



Measurement of time  
dependent CP violation  
in  $B^0 \rightarrow D^+D^-$  decays

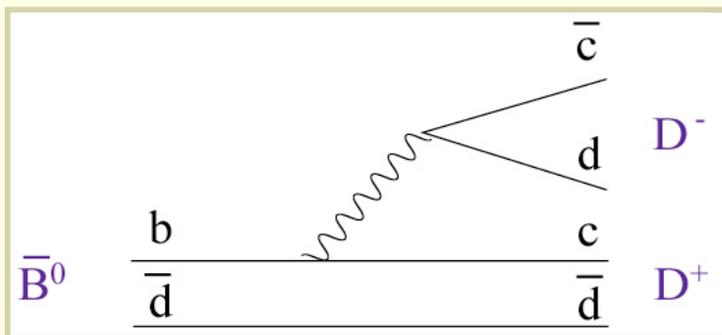
Saša Fratina

Jozef Stefan Institute, Ljubljana

# Physics motivation

Measure CP violation parameters in  $B^0 \rightarrow D^+ D^-$  decay.

$$\frac{dP_{sig}}{dt}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau}}{4\tau} (1 + q(S \sin(\Delta m \Delta t) + A \cos(\Delta m \Delta t)))$$



time-dependent CP violation

+ penguin

$\Delta t$ : time between the decay of two B mesons,  $\Delta z = \beta\gamma c \Delta t$

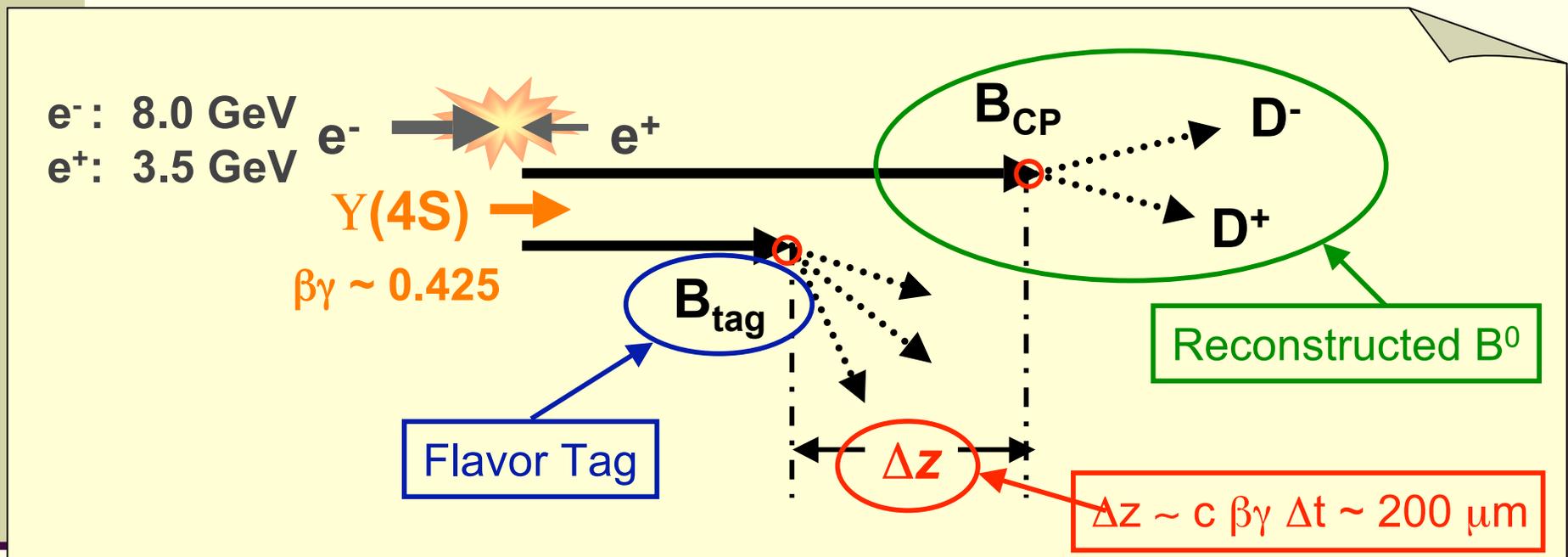
$q$ : flavor of B meson decaying to a CP eigenstate

$\Delta m$ : B mass difference  $m(B_1) - m(B_2)$

$S, A$ : CP violation parameters

SM expectations:  $S \approx -\sin 2\phi_1$ ,  $A \approx 3\%$  [Z.Z.Xing, PRD61, 014010 (2000)]

# Measuring the CP parameters S and A



$$\frac{dP_{\text{sig}}}{dt}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau}}{4\tau} (1 + q(S \sin(\Delta m \Delta t) + A \cos(\Delta m \Delta t)))$$

↑ ↑ ↑ ↑ ↑

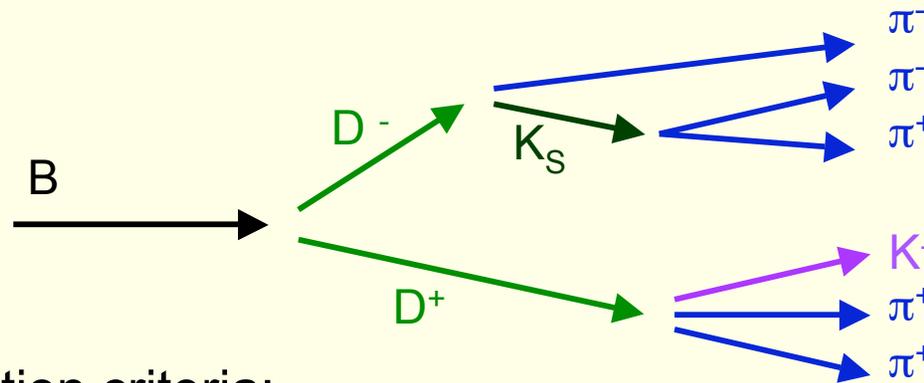
# Outline of the talk

---

- Event reconstruction and selection
  - Branching fraction measurement
- CP analysis
  - PDF description, cross-checks
  - Result for the 535 M BB-events data sample
- Summary

# Event reconstruction & selection

- $B^0 \rightarrow D^+ D^-$ ,  $D \rightarrow K\pi\pi$  or  $D \rightarrow K_S\pi$  reconstruction channels
- Vertex reconstruction: first  $D^+$  and  $D^-$ , then  $B^0$  from  $D^+D^-$  and the IP

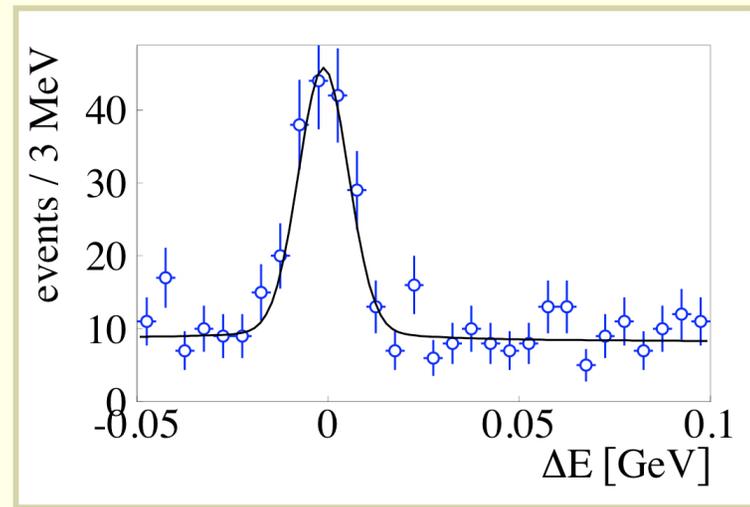
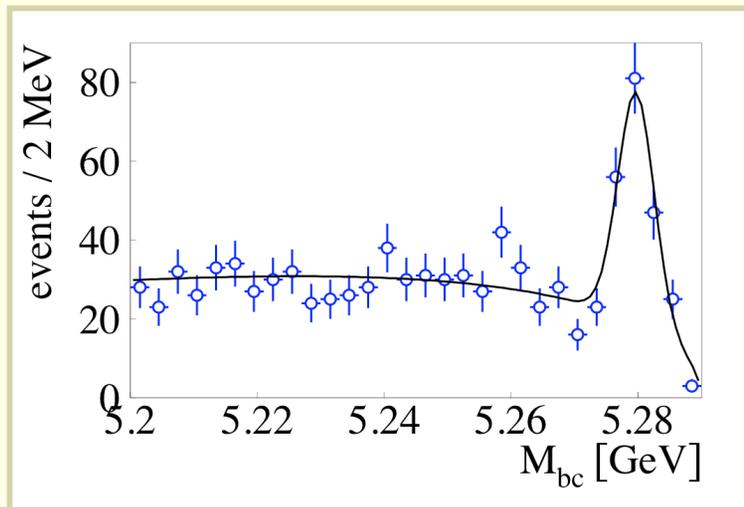


- Event selection criteria:
  - continuum suppression: use spherical moments to separate jet-like and spherical events
  - D mass cut, D mass is also used for a best candidate selection
  - pion and kaon PID, electron veto
  - distance from the interaction point  $|\Delta r|$  and  $|\Delta z|$
- 12% event reconstruction efficiency

# Peaking background study

- Non-resonant B decays peaking in the  $M_{bc}$ ,  $\Delta E$ 
  - $B^0 \rightarrow D^- \pi^+ K^0$  ( $K^0 \rightarrow K_S$ )  $\rightarrow$  peaking in  $K_S \pi$
  - $B^0 \rightarrow D^- \pi^+ K^{*0}(892)$  ( $K^{*0}(892) \rightarrow K^- \pi^+$ )  $\rightarrow$  in  $K \pi \pi$
- Determine the amount from D mass sidebands in data sample (cross-check with MC)
  - One D meson from the D mass signal region, the other from the sideband
- No significant peaking observed,
  - $K \pi \pi$ :  $2.0 \pm 1.8$  events expected in the sig. region
  - $K_S \pi$ :  $1.4 \pm 1.0$  events
- Taken into account for the CP-fit

# Signal yield for the $535 \cdot 10^6 \text{ B}\bar{\text{B}}$ events



$$M_{bc} = \sqrt{E_{beam}^2 - p_B^2} \quad (\text{in the CMS system}) \quad \Delta E = E_B - E_{beam}$$

	$N_{sig}$	$N_{nr}$	$N_{bcg}$
$K\pi\pi$	$123 \pm 19$	$2.0 \pm 1.8$	$109 \pm 1$
$K_S\pi$	$24 \pm 8$	$1.4 \pm 1.0$	$15 \pm 1$

about 130 signal events  
with  $S/(S+B) \sim 0.6$   
available for the time-  
dependent analysis

# Branching fraction measurement

- Previous measurements:
  - $(1.91 \pm 0.51 \pm 0.30) 10^{-4}$  [Belle, PRL95, 040813 (2005)]
  - $(2.8 \pm 0.4 \pm 0.5) 10^{-4}$  [Babar, PRL95, 131802 (2005)]
- An update with higher statistics;
  - sum the number of reconstructed events in the  $K\pi\pi$  and  $K_S\pi$  rec. ch. and average the efficiency
  - $\text{Br}(B^0 \rightarrow D^+D^-) = ( 1.98 \pm 0.23 \pm 0.22 ) 10^{-4}$  Preliminary  
(stat) (syst)
  - Systematic errors: D meson branching fractions (6%), track reconstruction efficiency (6%), PID eff. (6%), other smaller than 2%

# CP analysis

$\Delta t$ : time between the decay of two B mesons,  $\Delta z = \beta\gamma c \Delta t$

q: flavor of B meson decaying to a CP eigenstate

$\Delta m$ : B mass difference  $m(B_1) - m(B_2)$

S, A: CP violation parameters

- Signal:

$$\frac{dP_{sig}}{dt}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau}}{4\tau} (1 + q(S \sin(\Delta m \Delta t) + A \cos(\Delta m \Delta t))) \otimes \text{det. resol.}$$

Imperfect tagging:  $q \rightarrow q(1-2w)$ ;

w is a wrong tag fraction

kinematic smearing

detector resolution

non-primary tracks

- Background:

$$\frac{dP_{bcg}}{dt}(\Delta t) = \left[ (1-f) \frac{e^{-|\Delta t|/\tau}}{2\tau} + f\delta(\Delta t) \right] \otimes \frac{e^{-\Delta t^2/2\sigma^2}}{\sqrt{2\pi}\sigma}$$

- Event PDF: → unbinned ML fit

$$\frac{dP}{dt}(\Delta t, q) = f_{sig} \frac{dP_{sig}}{dt}(\Delta t) + f_{nr} \frac{dP_{nr}}{dt}(\Delta t) + f_{bcg} \frac{dP_{bcg}}{dt}(\Delta t)$$

$$f_i = f_i(M_{bc}, \Delta E)$$

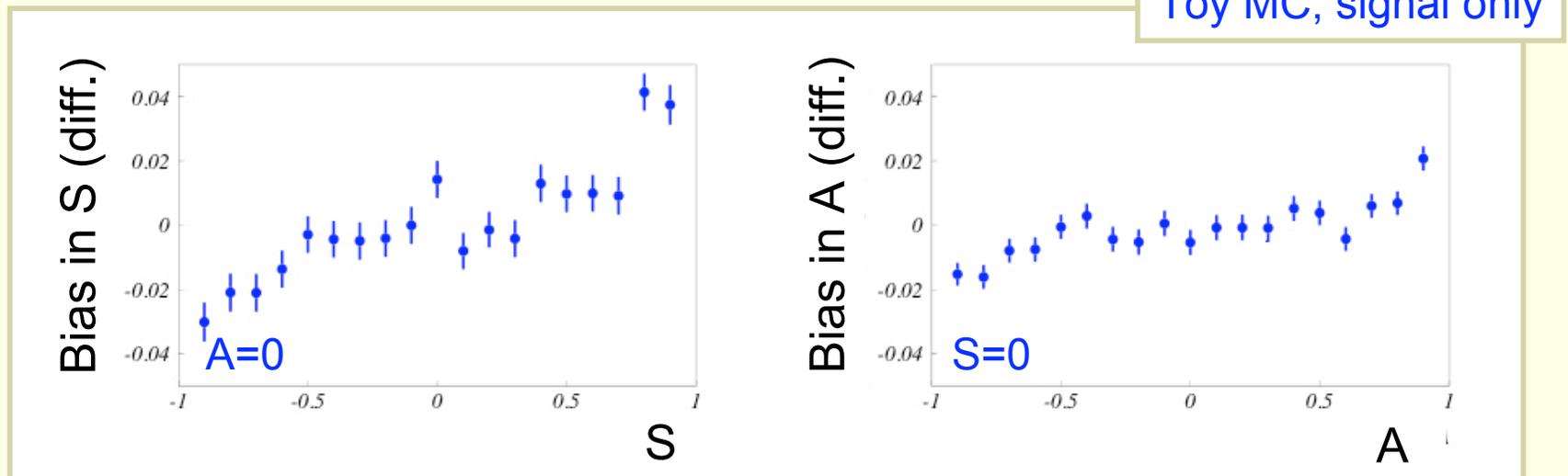
# CP analysis, cont.

---

- Use kinematically similar  $B^0 \rightarrow D_s^+ D^-$  decays as a control sample
  - $B^0 \rightarrow D_s^+ D^-$  reconstruction [hep-ex/0508040, LP2005]
  - approx. 2000 reconstructed events (larger data sample)
  - Also used to determine the  $B_{CP}$  vertex resolution parameters for the data sample

# Test for CP-fit bias

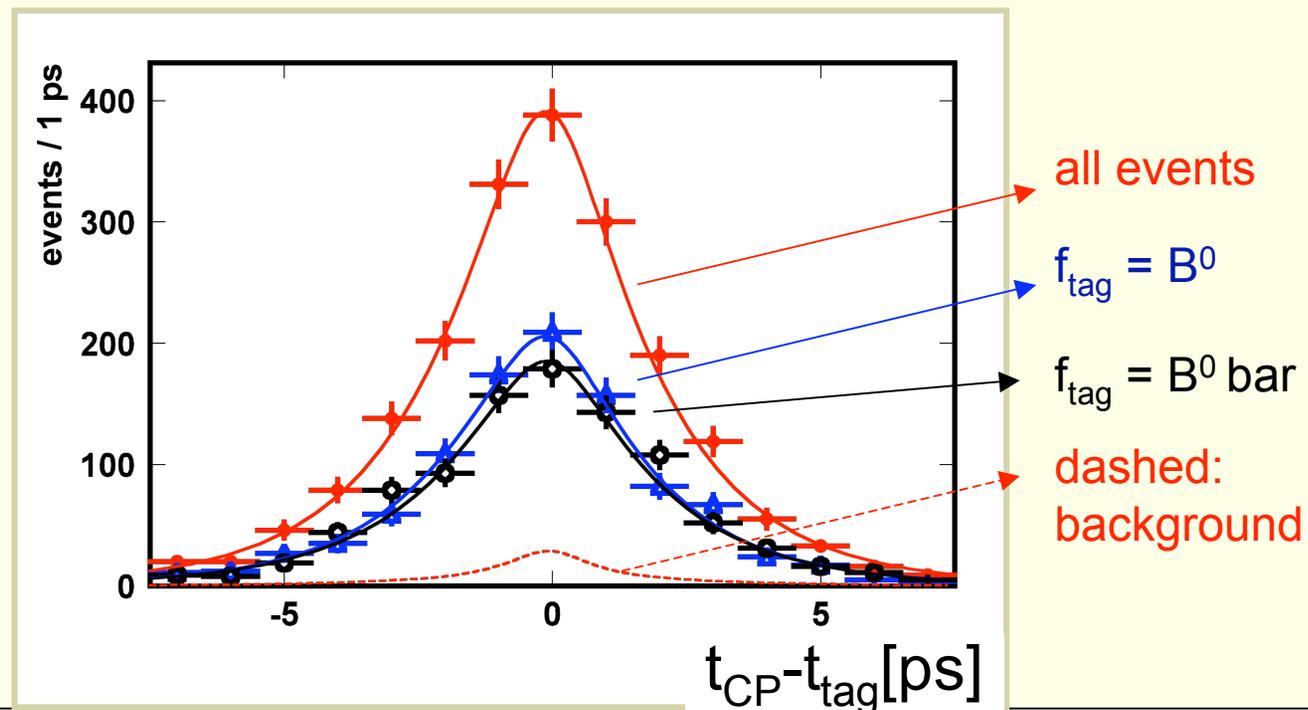
- Use signal MC and toy MC to check if there is any fit bias due to the small sample statistics



- Fit the bias dependence on S and A (sig+bcg toy MC):
  - $\mu_S \approx [ 0.99 + 0.07 (S^2+A^2) ] S$
  - $\mu_A \approx [ 0.99 + 0.03 (S^2+A^2) ] A$

# CP-fit to the control sample data

- Control sample of  $B^0 \rightarrow D_s^+ D^-$  decays
- $S = -0.064 \pm 0.094$  (stat)  $\pm 0.012$  (syst)
- $A = 0.091 \pm 0.060$  (stat)  $\pm 0.010$  (syst)

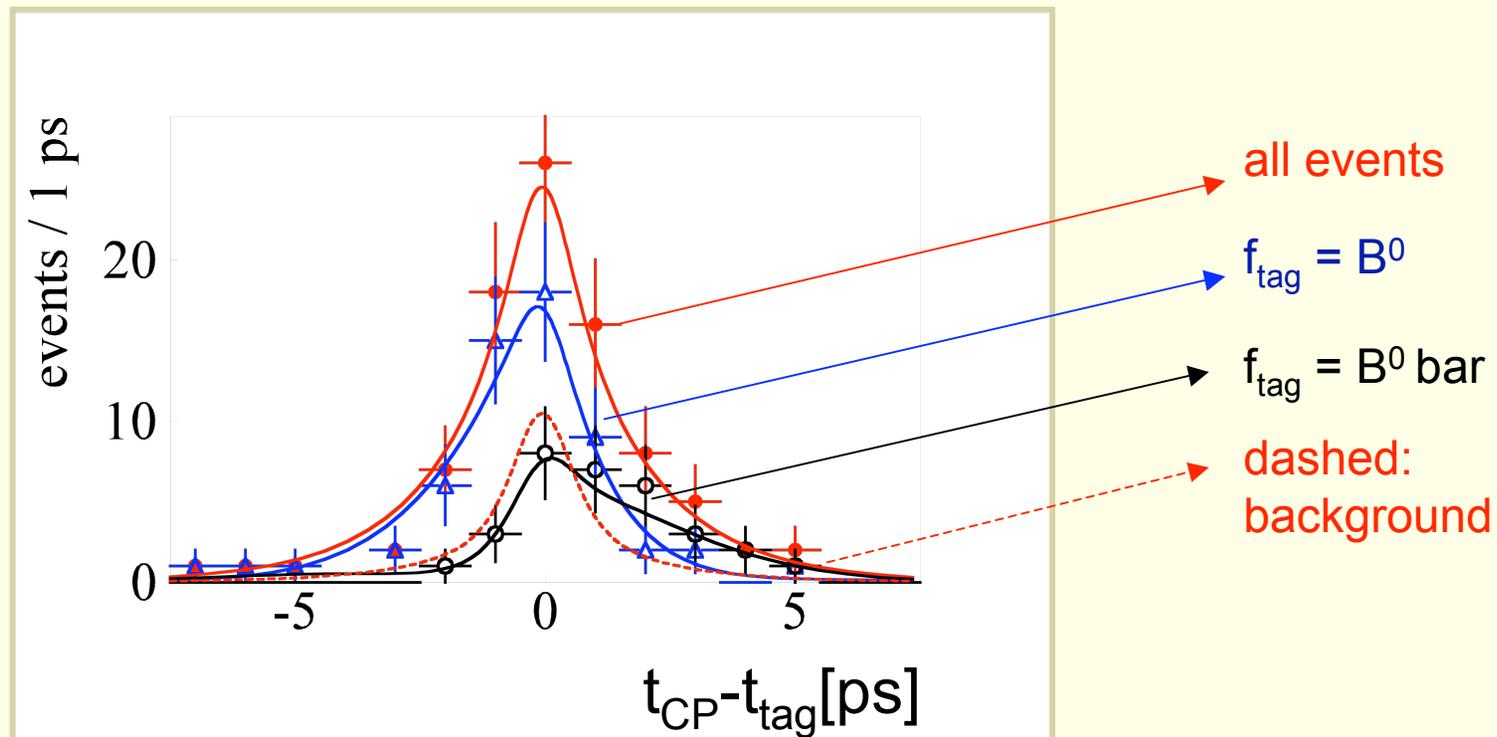


# $B^0 \rightarrow D^+D^-$ CP violation parameters

$$S = -1.12 \pm 0.37 \text{ (stat)} \pm 0.09 \text{ (syst)}$$

$$A = 0.92 \pm 0.23 \text{ (stat)} \pm 0.05 \text{ (syst)}$$

Preliminary



# Systematic errors

	$\sigma_S$	$\sigma_A$
CP-fit bias	0.06	0.02
signal fraction	0.035	0.015
non-resonant background	0.01	0.02
vertex resolution function params.	0.04	0.03
background distribution	0.02	0.01
vertex quality cuts	0.01	0.01
wrong tag fraction	0.017	0.014
values of $\tau$ and $\Delta m$	0.023	0.007
sum in squares	0.09	0.05

For all contributions, vary relevant parameters by  $\pm\sigma$  or do the same in the toy MC study (explained in the back-up slides).

# Statistical errors and significance

- Use Feldman-Cousins method to determine the statistical significance (similar as for the Belle  $B^0 \rightarrow \pi^+ \pi^-$  analysis)
- First: confirm that the RMS of the S and A distributions (from toy MC) simulate the expected errors in data

	Data, CP-blind fit	Toy MC S = -0.725, A = 0	Toy MC S = -0.725, A = 0.6
$\sigma_S$	0.37	0.36	0.37
$\sigma_A$	0.22	0.24	0.23

5-10% difference, its impact on the significance is evaluated by rescaling the toy MC widths with the corresponding factors (+8% change in CL)

Systematic errors are included in the simulation.

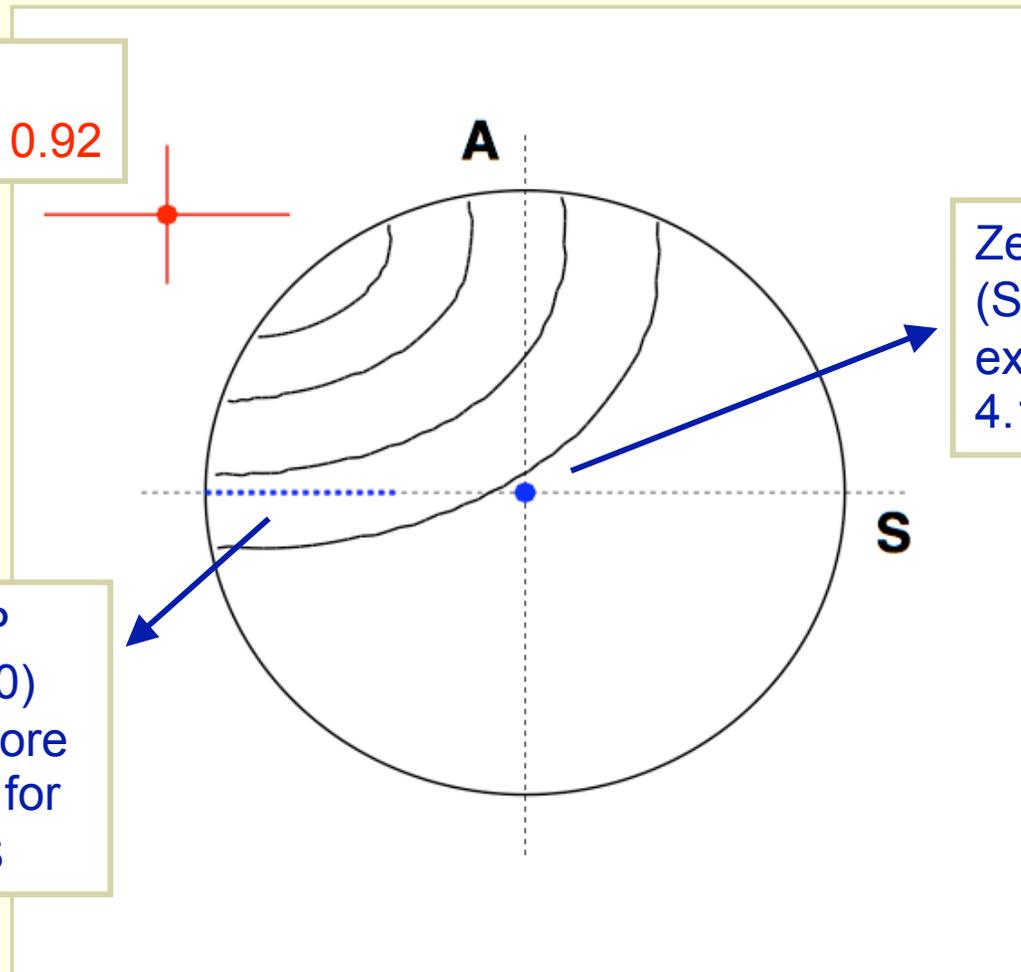
# Result of the Feldman-Cousins significance study

Preliminary

data point:  
 $S = -1.12, A = 0.92$

Zero direct CP violation ( $A = 0$ ) excluded at more than  $3.2 \sigma$  CL for any value of  $S$

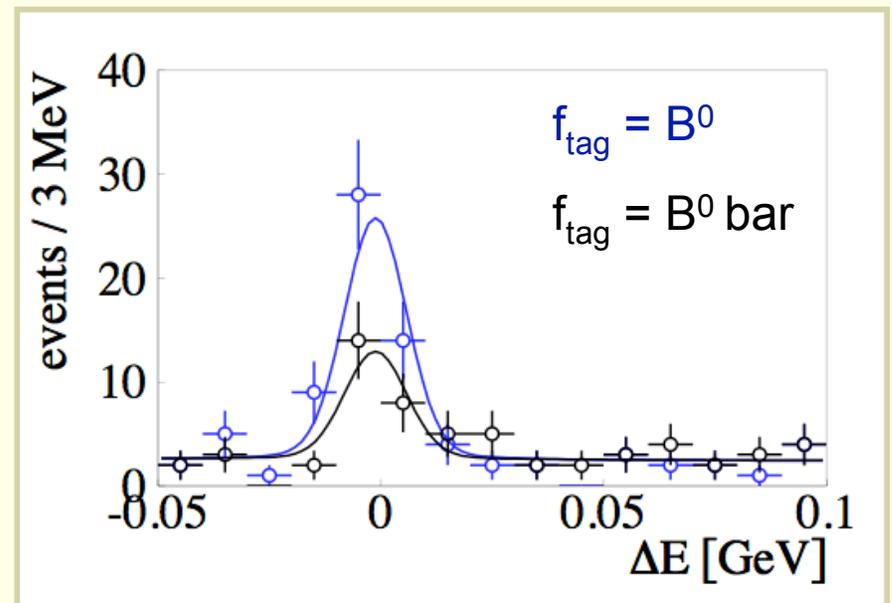
Zero CP violation ( $S = A = 0$ ) excluded at a  $4.1 \sigma$  CL



# Time-integrated fit

- $A \neq 0 \Rightarrow$  Raw asymmetry =  $\frac{N_{tag=B^0} - N_{tag=B^0\bar{0}}}{N_{tag=B^0} + N_{tag=B^0\bar{0}}} \neq 0$
- Can check the consistency of the result if one does not use any time information
- Time-integrated cross-check:  
 $A = 0.86 \pm 0.32$  ( $2.7 \sigma$ );  
consistent with  
time-dependent fit

$$r > 0.5$$



# Check for flavor asymmetry in the background events

---

- Perform the CP-fit for the background events in the  $M_{bc} < 5.27 \text{ GeV} / c^2$  sideband region
  - larger number of events (6000)
  - assign the same signal fraction to all events (0.63)
  - $S = 0.03 \pm 0.10$ ;  $A = -0.01 \pm 0.06$ ; consistent with zero

# Summary

- New measurement in  $B^0 \rightarrow D^+D^-$  decays based on the data sample of  $535 \cdot 10^6$  B meson pairs recorded by the Belle detector
- Updated branching fraction:  
 $Br = (1.98 \pm 0.23 \text{ (stat)} \pm 0.22 \text{ (syst)}) \cdot 10^{-4}$
- We measure the CP parameters to be:  
 $S = -1.12 \pm 0.37 \pm 0.09$ ;  $A = 0.92 \pm 0.23 \pm 0.05$ 
  - SM expectations:  $S = -0.72$ ;  $A \approx 3\%$ ;
  - BaBar, 232M BB pairs [PRL95, 131802 (2005)]:  
 $S = -0.29 \pm 0.63 \pm 0.06$ ;  $A = -0.11 \pm 0.35 \pm 0.06$   
difference at a  $2.2 \sigma$  level.

# Summary

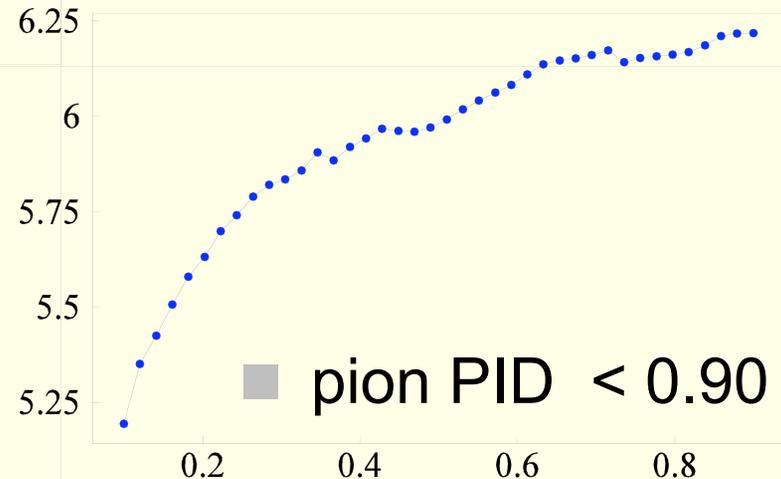
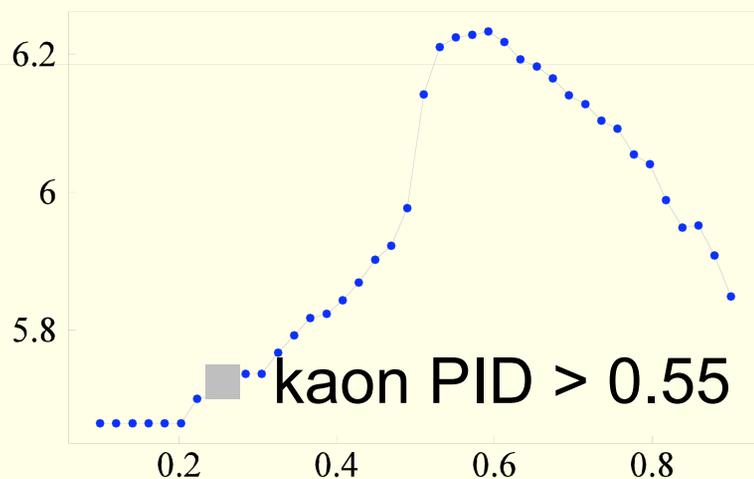
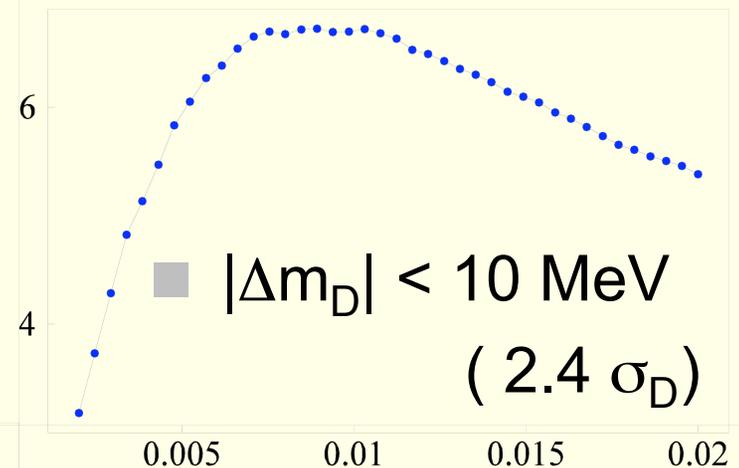
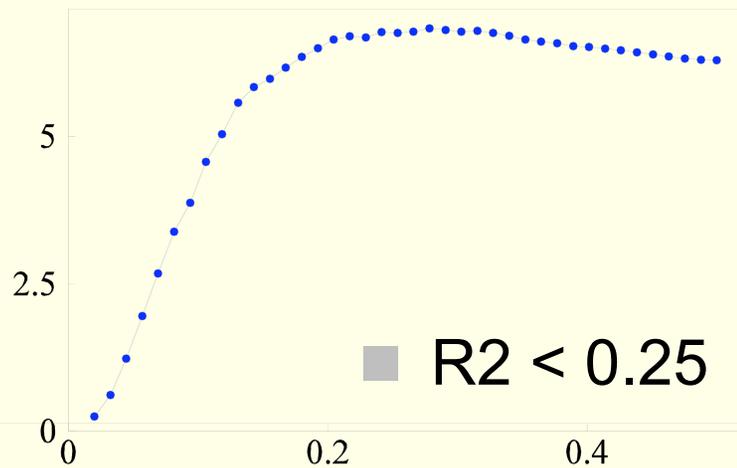
- First evidence of CP violation in  $B^0 \rightarrow D^+D^-$  decays at a  $4.1\sigma$  CL.
- Evidence of direct CPV at a  $3.2\sigma$  CL.
  - Such a large direct CPV not expected by the SM.
  - Not indicated by the previous measurement.
- Need more data to settle the issue, study isospin-conjugated  $B^- \rightarrow D^0D^-$  decays

# Back-up slides

---

# Event selection criteria

plot  $\frac{S}{\sqrt{S+B}}$  rescaled to  $417\text{fb}^{-1}$ , after all other cuts



# The Feldman – Cousins method

- Simulate **toy MC** according to the corresponding distributions in data:
  - Signal and background  $\Delta t$  distributions
  - Signal fraction, kinematic variables
  - CP- and tag-side vertex errors and vertex quality, vertex residuals
  - wrong tag fractions
- Fit S and A for each toy MC sample:  $P(S, A | S^{\text{hyp}}, A^{\text{hyp}})$
- Use the **Feldman - Cousins ordering principle**:
  - F-C:  $P(S, A | S^{\text{hyp}}, A^{\text{hyp}}) / P(S, A | S^{\text{best}}, A^{\text{best}})$ , where  $(S^{\text{best}}, A^{\text{best}})$  are the values inside the physical region for which  $P(S, A | S^{\text{best}}, A^{\text{best}})$  is maximal (definition)
- $CL = \int_{\Omega} P(S, A | S^{\text{hyp}}, A^{\text{hyp}}) dS dA$   
where the int. area  $\Omega$  is determined by the above criteria

# Treatment of the systematic error

---

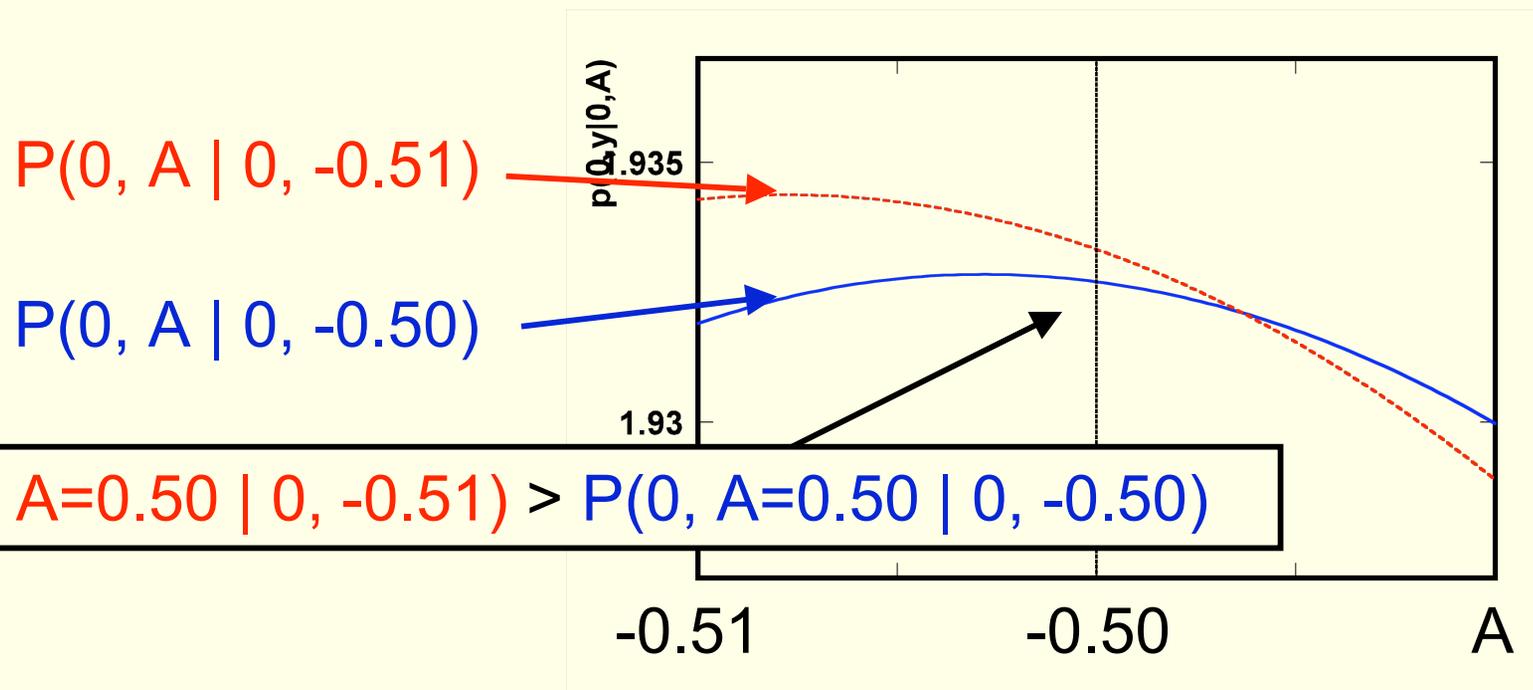
- Procedure:
  - a) Generate a toy MC sample with the default parameters.
  - b) Smear the CP-side resolution parameters used for the fit and repeat the fit on the same toy MC sample
  - c) Repeat the same for the parameters describing the signal fraction
- The difference (a-b) and (a-c) is the corresponding systematic error

# Toy MC: $P(S, A | S^{\text{hyp}}, A^{\text{hyp}})$

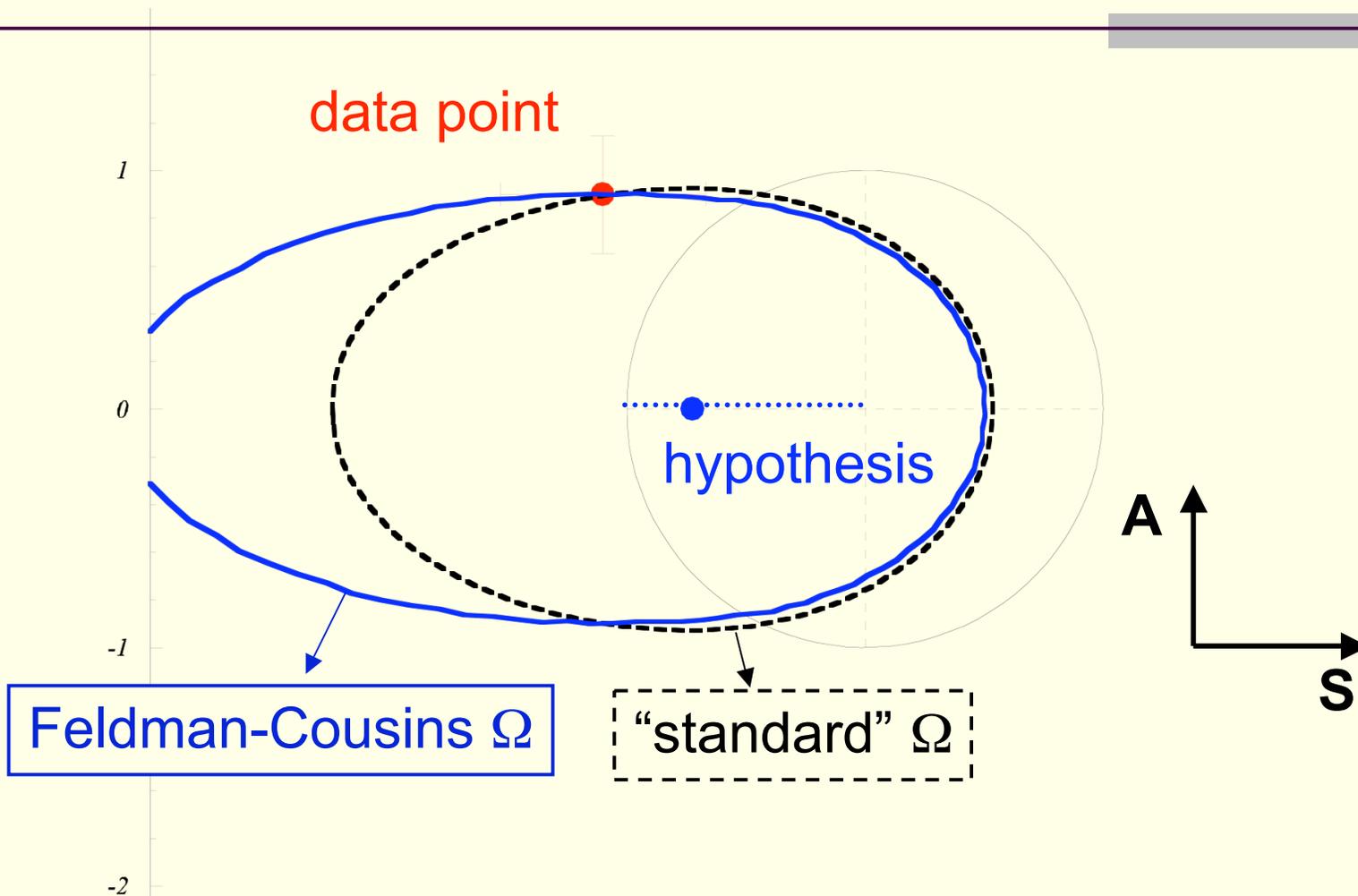
- $P(S, A | S^{\text{hyp}}, A^{\text{hyp}}) = G(S | \mu_S, \sigma_S^p, \sigma_S^n) G(A | \mu_A, \sigma_A^p, \sigma_A^n)$ 
  - $\mu_S = \mu_S(S^{\text{hyp}}, A^{\text{hyp}})$
  - $\sigma_S^p = \sigma_S^p(S^{\text{hyp}}, A^{\text{hyp}})$
  - ...
- Simulate toy MC for different input values  $S^{\text{hyp}}, A^{\text{hyp}}$
- Fit the parameters  $\mu_S, \sigma_S^p, \dots$  for all  $S^{\text{hyp}}, A^{\text{hyp}}$
- Fit the dependency  $\mu_S(S^{\text{hyp}}, A^{\text{hyp}}), \dots$  with an up to 4<sup>th</sup> order polynomial function
- The possibility of wider-than Gaussian tails is taken into account

# $S^{\text{best}}, A^{\text{best}}$

- For a given measured point  $(S, A)$ , the values  $(S^{\text{best}}, A^{\text{best}})$  are the values inside the physical region for which  $P(S, A | S^{\text{best}}, A^{\text{best}})$  is maximal
- $(S^{\text{best}}, A^{\text{best}})$  can be different from  $(S, A)$  even inside the physical region

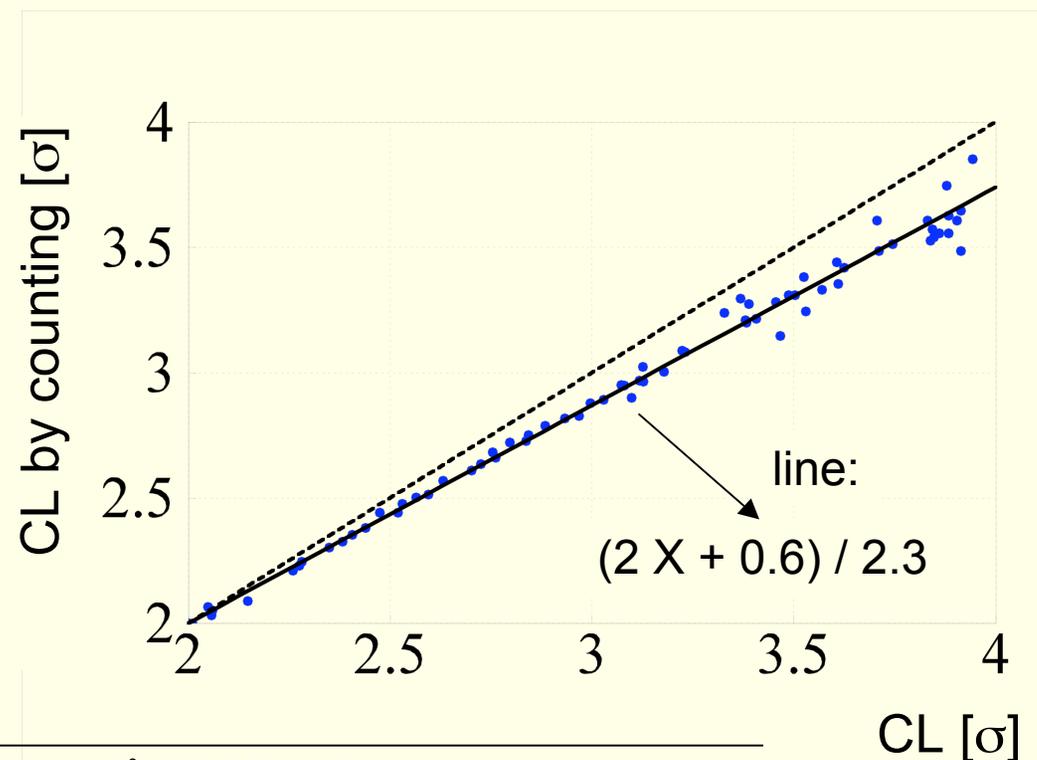


# Integration area

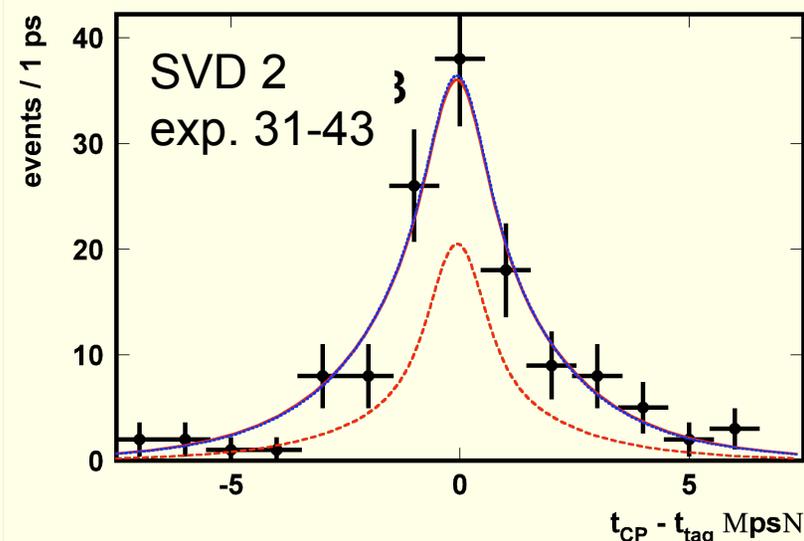
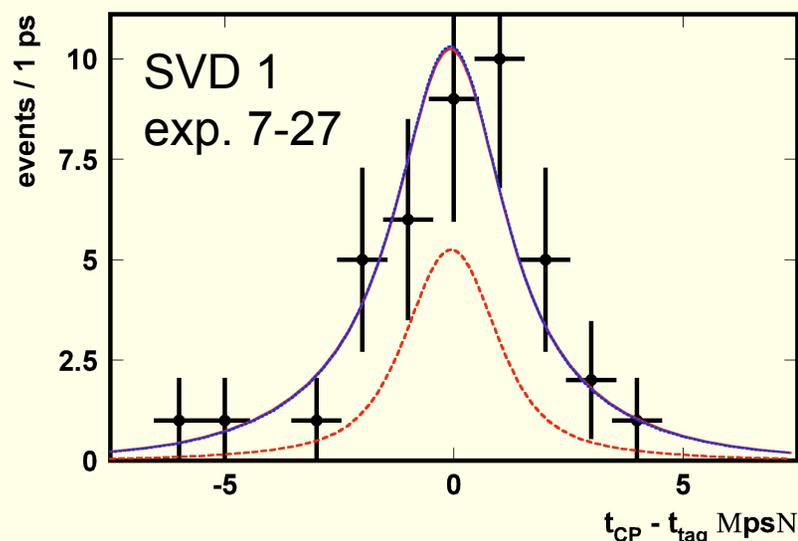


# Counting method

- $P(S, A | S^{\text{hyp}}, A^{\text{hyp}})$  is described by the Gaussian f.
- If the tails in the distributions are wider than is the case of the Gaussian distr., this would lead to an over-estimation of the significance
- One can obtain the CL also by counting the fraction of toy MC samples satisfying the F-C ordering principle ( $N(\Omega)/N(\text{all})$  instead of  $\int_{\Omega}$ ; larger fluctuations)



# $B^0 \rightarrow D^+D^-$ exp. 7-49 data sample lifetime and CP-blind fit



## Lifetime fit

7-27	$1.58 \pm 0.40$ ps
31-49	$1.45 \pm 0.23$
7-49	$1.48 \pm 0.20$

## CP-blind fit

	S	A
$\mu$	0.018	0.015
$\sigma$	0.40	0.25
$\langle \text{err} \rangle$	0.38	0.24

# Time-integrated CP parameters (by unbinned ML fit for each r-bin)

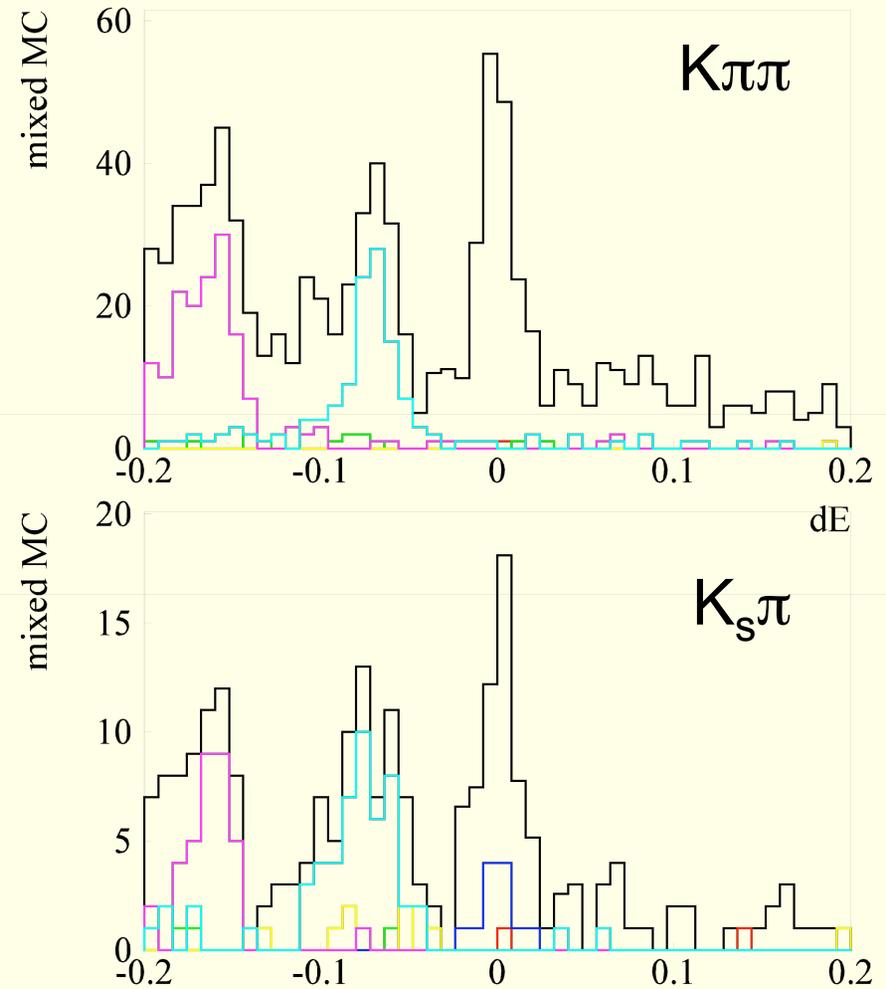
- Expected  $A$  (from  $A=0.90$ ) =  $(-\Delta w + (1 - 2 w) 0.626 A)$
- Error on meas.  $A$  estimated as  $1 / \text{sqrt} (N(B^0)+N(B^0\text{bar}))$

r-bin	$N(f_{\text{tag}}=B^0\text{bar})$	$N(f_{\text{tag}}=B^0)$	$\frac{N_{\text{tag}=B^0} - N_{\text{tag}=B^0\text{bar}}}{N_{\text{tag}=B^0} + N_{\text{tag}=B^0\text{bar}}}$	expect. $A$
1	13	33	$0.43 \pm 0.15$	0.03
2	7	7	$0.03 \pm 0.26$	0.23
3	5	5	$0.02 \pm 0.31$	0.29
4	5	13	$0.47 \pm 0.24$	0.37
5	4	7	$0.25 \pm 0.30$	0.47
6	6	19	$0.54 \pm 0.20$	0.54

# $\Delta E$ background study

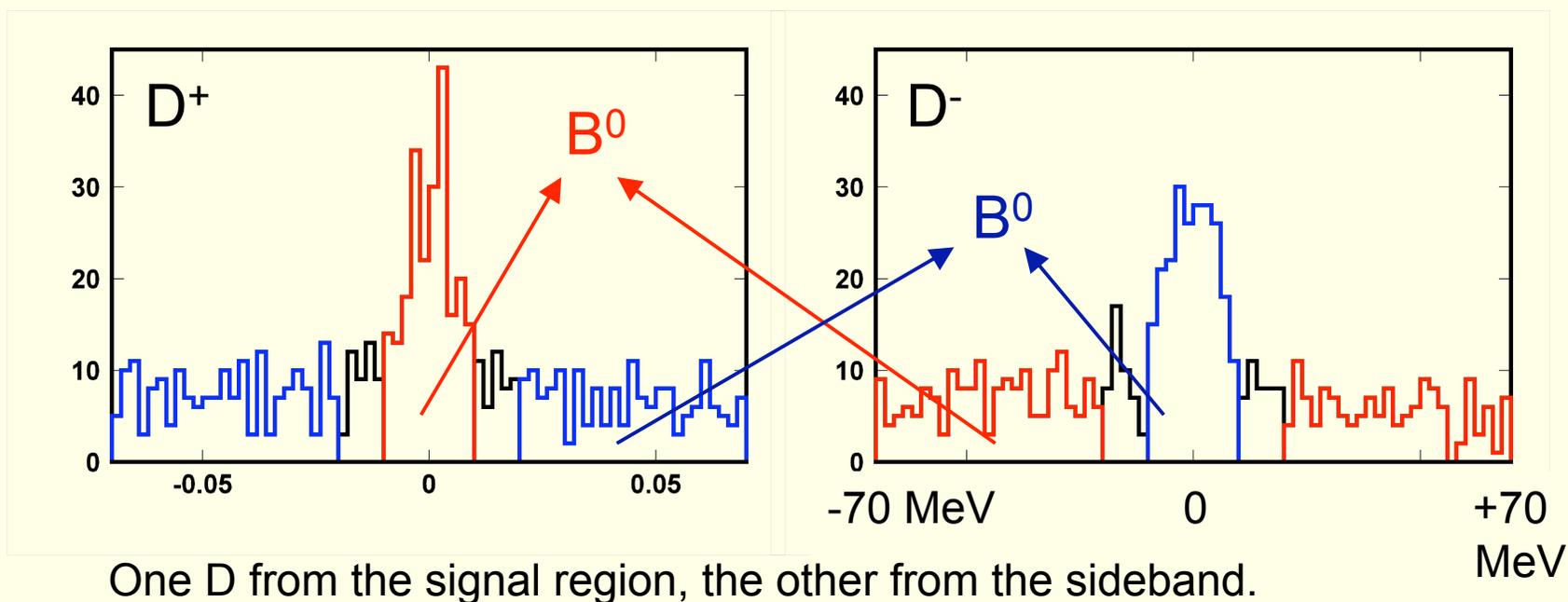
- Contributions of different backgrounds in  $\Delta E$  distribution for  $K\pi\pi$  and  $K_s\pi$  channel

- $B^0 \rightarrow D^* D$
- $B^0 \rightarrow D_s^+ D^-$
- $B^0 \rightarrow D^- K^+ \bar{K}^{*0}(892)$
- $B^0 \rightarrow D^- K^+ \bar{K}^0$
- $B^0 \rightarrow D^- \pi^+ K^{*0}(892)$
- $B^0 \rightarrow D^- \pi^+ K^0$



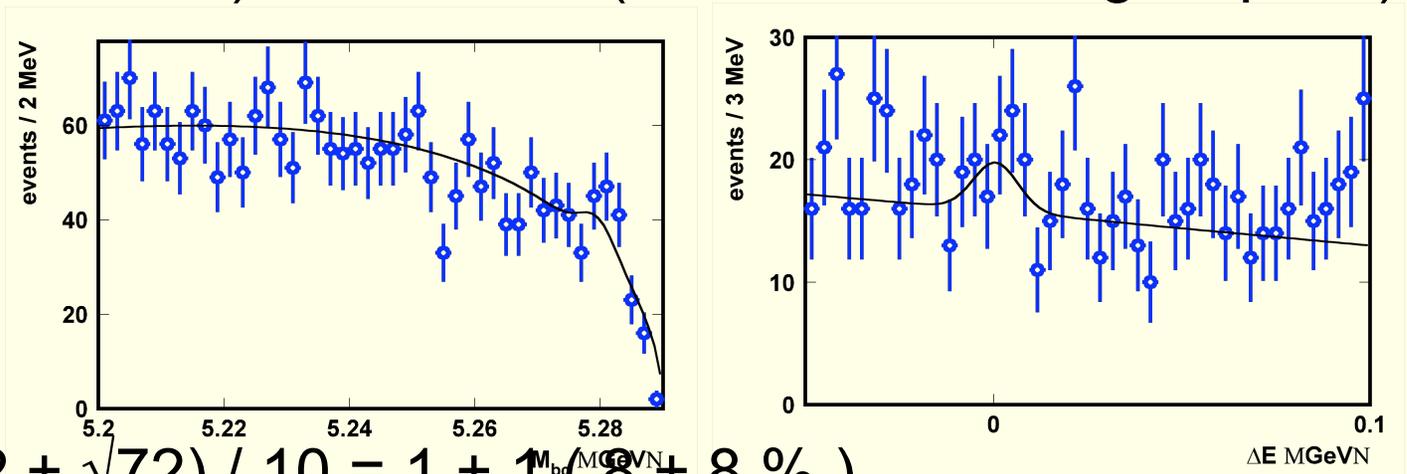
# Estimation of the peaking bkg. from the D-meson sidebands

- Evtgen MC studies indicated  $m_{BC} \Delta E$  peaking background in the  $K_S \pi$  reconstruction channel coming from the non-resonant  $B^0 \rightarrow D^- \pi^+ K^0$  decays
- Estimate its amount from the D-meson sideband study

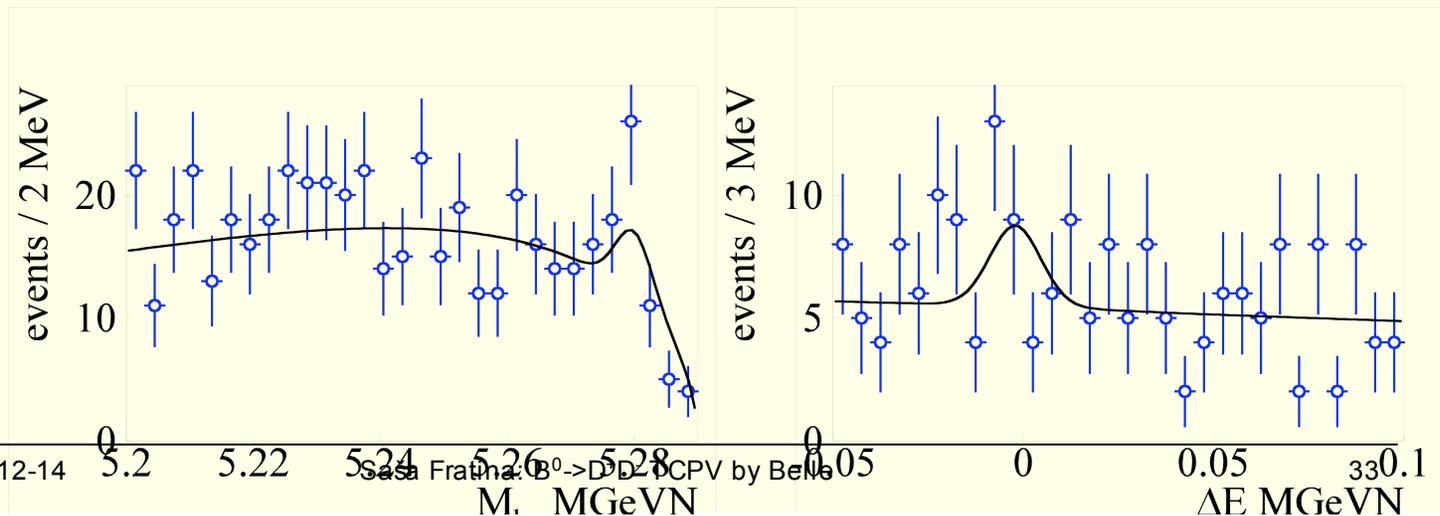


# Unbinned 2D ML fit to the $m_{BC}$ and $\Delta E$ distribution for the D-meson sidebands

- $K\pi\pi$ :  $(20 \pm \sqrt{315}) / 10 = 2 \pm 2$  (  $2 \pm 2$  % of the signal peak )



- $K_S\pi$ :  $(12 \pm \sqrt{72}) / 10 = 1 \pm 1$  (  $8 \pm 8$  % )



# D mass sideband plots

Right: D mass ( - D nominal mass), best r-bin, Mbc dE sideband

Bottom: mBC plots, D mesons: signal / sideband combinations, different r-ranges

