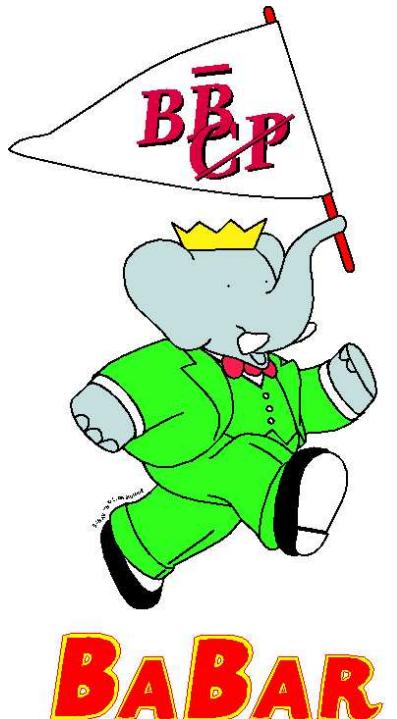


# *BABAR* status and prospects for $CP$ asymmetry measurements: $\sin(2\beta + \gamma)$

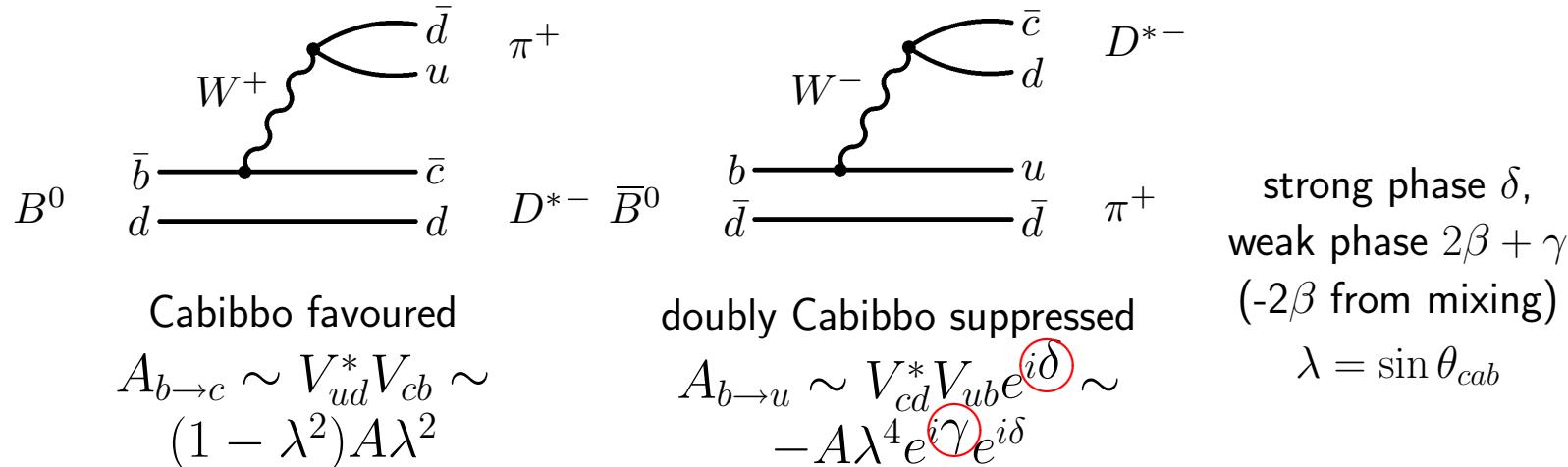
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*December 13, 2006  
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Nagoya, Japan*

- ☞ The  $B$  decays relevant to the  $\sin(2\beta + \gamma)$  have either small branching fraction ( $B \rightarrow D^{(*)} K^{(*)}$ ) or a small asymmetry ( $B \rightarrow D^{(*)} \pi/\rho/a_1$ )



- ☞ Contribution from only pure tree decays (no penguin)

☞ Time evolution:

$$P(B^0 \rightarrow D^{*\mp} \pi^\pm, \Delta t) \propto 1 \pm C \cos(\Delta m_d \Delta t) + S^\mp \sin(\Delta m_d \Delta t)$$

$$P(\bar{B}^0 \rightarrow D^{*\mp} \pi^\pm, \Delta t) \propto 1 \mp C \cos(\Delta m_d \Delta t) - S^\pm \sin(\Delta m_d \Delta t)$$

$$S^\pm = \frac{2r}{1+r^2} \sin(2\beta + \gamma \pm \delta) \quad C = \frac{1-r^2}{1+r^2} \approx 1$$

$$r = \frac{A(\bar{B}^0 \rightarrow D^{*-} \pi^+)}{A(B^0 \rightarrow D^{*-} \pi^+)} \approx 0.02$$

- ☞ small  $CP$  violating asymmetries

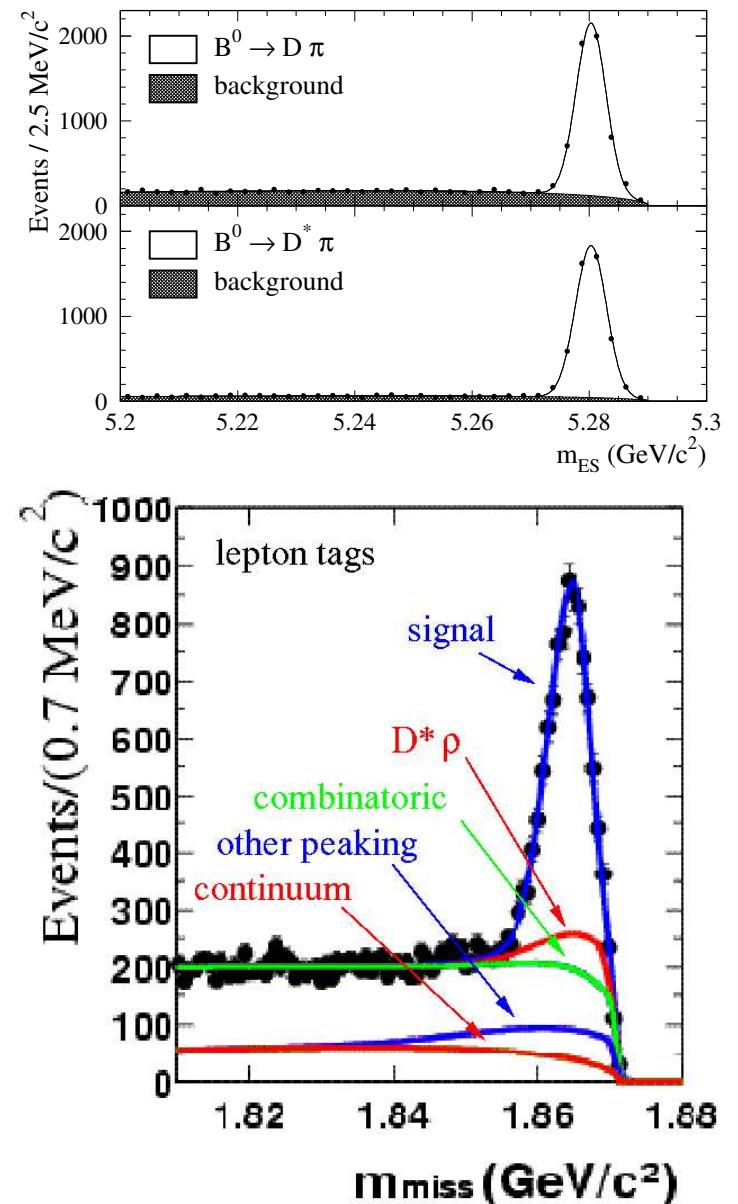
- ☞  $r$  can not be extracted fitting  $C$  ( $1 - C \sim 10^{-4}$ )

- ☞  $CP$  asymmetry is small  $\Rightarrow$  statistics is crucial
- ☞ Two methods of the reconstruction:
- ☞ **exclusive**: low background

☞ **partial reconstruction**:  
 increases efficiency  
 about  $\times 10$

$B^0 \rightarrow \pi_f^+ D^{*-} \rightarrow \bar{D}^0 \pi_s^- X$

Sample	Yields	Purity
Fully Reconstructed $(232 \text{ M } B\bar{B})$		
$D^\pm \pi^\mp$ (all tag)	$15038 \pm 132$	87%
$D^{*\pm} \pi^\mp$ (all tag)	$14002 \pm 123$	93%
$D^\pm \rho^\mp$ (all tag)	$8736 \pm 101$	82%
Partially Reconstructed $(232 \text{ M } B\bar{B})$		
$D^{*\pm} \pi^\mp (\ell)$	$18705 \pm 273$	54%
$D^{*\pm} \pi^\mp (K)$	$70584 \pm 661$	31%



# Exclusive $B^0 \rightarrow D^{(*)\mp} \pi^\pm / \rho^\pm$

- ☞ exclusive reconstruction [Phys.Rev.D 73, 111101 (2006)]
- ☞ presence of the DCS decays on tag-side introduces extra  $CP$ -violation [Phys.Rev.D 68, 034010 (2003)]
  - ➡ use abc-parameterization

$$\begin{aligned} a &= 2r \sin(2\beta + \gamma) \cos \delta \\ b &= 2r' \sin(2\beta + \gamma) \cos \delta' \\ c &= 2 \cos(2\beta + \gamma)(r \sin \delta - r' \sin \delta') \end{aligned}$$

- ☞ PDF includes combinatorial and peaking background
- ☞ fit all decay samples and tagging categories simultaneously (assume  $r' = 0$  for lepton tag)

$$a^{D\pi} = -0.010 \pm 0.023 \pm 0.007$$

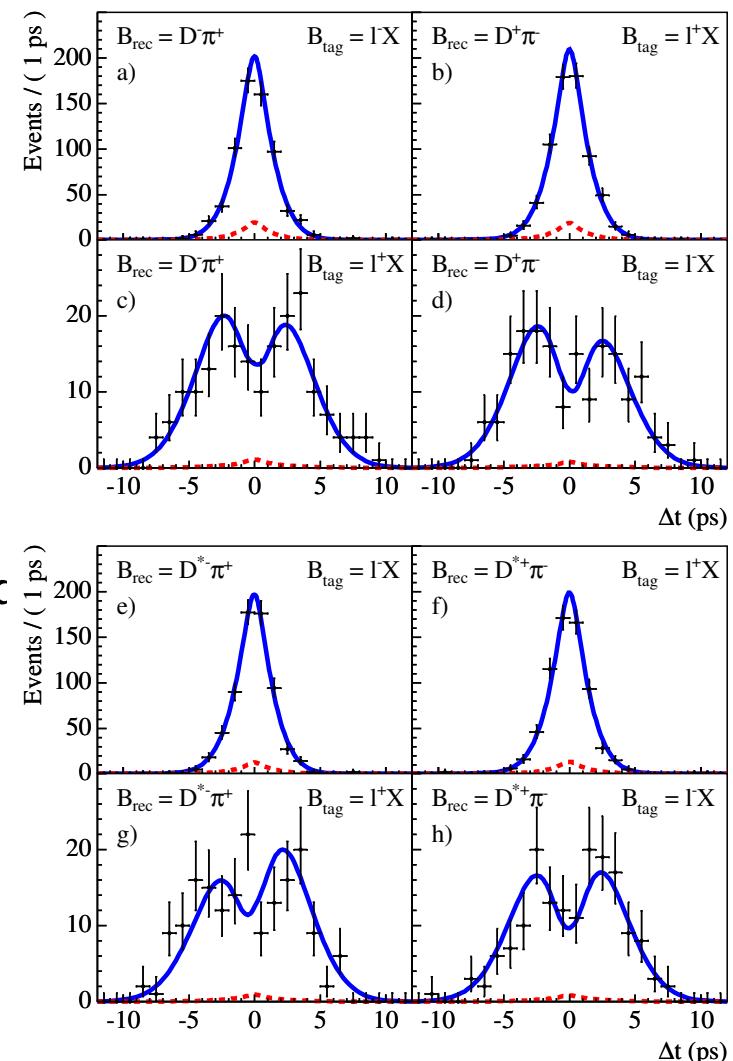
$$c_{\text{lep}}^{D\pi} = -0.033 \pm 0.042 \pm 0.012$$

$$a^{D^*\pi} = -0.040 \pm 0.023 \pm 0.010$$

$$c_{\text{lep}}^{D^*\pi} = 0.049 \pm 0.042 \pm 0.015$$

$$a^{D\rho} = -0.024 \pm 0.031 \pm 0.009$$

$$c_{\text{lep}}^{D\rho} = -0.098 \pm 0.055 \pm 0.018$$



☞ 3-Gaussian resolution function

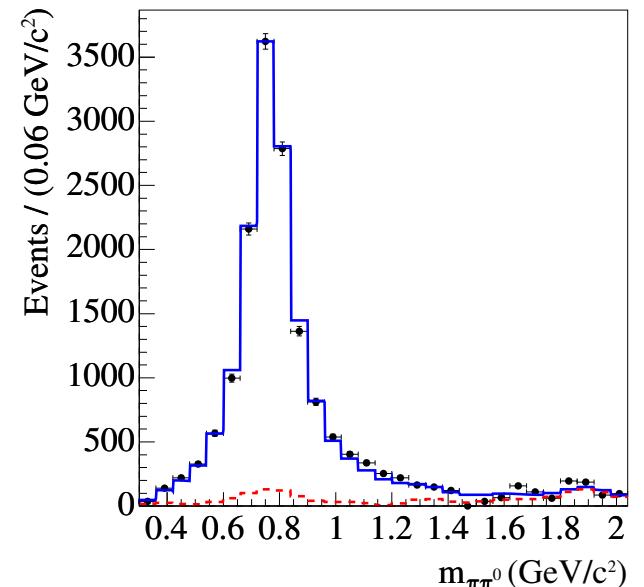
## Exclusive $B^0 \rightarrow D^{(*)\mp}\pi^\pm/\rho^\pm$ (Systematics)

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☞ Dominant systematic error  $\Rightarrow$  vertexing

- ➡ SVT misalignment, resolution function;
- ➡ beam spot position and z-scale uncertainty.

$B^0$ mode	$D^\pm\pi^\mp$		$D^{*\pm}\pi^\mp$		$D^\pm\rho^\mp$	
Source	$\sigma_a$	$\sigma_c$	$\sigma_a$	$\sigma_c$	$\sigma_a$	$\sigma_c$
Vertexing ( $\sigma_{\Delta t}$ )	0.37	0.64	0.80	1.14	0.47	1.15
Fit ( $\sigma_{\text{fit}}$ )	0.51	0.95	0.52	0.99	0.75	1.34
Model ( $\sigma_{\text{mod}}$ )	0.12	0.13	0.12	0.13	0.01	0.18
Tagging ( $\sigma_{\text{tag}}$ )	0.07	0.16	0.11	0.14	0.06	0.12
Background ( $\sigma_{\text{bkg}}$ )	0.13	0.10	0.10	0.09	0.28	0.29
$m_{\pi\pi^0}$ Dependence ( $\sigma_\lambda$ )	—	—	—	—	0.16	0.16
Total ( $\sigma_{\text{tot}}$ )	0.66	1.17	0.97	1.53	0.94	1.81

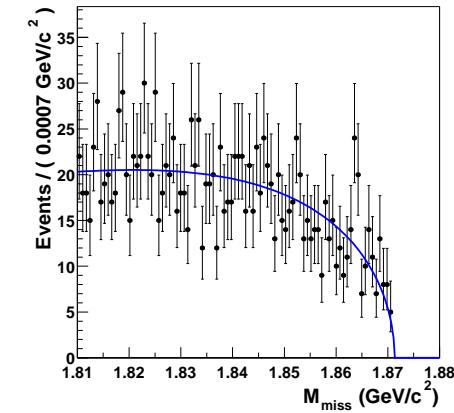
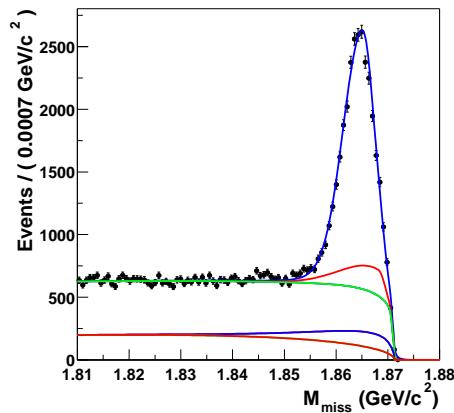


☞ In case of  $B^0 \rightarrow D^\mp\rho^\pm$  two additional background components were considered:  $B^0 \rightarrow D^\mp\rho^\pm(1450)$  and  $B^0 \rightarrow D^\mp\pi^\pm\pi^0$  (non-resonant S-wave)

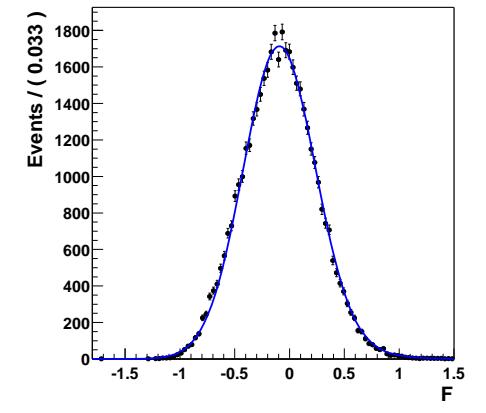
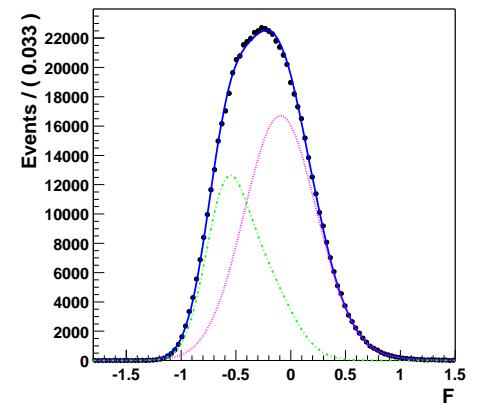
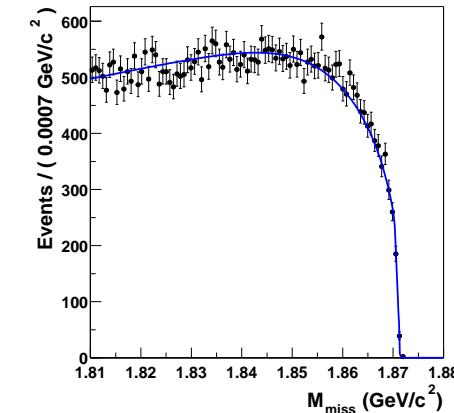
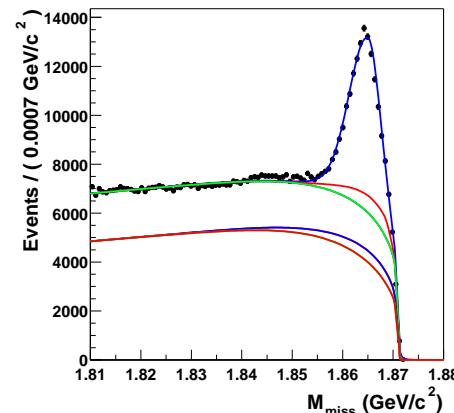
➡  $f(D^\mp\rho^\pm(1450) + D^\mp\pi^\pm\pi^0) < 0.02$  at 90% CL

# Inclusive $B^0 \rightarrow D^{*\mp} \pi^\pm$ (Kinematical Fit)

## Lepton tag



## Kaon tag



👉  $211.4 \text{ fb}^{-1}$  (on-res.) ( $232 \text{ M } B\bar{B}$ ) and  $21.7 \text{ fb}^{-1}$  (off-res.)

👉 All PDF parameters are extracted from the data.

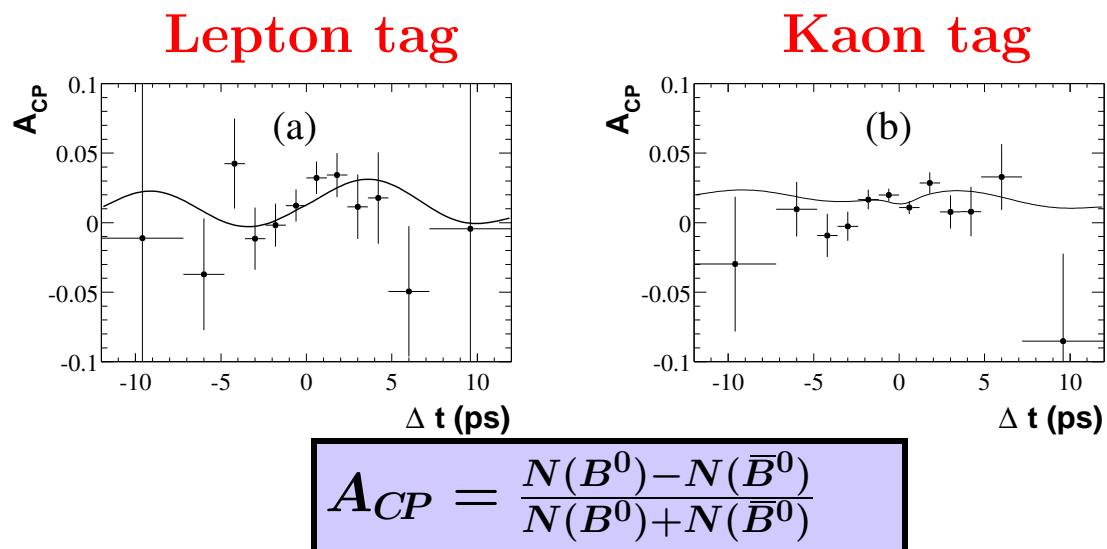
# Inclusive $B^0 \rightarrow D^{*\mp} \pi^\pm$ (Fit results)

## Lepton-tagged

$2r \sin(2\beta + \gamma) \cos \delta^*$	<b>-0.042 ± 0.019 ± 0.010</b>
$2r \cos(2\beta + \gamma) \sin \delta^*$	<b>-0.019 ± 0.022 ± 0.013</b>

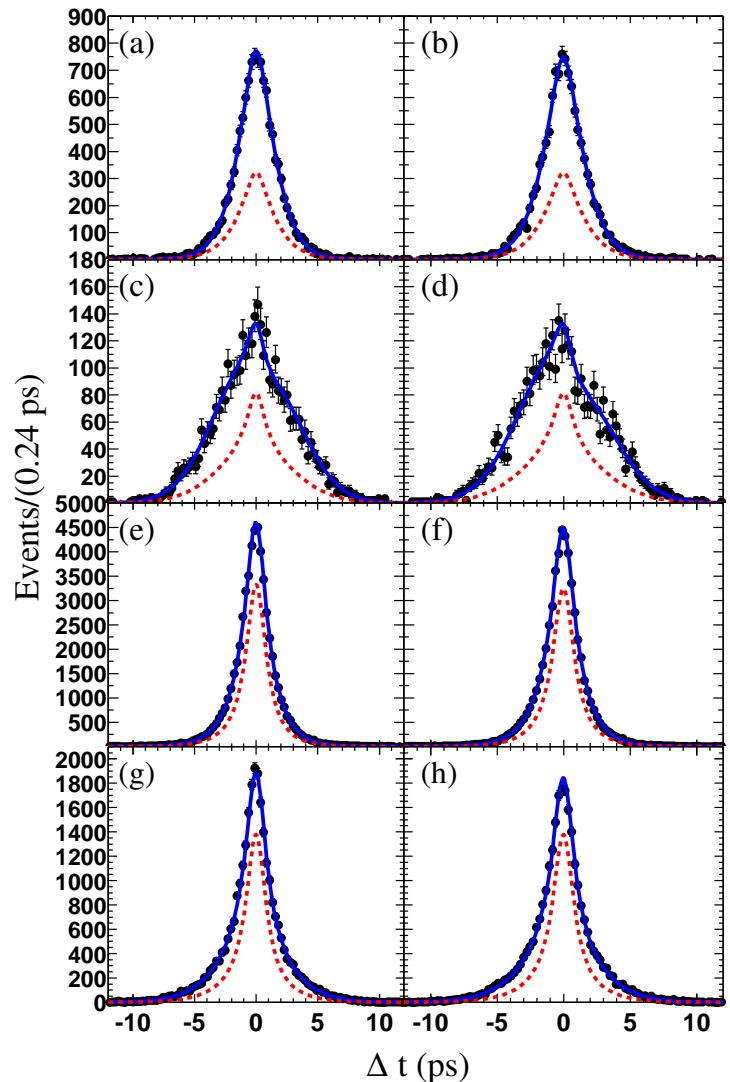
## Kaon-tagged

$2r \sin(2\beta + \gamma) \cos \delta^*$	<b>-0.025 ± 0.020 ± 0.013</b>
$2r' \sin(2\beta + \gamma) \cos \delta'$	<b>-0.004 ± 0.010 ± 0.010</b>
$2 \cos(2\beta + \gamma)(r \sin \delta^* - r' \sin \delta')$	<b>-0.002 ± 0.020 ± 0.015</b>



☞ The most precise time-dependent  $CP$  asymmetry measurement [Phys.Rev.D 71, 112003 (2005)]

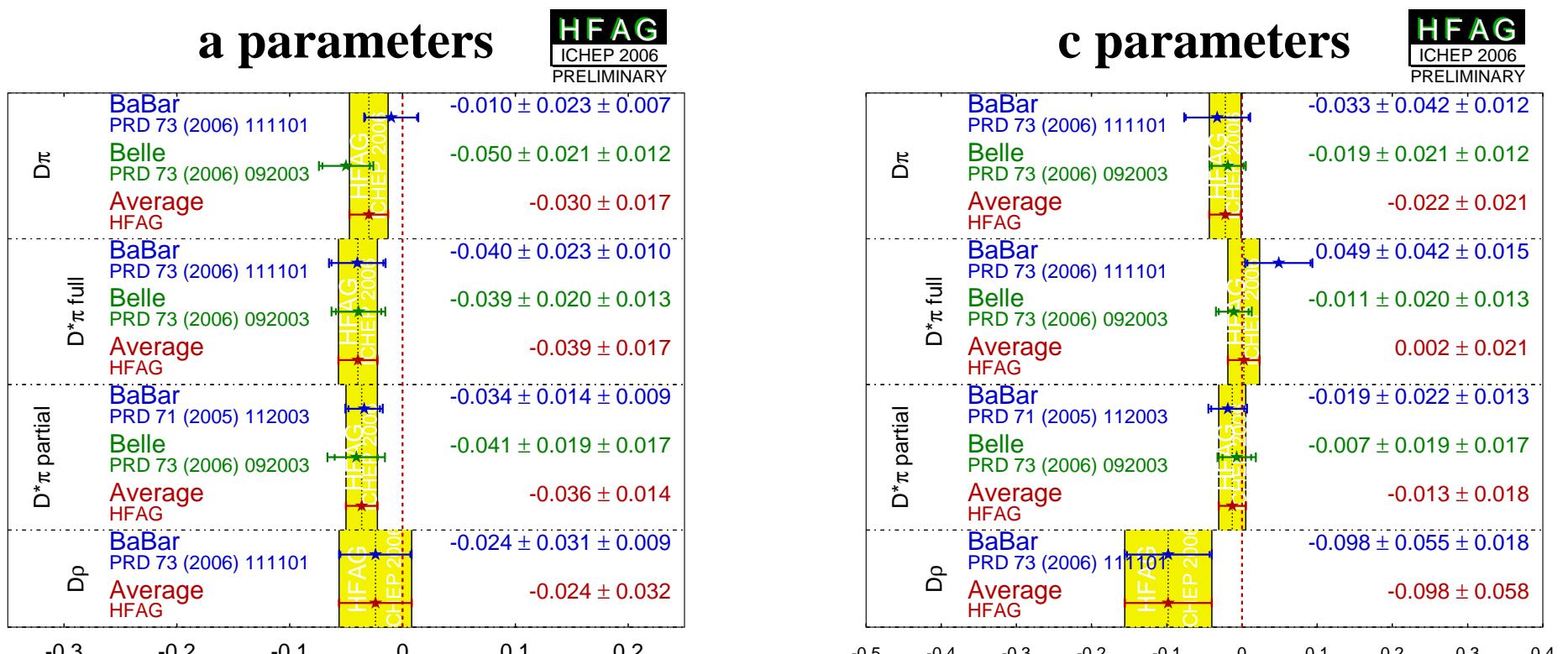
$$2r \sin(2\beta + \gamma) \cos \delta = -0.034 \pm 0.014 \pm 0.009$$



# Inclusive $B^0 \rightarrow D^{*\mp} \pi^\pm$ (Systematics)

Source	Error ( $\times 10^{-2}$ )				
	Lepton-tagged		Kaon-tagged		
	$a_{D^*\pi}^\ell$	$c_{D^*\pi}^\ell$	$a_{D^*\pi}^K$	$b_{D^*\pi}^K$	$c_{D^*\pi}^K$
1. Step 1 fit	0.04	0.04	0.10	0.04	0.04
2. Sideband statistics	0.08	0.08	0.40	0.12	0.44
3. $f_{D^*\pi}^{\text{miss}}$	0.02	0.02	0.02	negl.	negl.
4. $\rho_{D^*\pi}$	0.02	0.02	0.02	negl.	negl.
5. MC statistics	0.60	0.82	0.68	0.34	0.70
6. Beam spot size	0.10	0.10	0.07	0.13	0.06
7. Detector $z$ scale	0.03	0.03	0.02	negl.	0.03
8. Detector alignment	0.25	0.55	0.25	0.13	0.41
9. Combinatoric background $CP$ content	0.25	0.22	0.80	0.56	0.72
10. Peaking background $CP$ content	0.36	0.38	0.29	0.17	0.27
11. $D^*\rho$ $CP$ content	0.53	0.52	0.57	0.58	0.58
12. Peaking background	0.21	0.31	0.21	0.41	0.31
13. Signal region/sideband difference	0.0003	0.002	0.04	0.03	0.05
14. $\mathcal{B}(B \rightarrow D^{*\mp} \rho^\pm)$	0.17	0.33	0.17	0.22	0.33
Total systematic error	1.0	1.3	1.4	1.0	1.5
Statistical uncertainty	1.9	2.2	2.0	1.0	2.0

☞ Measure  $CP$ -violation in  $D^*\rho$  would minimize  $CP$  content systematics

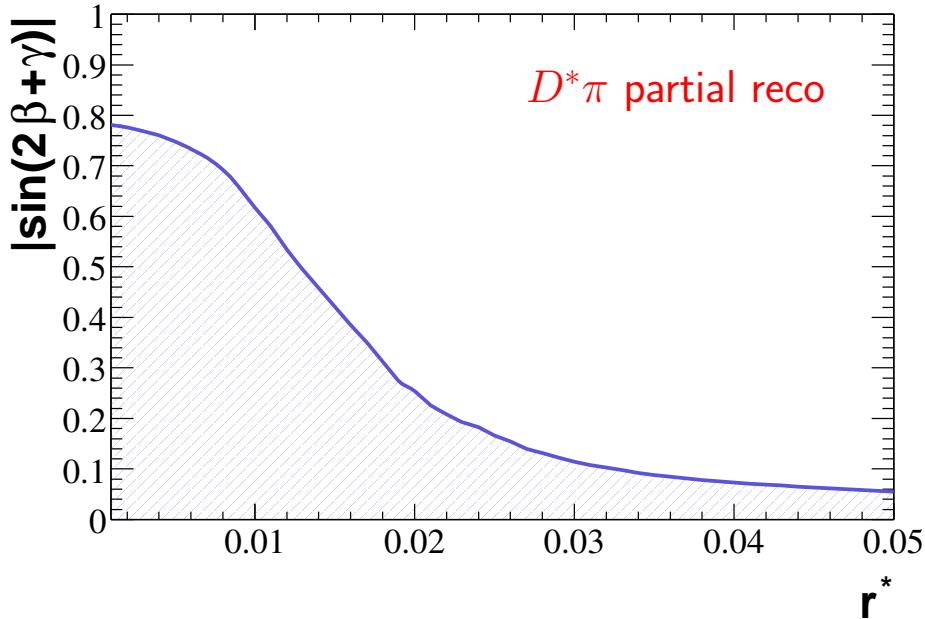


☞ Combined *BABAR/BELLE* result for  $B^0 \rightarrow D^{*\mp} \pi^\pm$  decays

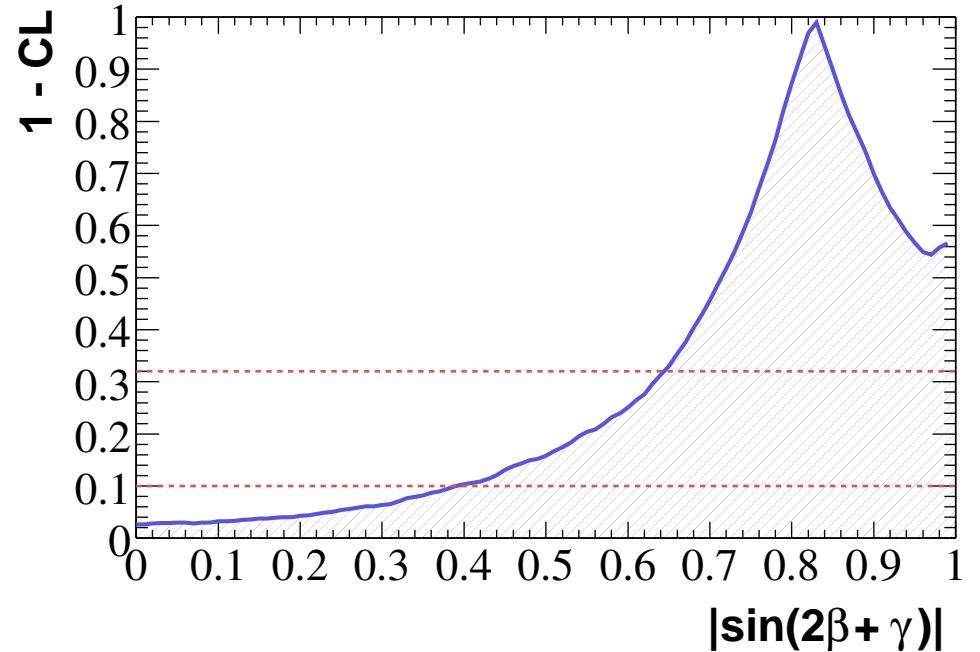
$$2r^{D^*\pi} \sin(2\beta + \gamma) \cos \delta = -0.037 \pm 0.011$$

## $\sin(2\beta + \gamma)$ Constraint

- ☞ Use frequentistic approach
- ☞ Two methods of interpretation:
  - ➡  $|\sin(2\beta + \gamma)|$  limit vs.  $r^{D^*\pi}$ ;
  - ➡ use SU(3) symmetry to constraint  $r$ ;



A lower 90% C.L. limit on  $|\sin(2\beta + \gamma)|$

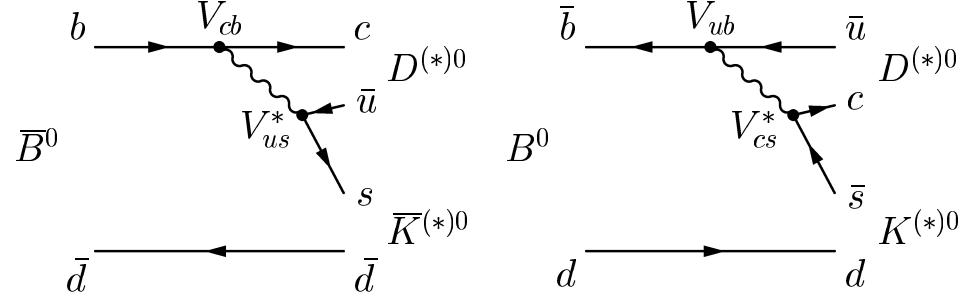


- ☞ Estimate  $r$  from  $\mathcal{B}(B \rightarrow D_s^{(*)+}\pi^-)$  with additional 30% error due to SU(3) breaking

$r^{D\pi} = 0.020 \pm 0.003$
$r^{D^*\pi} = 0.015^{+0.004}_{-0.006}$
$r^{D\rho} = 0.006 \pm 0.003$

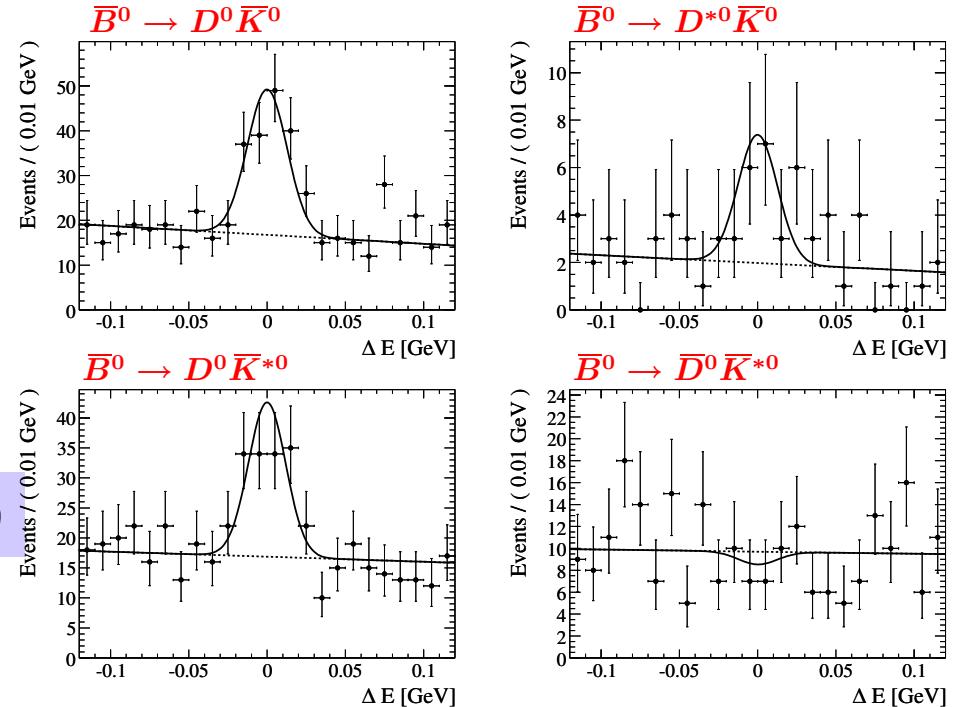
$|\sin(2\beta + \gamma)| > 0.40, 90\% \text{CL}$

# Perspectives $(\bar{B}^0 \rightarrow D^{(*)0} \bar{K}^{(*)0})$



- ☞ Small  $\mathcal{B} \sim \mathcal{O}(10^{-5})$ , estimate from  
 $\mathcal{B}(\bar{B}^0 \rightarrow D^{*0} \bar{K}^{*0}) \simeq \sin \theta_c \mathcal{B}(\bar{B}^0 \rightarrow D^{*0} \pi^0)$
- ☞ Expect  $r \sim 0.4 \Rightarrow$  enable to fit  $C$
- ☞ Use 226 M  $B\bar{B}$  [Phys.Rev.D 74, 031101 (2006)]

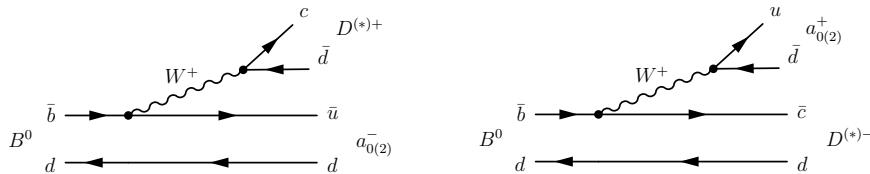
$$\begin{aligned}\mathcal{B}(\bar{B}^0 \rightarrow D^0 \bar{K}^0) &= (5.3 \pm 0.7 \pm 0.3) \times 10^{-5} \\ \mathcal{B}(\bar{B}^0 \rightarrow D^{*0} \bar{K}^0) &= (3.6 \pm 1.2 \pm 0.3) \times 10^{-5} \\ \mathcal{B}(\bar{B}^0 \rightarrow D^0 \bar{K}^{*0}) &= (4.0 \pm 0.7 \pm 0.3) \times 10^{-5} \\ \mathcal{B}(\bar{B}^0 \rightarrow \bar{D}^0 \bar{K}^{*0}) &< 1.1 \times 10^{-5} \text{ at 90% C.L.}\end{aligned}$$



$$R = \frac{\Gamma([K^+ \pi^-]_D \bar{K}^{*0})}{\Gamma([K^- \pi^+]_D \bar{K}^{*0})} = r_B^2 + r_D^2 + 2r_B r_D \cos(\gamma + \delta_i)$$

- ☞ Bayesian constraint from observables  
 $r_B < 0.40$  at 90% C.L.
- ☞ Substantially larger data sample is required for  $\sin(2\beta + \gamma)$  measurement

☞ Expect large  $CP$  asymmetry ( $r \sim 1$ )



Cabibbo suppressed  
isospin favoured

Cabibbo favoured  
isospin suppressed

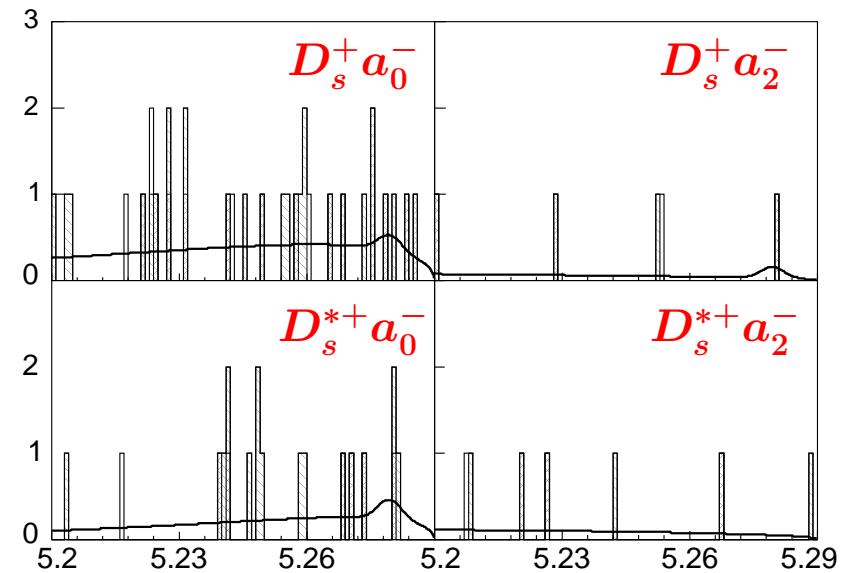
☞ Search  $B^0 \rightarrow D_s^\mp a_{0,2}^\pm$  (SU(3) conjugate)  
that have larger  $\mathcal{B}$

☞ Naive factorization:

$$\begin{aligned}\mathcal{B}(B^0 \rightarrow D_s^\mp a_0^\pm) &\simeq 8 \cdot 10^{-5} \\ \mathcal{B}(B^0 \rightarrow D_s^\mp a_2^\pm) &\simeq 1.5 \cdot 10^{-5}\end{aligned}$$

☞ Reconstruction modes:

- ⇒  $D_s^+ \rightarrow \phi \pi^+, \bar{K}^{*0} K^+ K_S^0 K^+$
- ⇒  $a_{0,2}^+ \rightarrow \eta \pi^+ (\mathcal{B}=100, 15\%)$



☞ Use 230 M  $B\bar{B}$  [Phys.Rev.D 73, 071103 (2006)]

☞ Upper limits at 90% C.L.

$$\begin{aligned}\mathcal{B}(B^0 \rightarrow D_s^+ a_0^-) &< 1.9 \cdot 10^{-5} \\ \mathcal{B}(B^0 \rightarrow D_s^+ a_2^-) &< 1.9 \cdot 10^{-4} \\ \mathcal{B}(B^0 \rightarrow D_s^{*+} a_0^-) &< 3.6 \cdot 10^{-5} \\ \mathcal{B}(B^0 \rightarrow D_s^{*+} a_2^-) &< 2.0 \cdot 10^{-4}\end{aligned}$$

☞ Rule out the naive factorization

☞ Decay modes relevant to  $\sin(2\beta + \gamma)$  measurement:

- ⇒ extraction of  $r$  (talk M.Baak):  $B^0 \rightarrow D_s^{(*)+} \pi^- / \rho^-$ ,  $B^+ \rightarrow D_{(s)}^+ \pi^0$
- ⇒ model independent  $\sin(2\beta + \gamma)$  measurement with  $B^0 \rightarrow D^{*\mp} \rho^\pm$ 
  - time-dependent angular analysis with a fully reconstructed sample;
  - the interference term between different helicity amplitudes  $\propto r$ ;
  - enhance statistics with a partially reconstructed sample;
- ⇒ time-dependent Dalitz analysis (talk F.Polci):  $B^0 \rightarrow D^+ K^0 \pi^-$

☞ Could be done

- ⇒  $B^0 \rightarrow D^{*\mp} a_1^\pm$  resolves two-fold ambiguity in  $CP$  angles
- ⇒  $B^0 \rightarrow D^{**\mp} \pi^\pm$  CLEO partial reconstruction proved the principle

☞ **BABAR has very broad program to measure  $\sin(2\beta + \gamma)$**

☞ Available results with 232 M  $B\bar{B}$ :

- ⇒  $B^0 \rightarrow D^{(*)\mp} \pi^\pm$  and  $B^0 \rightarrow D^\mp \rho^\pm$  with full reconstruction technique
- ⇒  $B^0 \rightarrow D^{*\mp} \pi^\pm$  with partial reconstruction technique
  - uses both “lepton” and “kaon”  $B$  flavor tagging;
  - provides the most precise measurement of time-dependent  $CP$  asymmetry:

$$2r \sin(2\beta + \gamma) \cos \delta = -0.034 \pm 0.014 \pm 0.009$$

☞ The other analyses relevant to  $\sin(2\beta + \gamma)$

- ⇒  $\bar{B}^0 \rightarrow D^{(*)0} \bar{K}^{(*)0}$  (BF)
- ⇒  $B^0 \rightarrow D^{(*)\mp} a_{0,2}^\pm$  (BF of SU(3) partners )
- ⇒  $B^0 \rightarrow D^{*\mp} \rho^\pm$  (BF, lifetime,  $\Delta m$ , transversity)

☞ Other potential analyses could be done:

- ⇒  $B^0 \rightarrow D^{*\mp} a_1^\pm$
- ⇒  $B^0 \rightarrow D^{**\mp} \pi^\pm$

Backup slides

☞ Use a partial reconstruction technique for  $B^0 \rightarrow D^{*\mp} \pi^\pm$

### ☞ PDFs

➡ PDF for on-resonance data is a sum over the PDFs of the different event types:

$$\mathcal{P} = \sum_i f_i \mathcal{P}_i,$$

where the index  $i = \{D^* \pi, D^* \rho, \text{peak, comb}, q\bar{q}\}$

$$\mathcal{P}_i = \mathcal{M}_i(m_{\text{miss}}) \mathcal{F}_i(F) \mathcal{T}'_i(\Delta t, \sigma_{\Delta t}, s_t, s_m),$$

where  $s_t = 1(-1)$  for  $B^0(\bar{B}^0)$ ,  $s_m = 1(-1)$  for “unmixed” (“mixed”)

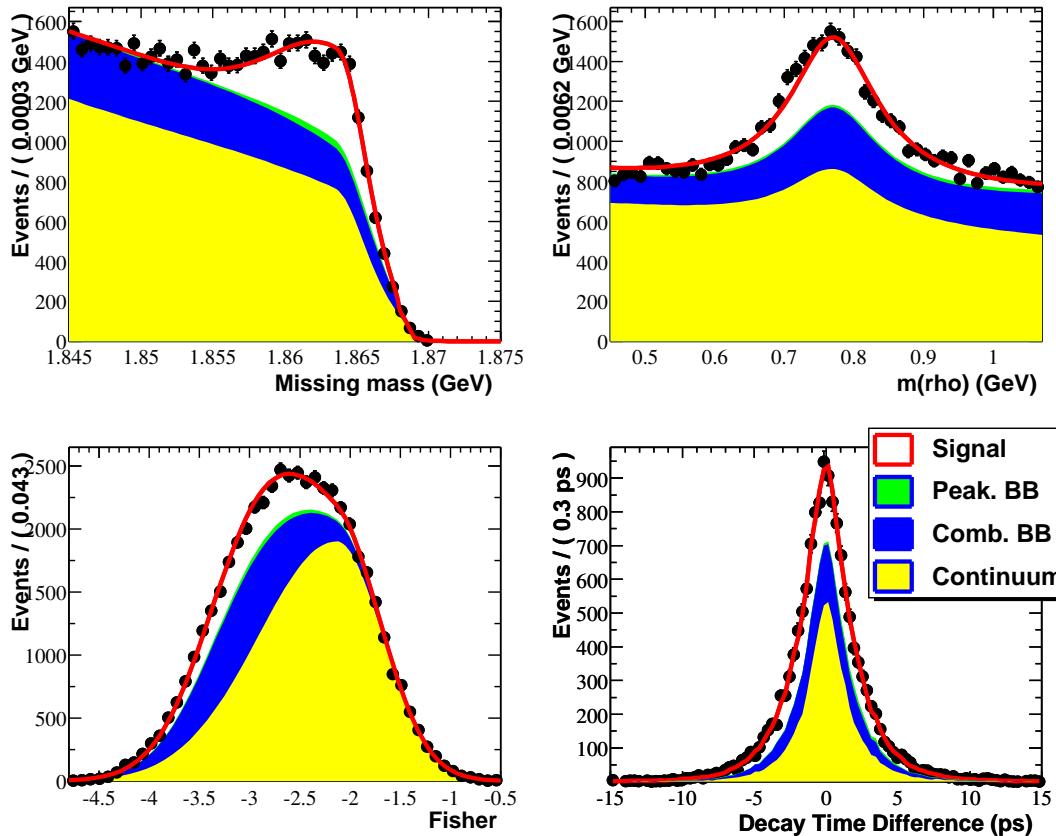
### ☞ Analysis steps:

- ➡ Determine  $f_i$ ,  $\mathcal{F}_{q\bar{q}}$ , and  $\mathcal{F}_{B\bar{B}}$  from the kinematical (KIN) fit:  $\mathcal{P}_i = \mathcal{M}_i(m_{\text{miss}}) \mathcal{F}_i(F)$
- ➡ Determine  $\mathcal{T}'_{\text{comb}}$  and  $\mathcal{T}'_{q\bar{q}}$  from fit of side-band (SB) region ( $1.81 < m_{\text{miss}} < 1.84 \text{ GeV}/c^2$ )
- ➡ Determine  $\mathcal{T}'_{D^* \pi}$  and  $\mathcal{T}'_{q\bar{q}}$  from signal-region fit ( $1.845 < m_{\text{miss}} < 1.880 \text{ GeV}/c^2$ ) using the results of the KIN and SB fits.

☞ All PDF parameters are extracted from the data.

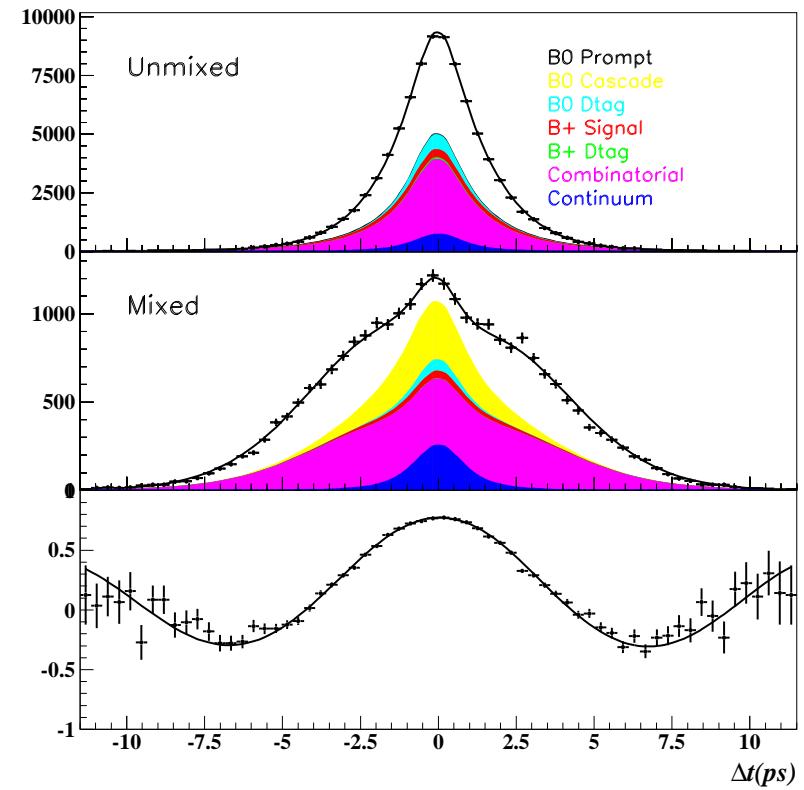
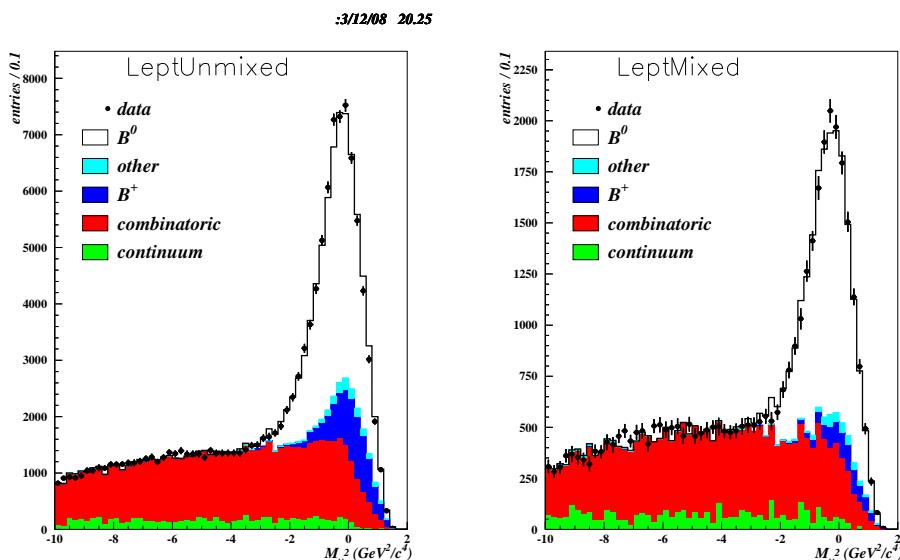
☞ Use abc-parameterization to take into account tag-side  $CP$ -violation effect.

$$\sin(2\beta + \gamma) \text{ with } B^0 \rightarrow D^{*\mp} \rho^\pm$$



- ☞  $20.7 \text{ fb}^{-1}$  - 5500 events
- ☞ In addition 690 peaked events from  $B^0 \rightarrow D^{*\mp} a_1^\pm$
- ☞  $q\bar{q}$  continuum is a dominant background
- ☞  $200 \text{ fb}^{-1}$  - about 55000 non-tagged signal events
- ☞  $200 \text{ fb}^{-1}$  - 6000 (20000) events for lepton (kaon) tag

- ☞ Only one decay amplitude for  $B^0 \rightarrow D^* \mp l^\pm \nu \Rightarrow$  no  $CP$ -violation
- ☞ Partial reconstruction provides large number of events (88 M  $B\bar{B}$ )
  - ➡ 117600 (561900)- lepton (kaon) tag
  - ➡ Expected statistical error  
 $\sigma[2r' \sin(2\beta + \gamma)] \sim 0.008$
- ☞ Use lepton tag as a validation check



- ☞ The most precise measurement of the lifetime and  $\Delta m$  [Phys.Rev.D 73, 012004 (2006)]

$\tau_{B_d} = 1.507 \pm 0.008 \pm 0.030 \text{ ps}$ 
 $\Delta m_{B_d} = 0.523 \pm 0.004 \pm 0.007 \text{ ps}^{-1}$