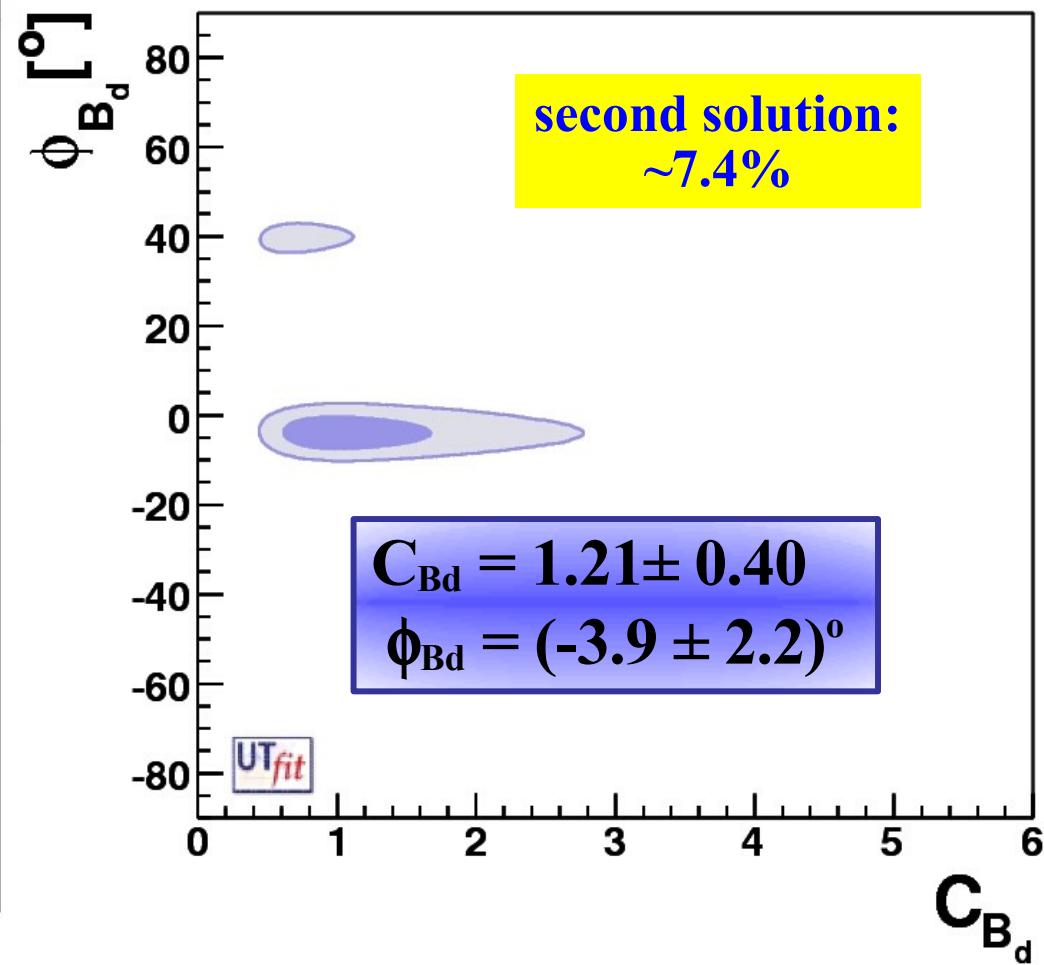
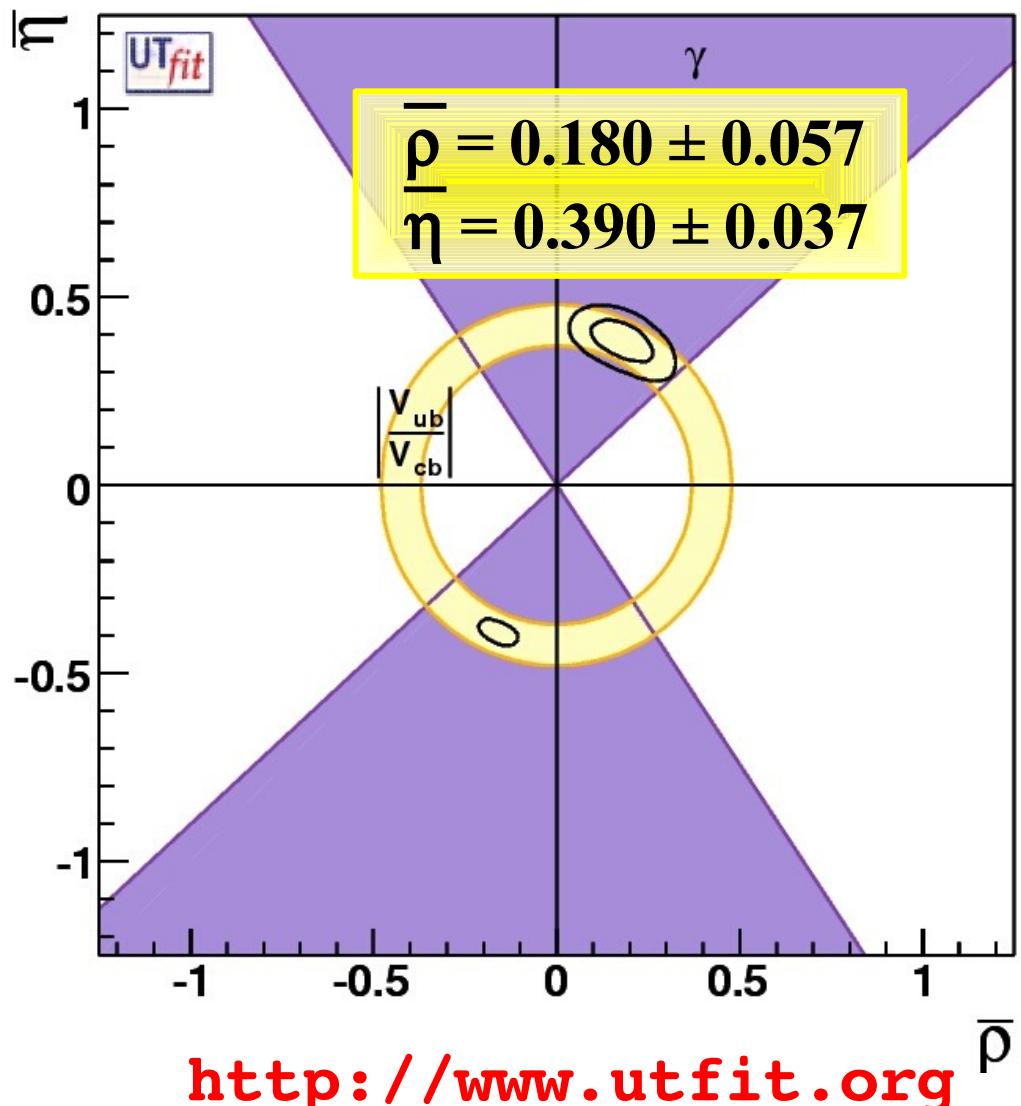
$$\chi = f_d \frac{\beta_d}{\langle \beta \rangle} \chi_d + f_s \frac{\beta_s}{\langle \beta \rangle} \chi_s$$

$$\bar{\chi} = f_d \frac{\beta_d}{\langle \beta \rangle} \bar{\chi}_d + f_s \frac{\beta_s}{\langle \beta \rangle} \chi_s$$

admixture of B_d and B_s
 dependent on $\bar{\rho}$ and $\bar{\eta}$
 and on NP effects

(C_{B_d} , ϕ_{B_d} , C_{B_s} , ϕ_{B_s})

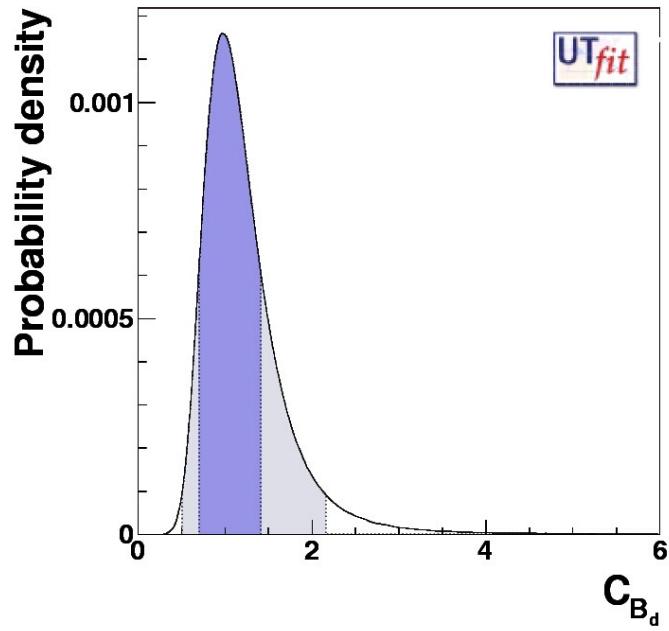
results of the model independent approach



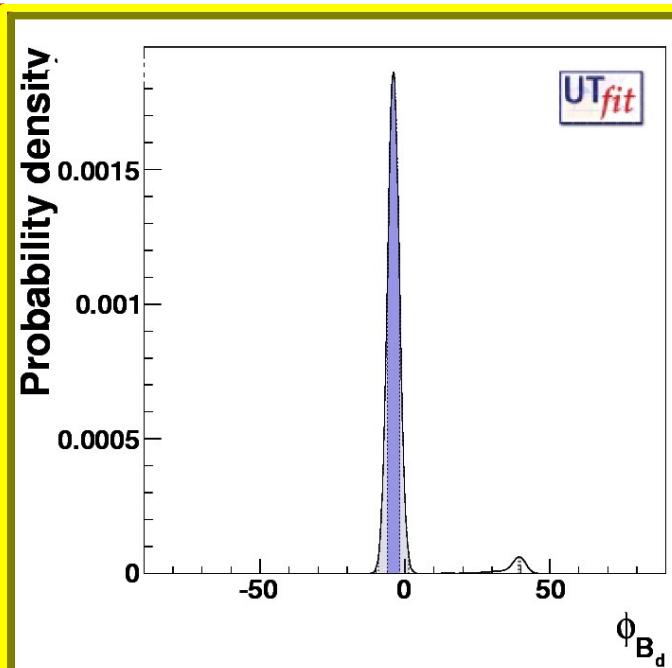
<http://www.utfit.org>

results in the B_d and K sectors:

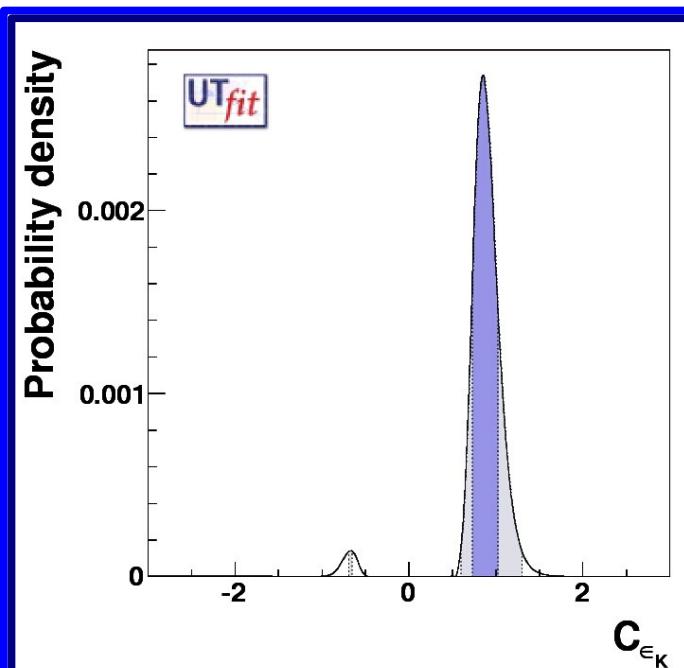
$$C_{B_d} = 1.21 \pm 0.40$$



$$\phi_{B_d} = -(3.9 \pm 2.2)^\circ$$



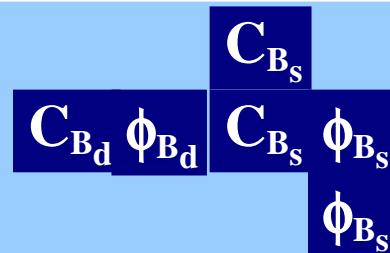
$$C_{\epsilon_K} = 0.88 \pm 0.15$$



NP in $\Delta B=2$ and $\Delta S=2$ could be up to 50% with respect to the SM only if it has the same phase of the SM

exploring new physics in the B_s sector:

- ✚ Δm_s : same as usual
- ✚ A_{CH} : already illustrated
- ✚ $\Delta\Gamma_s/\Gamma_s$: only from CDF
- ✚ flavour-specific B_s lifetime: only from CDF
- ✚ $TD(B_s \rightarrow J/\psi \phi)$: time dependent 3-dimensional angular analysis from D0



C_{Pen} and ϕ_{Pen}
to include $\Delta F = 1$
NP contributions

$\Delta\Gamma_s/\Gamma_s$

$$\frac{\Delta\Gamma_q}{\Delta m_q} = - \left[\frac{\kappa}{C_{B_q}} \left\{ \cos(2\phi_{B_q}) \left(n_1 + \frac{n_6 B_2 + n_{11}}{B_1} \right) - \frac{\cos(\phi_q^{SM} + 2\phi_{B_q})}{R_t^q} \left(n_2 + \frac{n_7 B_2 + n_{12}}{B_1} \right) + \frac{\cos(2(\phi_q^{SM} + \phi_{B_q}))}{R_t^{q^2}} \left(n_3 + \frac{n_8 B_2 + n_{13}}{B_1} \right) + \cos(\phi_q^{Pen} + 2\phi_{B_q}) C_q^{Pen} \left(n_4 + n_9 \frac{B_2}{B_1} \right) - \cos(\phi_q^{SM} - \phi_q^{Pen} + 2\phi_{B_q}) \frac{C_q^{Pen}}{R_t^q} \left(n_5 + n_{10} \frac{B_2}{B_1} \right) \right\} \right] \quad (7)$$

from angular
analysis of
 $B_s \rightarrow J/\psi \phi$

in presence of new physics, the experimental measurement
is actually a measurement of $\Delta\Gamma_q \cos 2(\phi_{B_q} - \beta_q)$

we use the CDF-only result

additional constraints the NP in the B_s sector:

flavour specific B_s lifetime

we use the CDF-only result

we now use τ_{B_s} only from the study of B_s decays to CP eigenstates which is connected to the values of Γ_s and $\Delta\Gamma_s$ by this relation

$$\tau_{B_s}^{FS} = \frac{1}{\Gamma_s} \frac{1 - \left(\frac{\Delta\Gamma_s}{2\Gamma_s}\right)^2}{1 + \left(\frac{\Delta\Gamma_s}{2\Gamma_s}\right)^2}$$

time-dependent angular analysis in $B_s \rightarrow J/\psi \phi$

D0 provided simultaneous bounds on β_s , $\Delta\Gamma$ and Γ :

we use the experimental likelihood

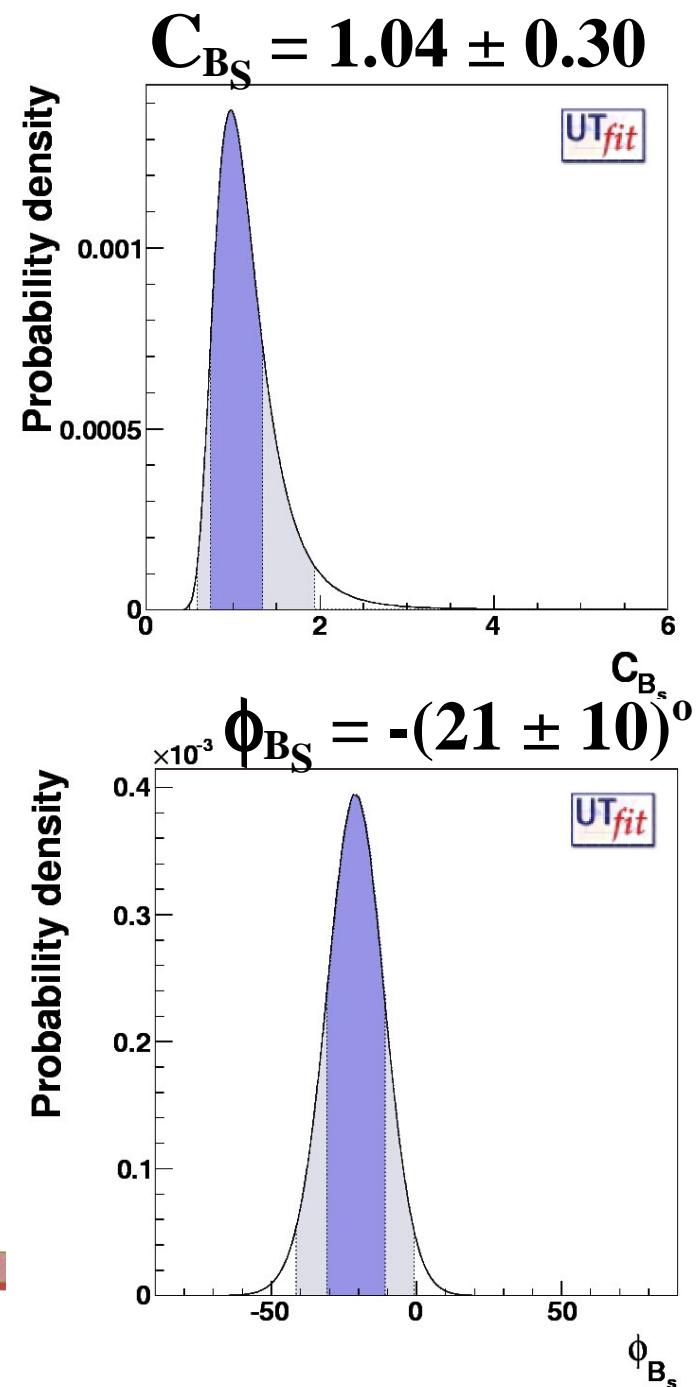
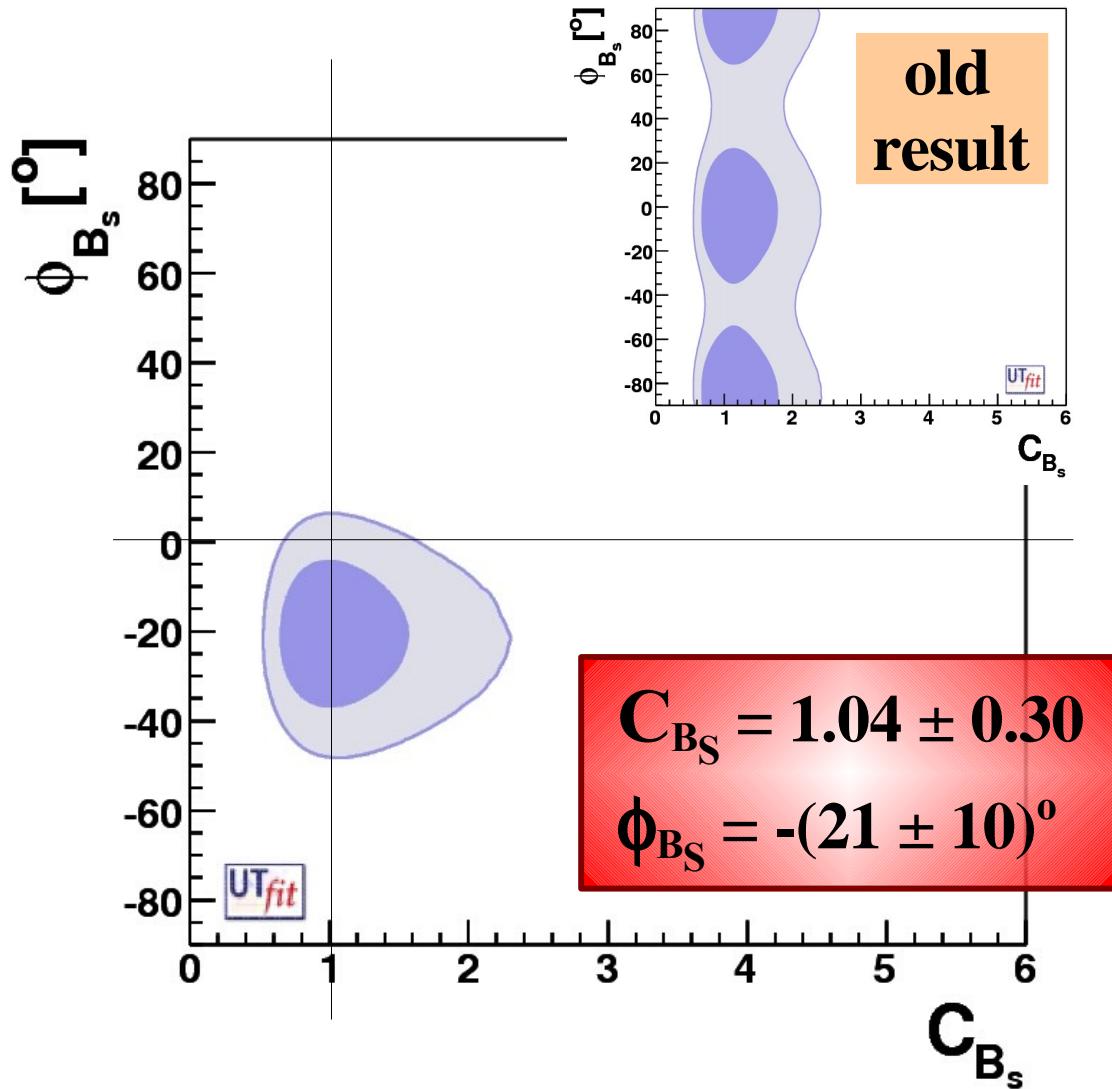
$C_{B_s} \phi_{B_s}$

including the 3x3 correlation matrix

and we don't use D0 values in the other constraints
(in order not to double count the measurements)

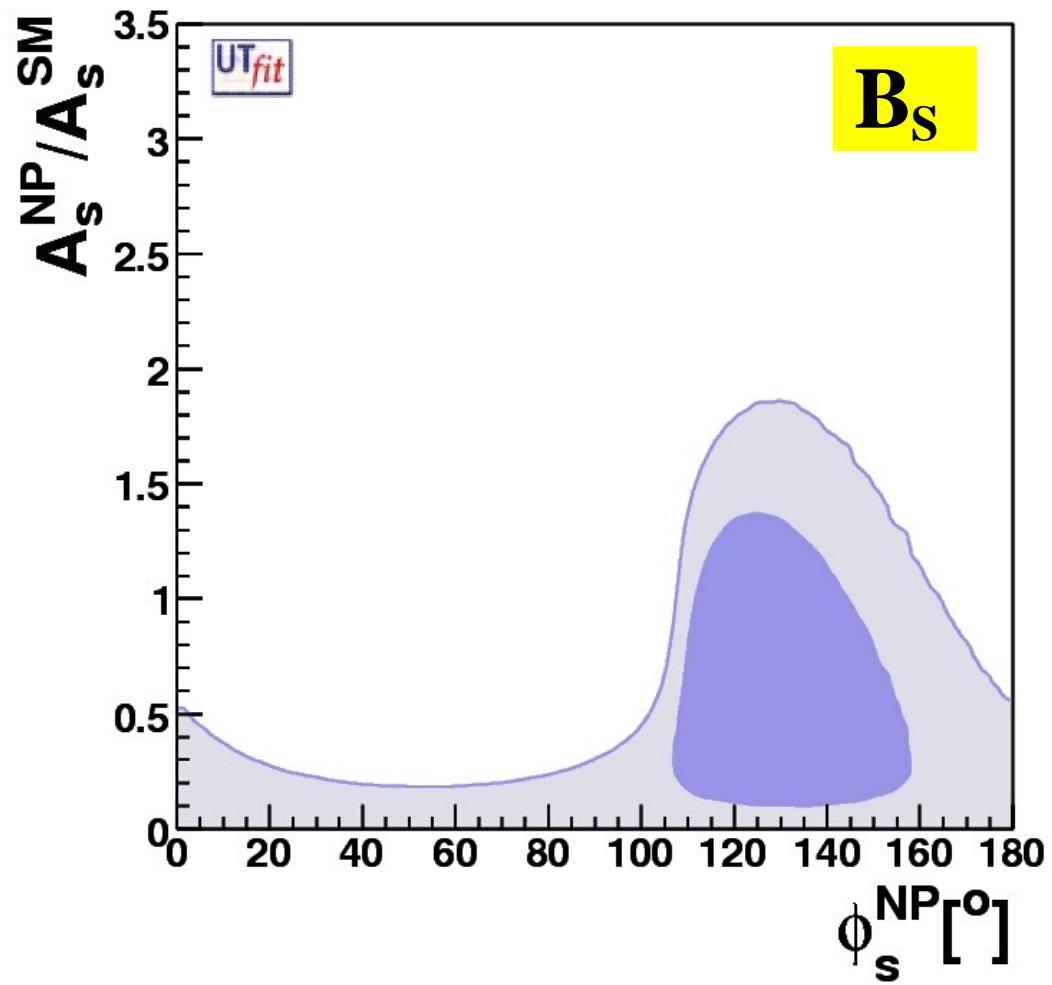
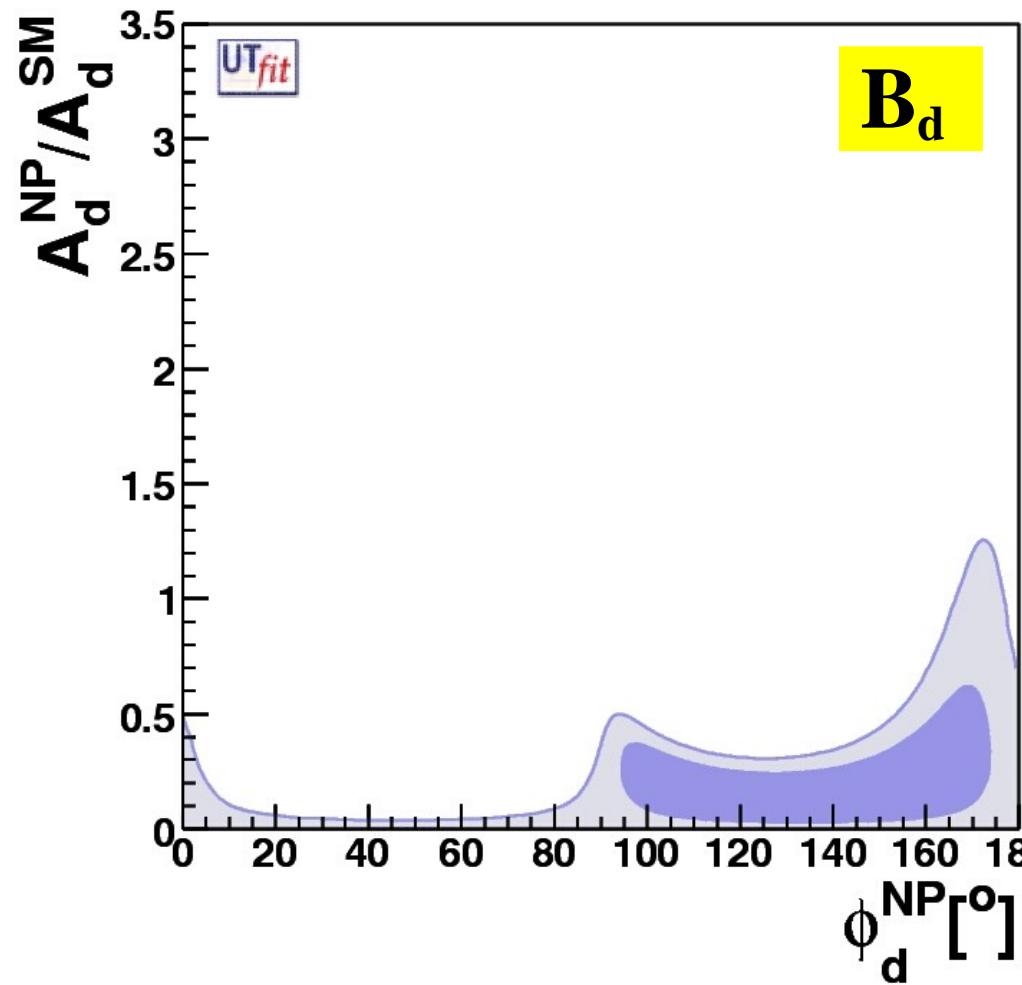
D0 result
ICHEP06

results in the B_s sector:



or if you prefer:

$$C_{B_q} e^{2i\phi_{B_q}} = \frac{A_q^{\text{SM}} e^{2i\beta_q} + A_q^{\text{NP}} e^{2i(\beta_q + \phi_q^{\text{NP}})}}{A_q^{\text{SM}} e^{2i\beta_q}}$$



Are there new sources of CPV?

- ▶ New sources of CPV in $s \rightarrow d$ and/or $b \rightarrow d$ transitions are
 - strongly constrained by the UT fit
 - “unnecessary”, given the great success and consistency of the fit
- ▶ New sources of CPV in $b \rightarrow s$ transitions are
 - much less (un-) constrained by the UT fit
 - natural in many flavour models, given the strong breaking of family SU(3)

L. Silvestrini
LP05

Pomarol, Tommasini; Barbieri, Dvali, Hall; Barbieri, Hall; Barbieri, Hall, Romanino; Berezhiani, Rossi; Masiero et al; ...

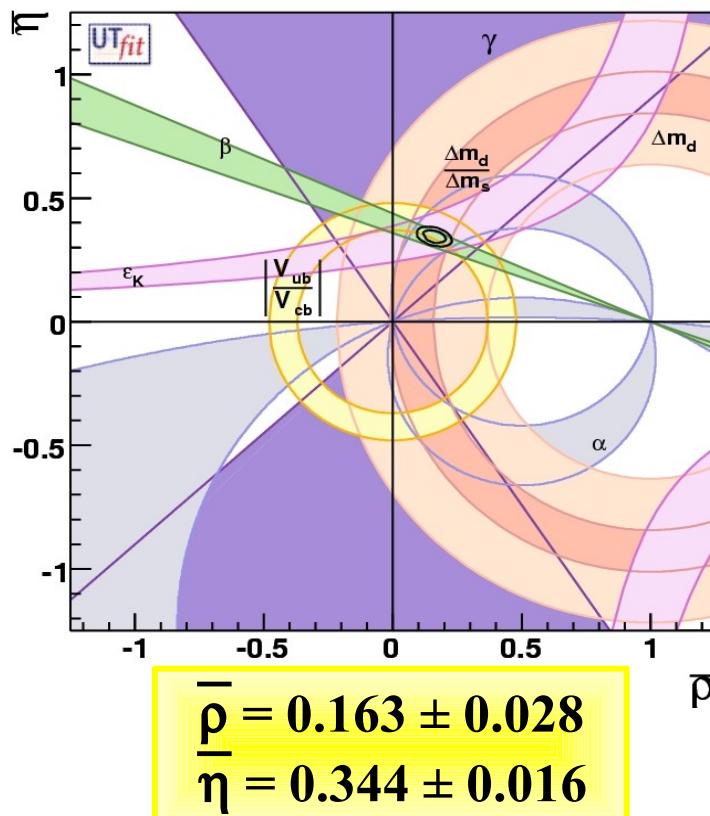
- hinted at by v's in SUSY-GUTs

Baek et al.; Moroi; Akama et al.; Chang, Masiero, Murayama; Hisano, Shimizu; Goto et al.; ...

exploring MFV scenario: starting from UUT

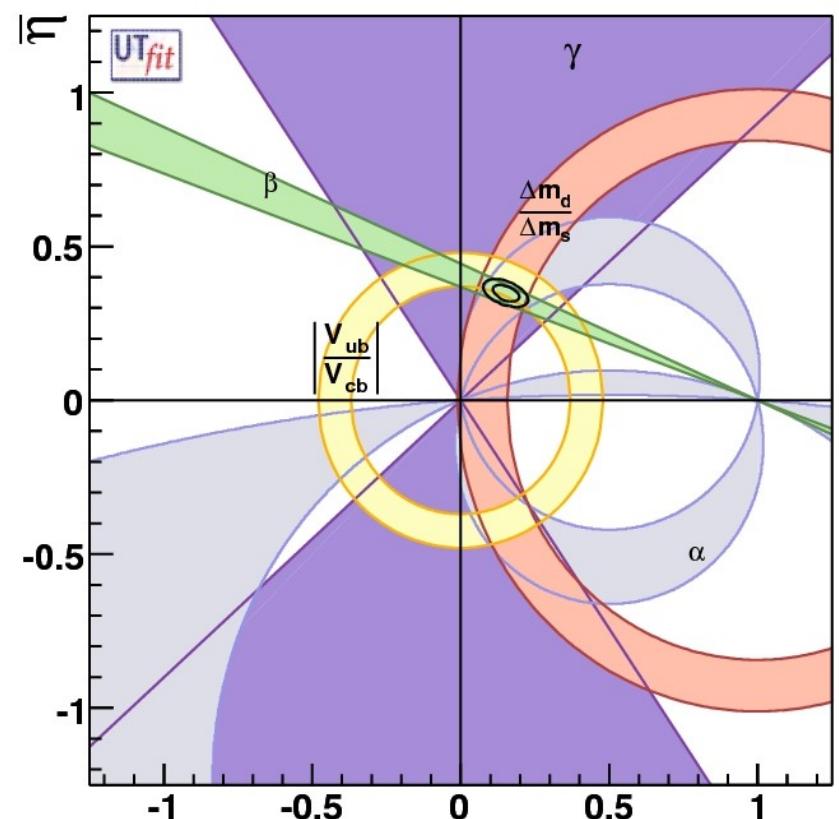
MFV = no additional flavour mixing
only mixing processes are sensitive to NP

Universal Unitarity Triangle
Buras et al. hep-ph/0007085



For UUT
we do not use
 ϵ_K and Δm_d
in the fit

Determines $\bar{\rho}$ and $\bar{\eta}$ independently
on the presence of MFV NP

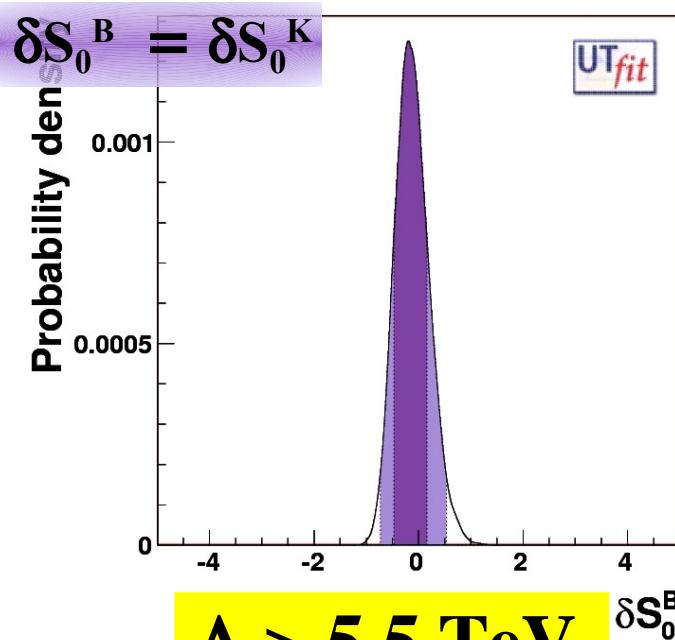


MFV analysis

Scale of NP can be indirectly tested

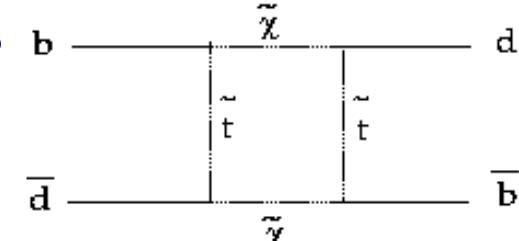
In models with one Higgs doublet or low/moderate $\tan\beta$

NP enters as additional contribution to the top box diagram



remaining constraints
(ε_K , Δm_d , and Δm_s)
probe NP in mixing

UT fit and new physics



$$S_0(x_t) \rightarrow S_0(x_t) + \delta S_0(x_t)$$

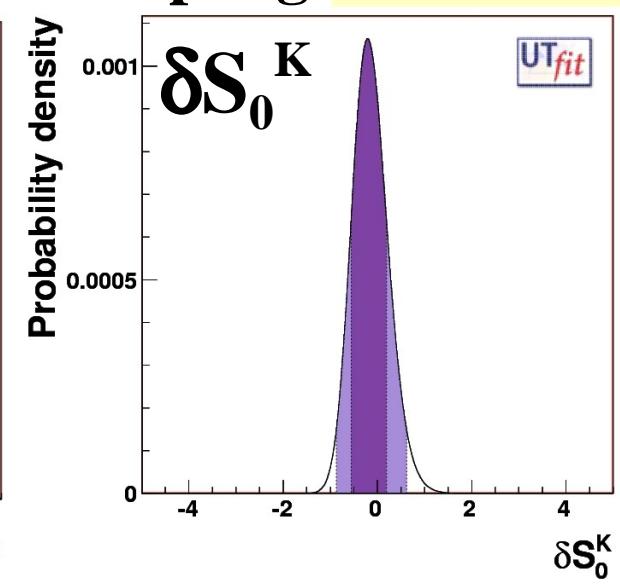
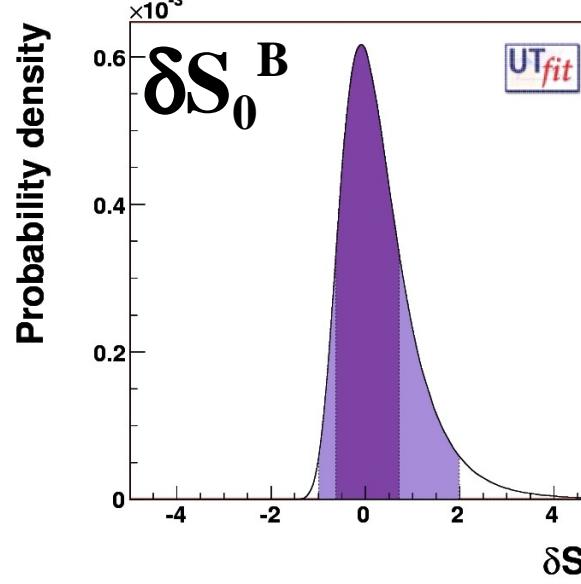
$$\delta S_0(x_t) = 4a \left(\frac{\Lambda_0}{\Lambda} \right)^2$$

$a = 1$ (as a reference) $\Lambda_0 = 2.4 \text{ TeV}$

Λ_0 is the equivalent SM scale

2 Higgs + large $\tan\beta$
→ also bottom Yukawa coupling

$$\delta S_0^B \neq \delta S_0^K$$



summary and conclusion

- **b → d transition:** given the enormous quantity of results the B factories have already achieved, the generalization of the UT analysis beyond the SM is already strongly effective in limiting the NP parameter space.
 - + it gives serious constraints on model building
 - + it points to MFV
- **b → s transitions** are starting to be impressively constrained, thanks to new measurements from the Tevatron:
 - + from CDF: $\Delta\Gamma_s/\Gamma_s$, flavour specific τ_{B_S}
 - + from D0: 3-dimensional β_s , $\Delta\Gamma$ and Γ bound
- in the MFV scenario it is possible to turn UT analysis into a probe for NP scale
- future scenarios..

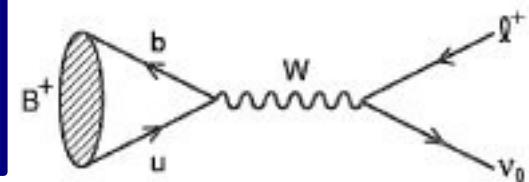
see:

M. Pierini and V. Vagnoni
in WG joint session

back-up slides

B → τν

$$\mathcal{B}(B \rightarrow \ell\nu) = \frac{G_F^2 m_B m_\ell^2}{8\pi} \left(1 - \frac{m_\ell^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B$$

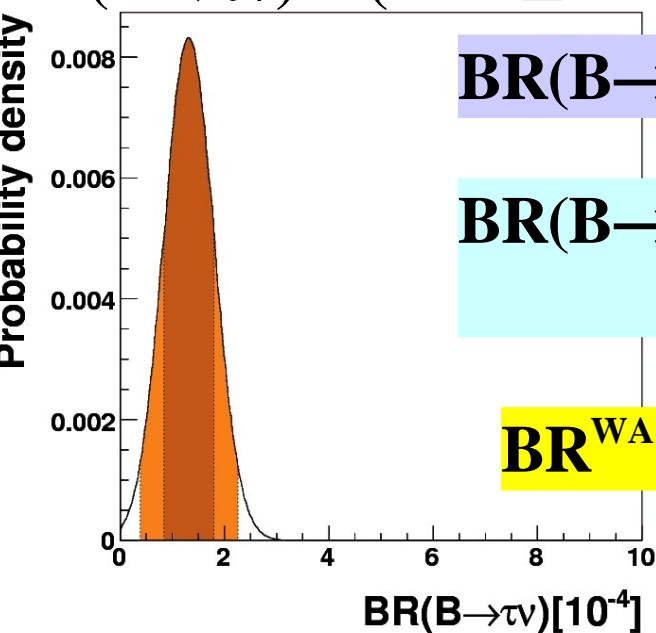


$$\text{BR}(B \rightarrow \tau\nu) = (1.06 \pm 0.38) 10^{-4}$$

$$\text{BR}(B \rightarrow \tau\nu) = (1.79 \pm 0.52 \pm 0.43) 10^{-4}$$



$$\begin{aligned} \text{BR}(B \rightarrow \tau\nu) &= (0.88 \pm 0.68 \pm 0.11) 10^{-4} \\ \text{BR} &< 1.80 10^{-4} @ 90\% \text{ CL} \end{aligned}$$



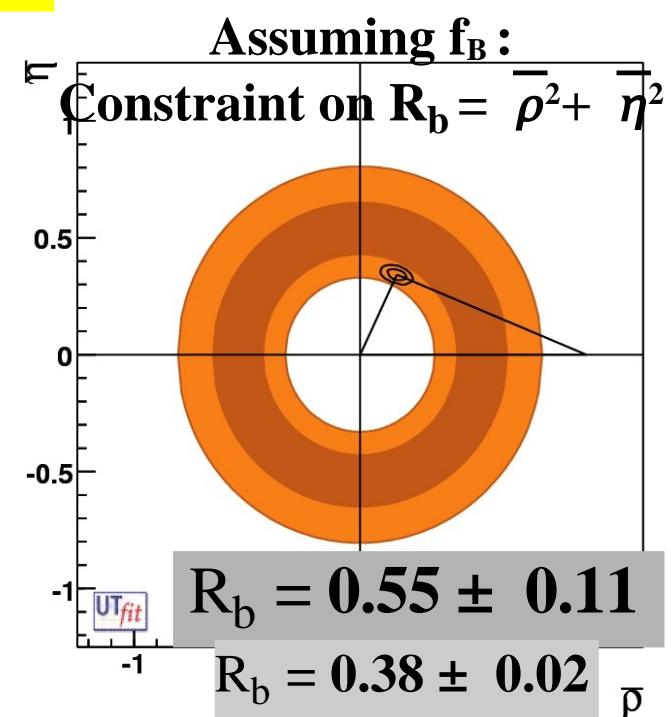
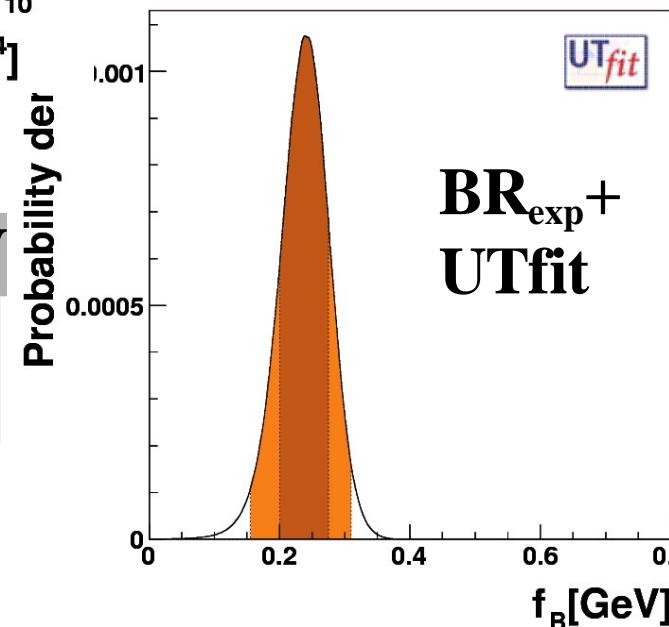
$$\text{BR}^{\text{WA}}(B \rightarrow \tau\nu) = (1.36 \pm 0.48) 10^{-4}$$

Assuming V_{ub} :

$$f_{Bd} = 0.237 \pm 0.037 \text{ GeV}$$

$$f_{Bd} = 0.189 \pm 0.027 \text{ GeV}$$

from lattice QCD



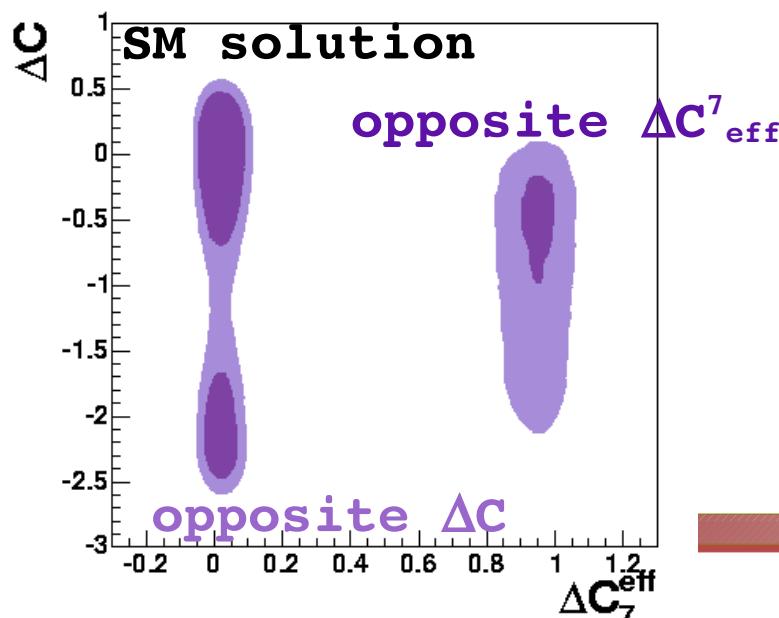
MFV bound from radiative decays

NP in MFV scenarios can be parameterized with few real parameters,
shifts of the master functions in

- + Z vertex
- + cromomagnetic penguin
- + box diagrams
- + gluonic penguin

Once CKM is known, we can bound NP with rare decays. At small/moderate $\tan\beta$, all the effects on leptonic/radiative modes from two parameters:

- + ΔC : NP in Z vertex (bound from $b \rightarrow s\gamma$)
- + ΔC^7_{eff} : NP in cromomagnetic penguin (bound from $b \rightarrow sll$)



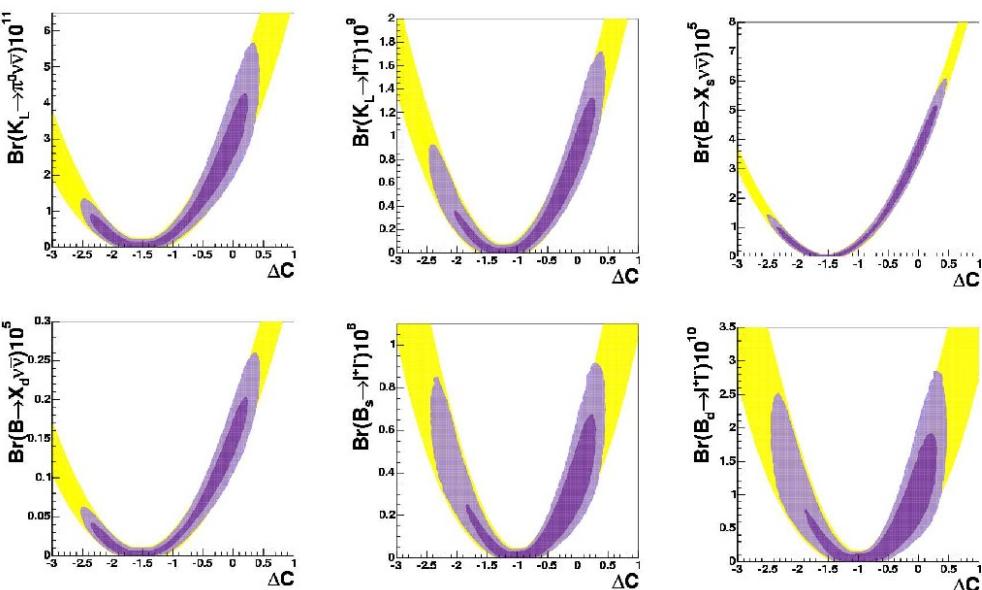
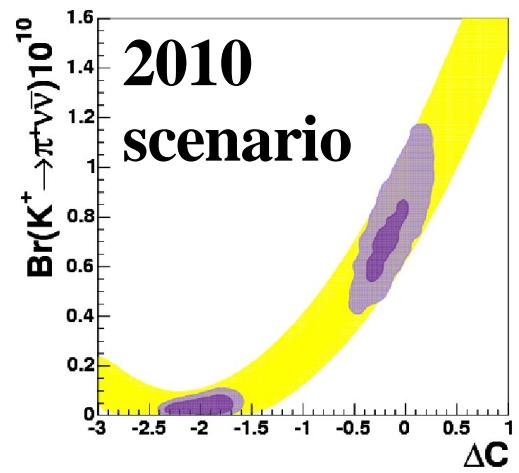
Relevant contributions in rare leptonic and radiative decays

Predictions on rare decays
can be obtained from this.
This peculiar correlation
can be tested with new
measurements

C. Bobeth *et al.*
Nucl.Phys.B726:252-274,2005
hep-ph/0505110

MFV prediction for rare decays

low/moderate
tan β



Branching fractions	MFV(95%)	SM (95%)	exp
$\text{Br}(K^+ \rightarrow \pi^+vv) \times 10^{11}$	<11.9	[6.1-10.9]	14.7+13.0-8.9
$\text{Br}(K_L \rightarrow \pi^0vv) \times 10^{11}$	<4.59	[2.03-4.26]	$<5.9 \times 10^4$
$\text{Br}(K_L \rightarrow \mu\mu) \times 10^9$	<1.36	[0.63-1.15]	
$\text{Br}(B \rightarrow X_s vv) \times 10^5$	<5.17	[3.25-4.09]	<64
$\text{Br}(B \rightarrow X_d vv) \times 10^6$	<2.17	[1.12-1.91]	
$\text{Br}(B_s \rightarrow \mu\mu) \times 10^9$	<7.42	[1.91-5.91]	$<2.7 \times 10^2$
$\text{Br}(B_d \rightarrow \mu\mu) \times 10^{10}$	<2.20	[0.47-1.81]	$<1.5 \times 10^3$

K physics

B_{d,s} physics

Very interesting the A_{FB} asymmetry of $B \rightarrow K^* ll$